Since there may be English speaking students in the exam, the questions below are in English—just like in all previous exercises. Though, answers can be given in Finnish, of course.

## Assignment 1. (3 p)
Define *soft matter*. What distinguishes soft matter from other types of condensed matter, for example crystalline solids and standard liquids? Give three every-day examples of soft matter and explain why your examples classify as soft matter.

## Assignment 2. (9 p)
Explain the following concepts, terms and phenomena. Use drawings and/or essay-like descriptions to clarify the issue, when needed.

a) Discuss the common features between lipids and carbohydrates. (1 p).
b) Discuss Brownian motion. Write the Langevin equation for a Brownian particle and discuss the physical origin and interpretation of the terms appearing in the equation. (2 p)
c) Persistence length. What does the persistence length describe? How would you define that? (1 p)
d) Describe the Boltzmann distribution; what is it good for? (1 p)
e) Protein folding and protein denaturation. (1 p)
f) Describe biological situations where hydrogen bonds are important. (1 p)
g) Describe the main phases of liquid crystals, including drawings to highlight their structures. (2 p)

## Assignment 3. (6 p)
a) In the 19th century, Benjamin Franklin carried out an experiment where he was standing by the lake with a teaspoon of oil (volume about 5 cm$^3$). He allowed that quantity of oil to spread on water. He found that this amount of oil covered an area of 2000 m$^2$. Estimate the thickness of the oil layer floating on top of water. What is your conclusion for the structure of the layer?

b) The orientational properties of liquid crystal molecules (among others) are described by the order parameter
$$S = A\langle\cos^2\theta\rangle - B.$$

The conditions are that when the molecules are all aligned along the director (the direction of an external field), then $S = 1$, and if all molecules are randomly oriented, then $S = 0$. Compute the values of $A$ and $B$ that satisfy these conditions.

## Assignment 4. (6 p)
a) Assume that the density of your body is 1200 kg/m$^3$, which is a bit more than the density of water, 1000 kg/m$^3$ (here we assume that you have plenty of muscles, which we know to be true, and there is no air in your lungs). Compute the effective mass of your body when you are diving in a pool such that you are completely below water-level. (Remember to account for buoyancy.) You may consider yourself as a cylinder whose height is 170 cm and radius is 14 cm.

b) Next assume that you are swimming breaststroke such that your head is above water-level all the time (this is no good since it overburdens your neck) while the rest of your body is below water-level. If your head accounts for 7 % of your body weight, compute the effective mass of your whole body while swimming.

Using these data, interpret the importance of mass on a cellular level.

**Assignment 5.   (6 p)**
Answer <u>either</u> to part (a) <u>or</u> (b).

(a) Assemblies made of lipids are often predicted by the structure and form of individual lipids. The quantity derived for this purpose is the so-called "surfactant packing parameter" $N_s$ defined in terms of the head-group area of the lipid, the length of the lipid chain, and the volume of the lipid chain. Show that 1) for spherical micelles $N_s \leq 1/3$, 2) for cylindrical micelles (figure below, left) $1/3 < N_s \leq 1/2$, and 3) for liposomes (figure below, right) $1/2 < N_s < 1$.
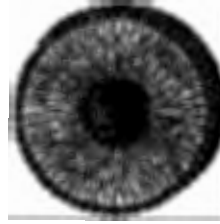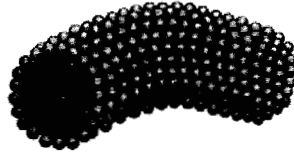


(b) b1. **Electrostatics.** Electrostatic interactions constitute one of the most important interaction types in soft and biological matter. Discuss what electrostatics actually is as well as its biological relevance.

b2. **Polymers.** Discuss what polymers are, and explain how their structure and dynamics can be characterized. Also consider what biological molecules are polymers, and give examples of polymers that can be used as carriers of drugs.

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These might be useful:
$\sin 2x = 2 \sin x \cos x$
$\sin 3x = 3 \sin x - 4 \sin^3 x$
$\cos 2x = 1 - 2 \sin^2 x$
$\cos 3x = 4 \cos^3 x - 3 \cos x$

Taylor expansion $(1 + x)^{-1/2} \approx 1 - \frac{1}{2}x + \frac{3}{8}x^2 + \mathcal{O}(x^3)$ for $|x| < 1$.

Boltzmann constant $1.380662 \cdot 10^{-23}$ J / K.

1 amu $= 1.66 \times 10^{-27}$ kg. (atomic mass unit)