

## 2<sup>nd</sup> Mid-Term Exam

### Answer 4 out of 5 questions

1. Explain the main features of the interaction of alpha- and beta- particles, and gamma-rays with matter (energy loss, path, range, straggling...)
2. a) In a PIXE experiment, a  $0.2 \text{ mg/cm}^2$  film containing 5 parts per million by weight of an element of mass number 100 is bombarded with a 200 nA beam of protons for 10 minutes. The cross section for exciting the L shell of the element is 800 barns and the probability of the excited atom emitting an L X-ray is 50%. Calculate the number of counts recorded if the overall detection efficiency is 0.5%.  
  
b) Calculate the mass of  $^{210}\text{Po}$  required to generate 10W of electric power using a thermoelectric converter that operates with an efficiency of 15%.  $^{210}\text{Po}$  has a half-life of 138 days and decays by alpha emission with an alpha decay Q-value of 5.4 MeV.
3. a) Draw a diagram showing the behavior of the stopping power or energy loss as a function of energy for a heavy charged particle (e.g. Hydrogen, Carbon, Lead, etc). The plot should go from very low to very high energy.  
  
b) Explain the main features of the plot.  
  
c) A beam of Ar ( $Z=18$ ) ions at an energy of 2 MeV/u is used to irradiate the following target materials: calcium ( $Z=20$ ), carbon ( $Z=6$ ), uranium ( $Z=92$ ) and tin ( $Z=50$ ). Write the list of target materials in order of increasing stopping power.
4. Explain very briefly (a couple of sentences):
  - a) What is meant by a compound-nucleus reaction? Give an example.
  - b) In calculating the reaction rate, i.e. the number of atoms/s expected in a typical nuclear structure experiment, what three important parameters are required?
  - c) There are 4 fundamental nuclear structure observables which may be obtained via laser spectroscopy. What are they?
  - d) A thermal neutron can induce fission in  $^{235}\text{U}$ . Why is the same mechanism not possible for  $^{238}\text{U}$ ?
  - e) Why is there a threshold energy in pair production and what is this energy?
  - f) Why is it not possible to identify light elements such as hydrogen in a Rutherford backscattering experiment?
5. a) List as many ingredients you believe necessary for successful (and safe) operation of a nuclear reactor. How is the energy extracted?

The graphite core of a fission reactor contains 1 atom of 1.5% enriched uranium fuel to every 500 atoms of carbon. In steady-state operation the reactor produces 3.5 MW of power for every tonne of fuel. The core is an intimate mixture of fuel and moderator.

- b). Calculate the neutron flux  $\phi$  in the core.
- c). Calculate the thermal neutron utilization factor  $f$ .

You may need the following data:

Recoverable energy per fission = 200 MeV

Cross section for thermal neutron-induced fission of  $^{235}\text{U}$   $\sigma_f = 579\text{b}$

Cross section for thermal neutron absorption in the fuel  $\sigma_a(\text{F}) = 12.9\text{ b}$

Cross section for thermal neutron absorption in graphite  $\sigma_a(\text{M}) = 0.0045\text{ b}$

**CONSTANTS**

Speed of light	$c$	$2.99792458 \times 10^8 \text{ m/s}$
Charge of electron	$e$	$1.602189 \times 10^{-19} \text{ C}$
Boltzmann constant	$k$	$1.38066 \times 10^{-23} \text{ J/K}$ $8.6174 \times 10^{-5} \text{ eV/K}$
Planck's constant	$h$	$6.62618 \times 10^{-34} \text{ J} \cdot \text{s}$ $4.13570 \times 10^{-15} \text{ eV} \cdot \text{s}$
	$\hbar = h/2\pi$	$1.054589 \times 10^{-34} \text{ J} \cdot \text{s}$ $6.58217 \times 10^{-16} \text{ eV} \cdot \text{s}$
Gravitational constant	$G$	$6.6726 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2$
Avogadro's number	$N_A$	$6.022045 \times 10^{23} \text{ mole}^{-1}$
Universal gas constant	$R$	$8.3144 \text{ J/mole} \cdot \text{K}$
Stefan-Boltzmann constant	$\sigma$	$5.6703 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4$
Rydberg constant	$R_\infty$	$1.0973732 \times 10^7 \text{ m}^{-1}$
Hydrogen ionization energy		$13.60580 \text{ eV}$
Bohr radius	$a_0$	$5.291771 \times 10^{-11} \text{ m}$
Bohr magneton	$\mu_B$	$9.27408 \times 10^{-24} \text{ J/T}$ $5.78838 \times 10^{-5} \text{ eV/T}$
Nuclear magneton	$\mu_N$	$5.05084 \times 10^{-27} \text{ J/T}$ $3.15245 \times 10^{-8} \text{ eV/T}$
Fine structure constant	$\alpha$	$1/137.0360$
	$hc$	$1239.853 \text{ MeV} \cdot \text{fm}$
	$\hbar c$	$197.329 \text{ MeV} \cdot \text{fm}$
	$e^2/4\pi\epsilon_0$	$1.439976 \text{ MeV} \cdot \text{fm}$

**PARTICLE REST MASSES**

	u	MeV/c <sup>2</sup>
Electron	$5.485803 \times 10^{-4}$	0.511003
Proton	1.00727647	938.280
Neutron	1.00866501	939.573
Deuteron	2.01355321	1875.628
Alpha	4.00150618	3727.409
$\pi^\pm$	0.1498300	139.5669
$\pi^0$	0.1448999	134.9745
$\mu$	0.1134292	105.6595

**CONVERSION FACTORS**

$1 \text{ eV} = 1.602189 \times 10^{-19} \text{ J}$	$1 \text{ b} = 10^{-28} \text{ m}^2$
$1 \text{ u} = 931.502 \text{ MeV}/c^2$ $= 1.660566 \times 10^{-27} \text{ kg}$	$1 \text{ Ci} = 3.7 \times 10^{10} \text{ decays/s}$