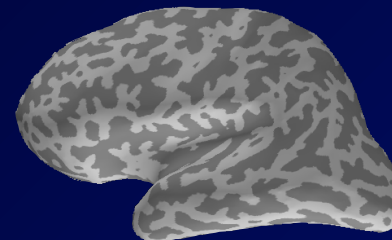


MEG/EEG Source Localization Methods

Matti Hämäläinen



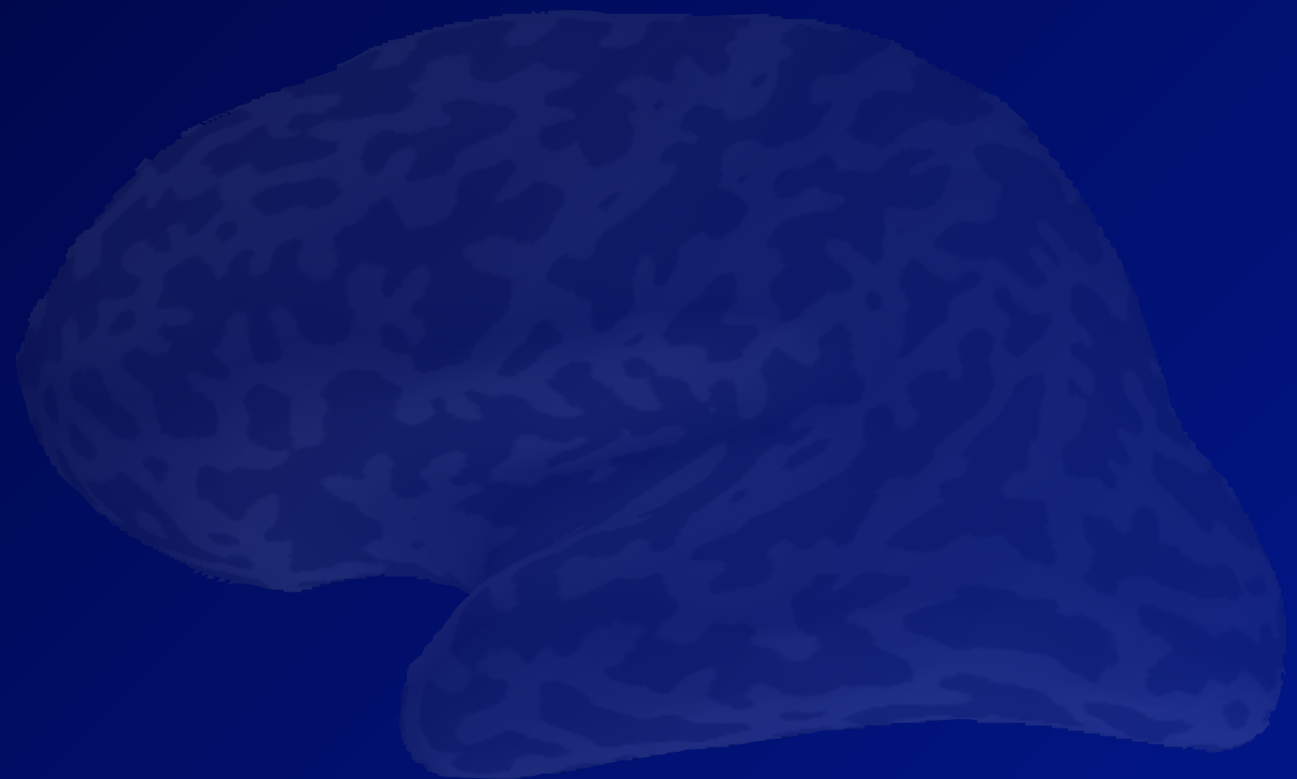
**MGH/MIT/HMS Athinoula A. Martinos Center for Biomedical Imaging
Charlestown, MA, USA**

**Brain Research Unit
Olli V. Lounasmaa Laboratory
Aalto University, School of Science
Espoo, Finland**



Contents

- Introduction to MEG and EEG source estimation
- Current dipole models
- Anatomically and functionally constrained source estimates



MEG and EEG source estimation



The Inverse Problem

Find the current distribution that generated the measured MEG/EEG

EEG/MEG

Equivalent
currents

The Inverse Problem

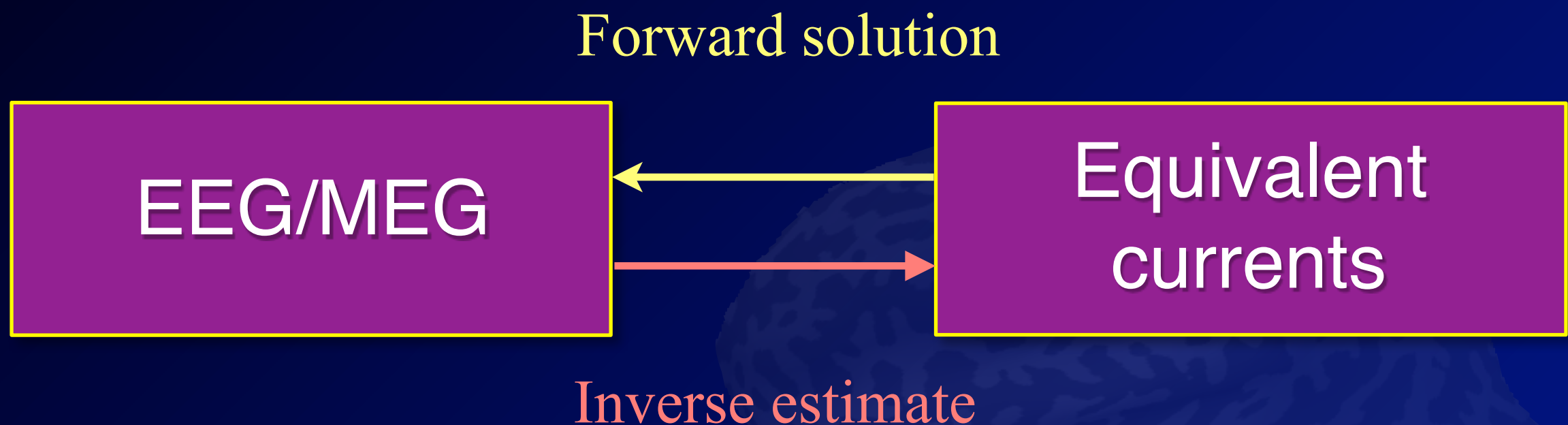
Find the current distribution that generated the measured MEG/EEG

Forward solution

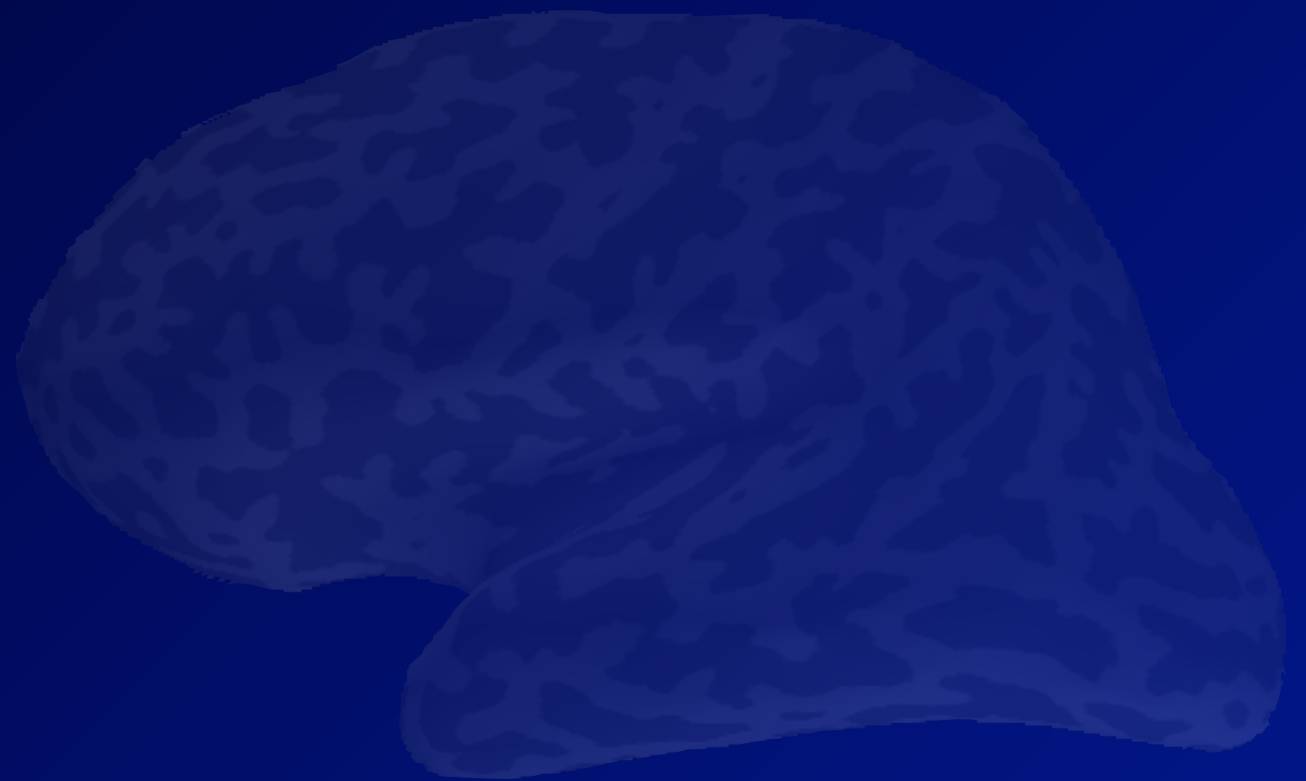


The Inverse Problem

Find the current distribution that generated the measured MEG/EEG



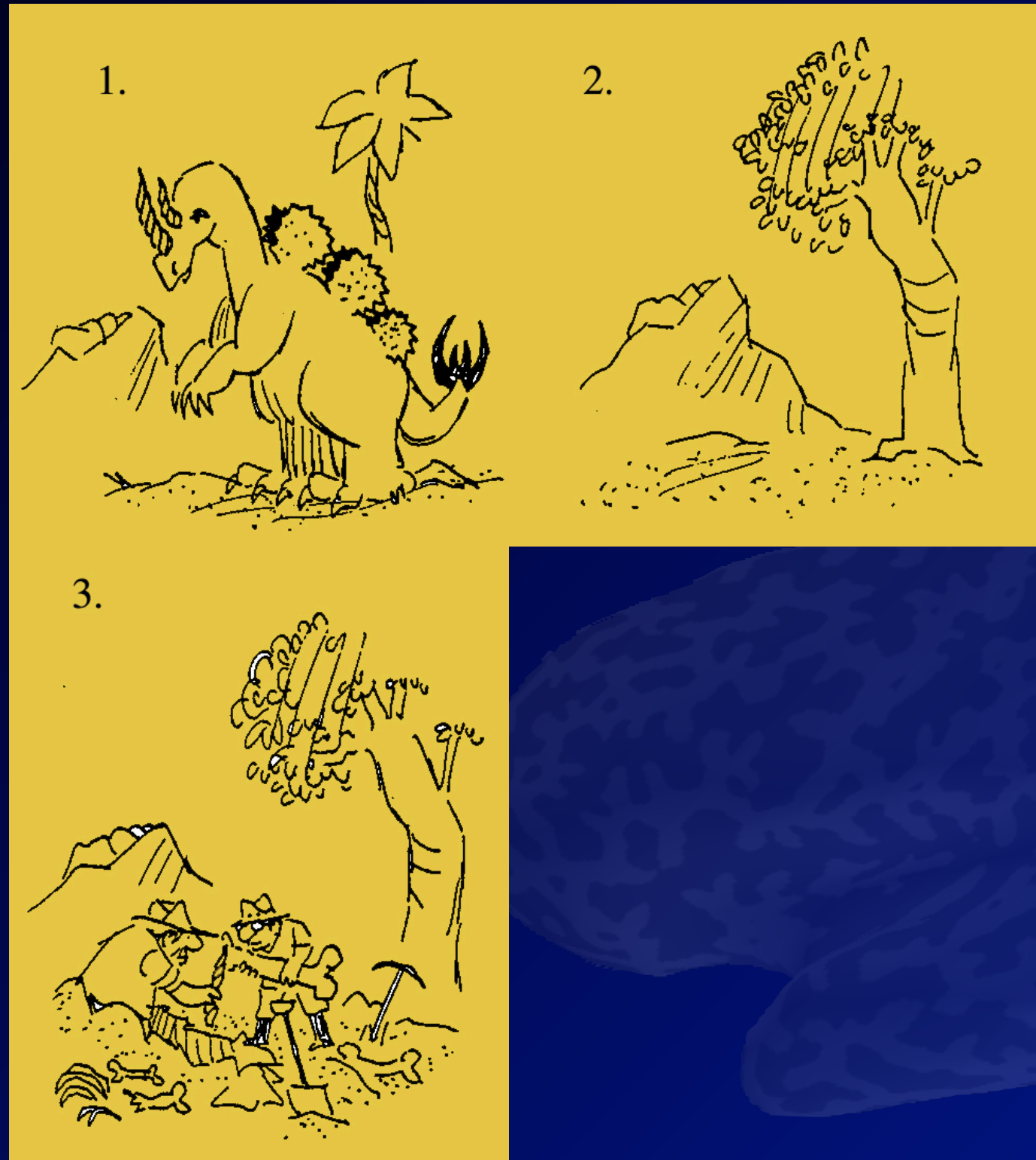
Another Kind of an Inverse Problem



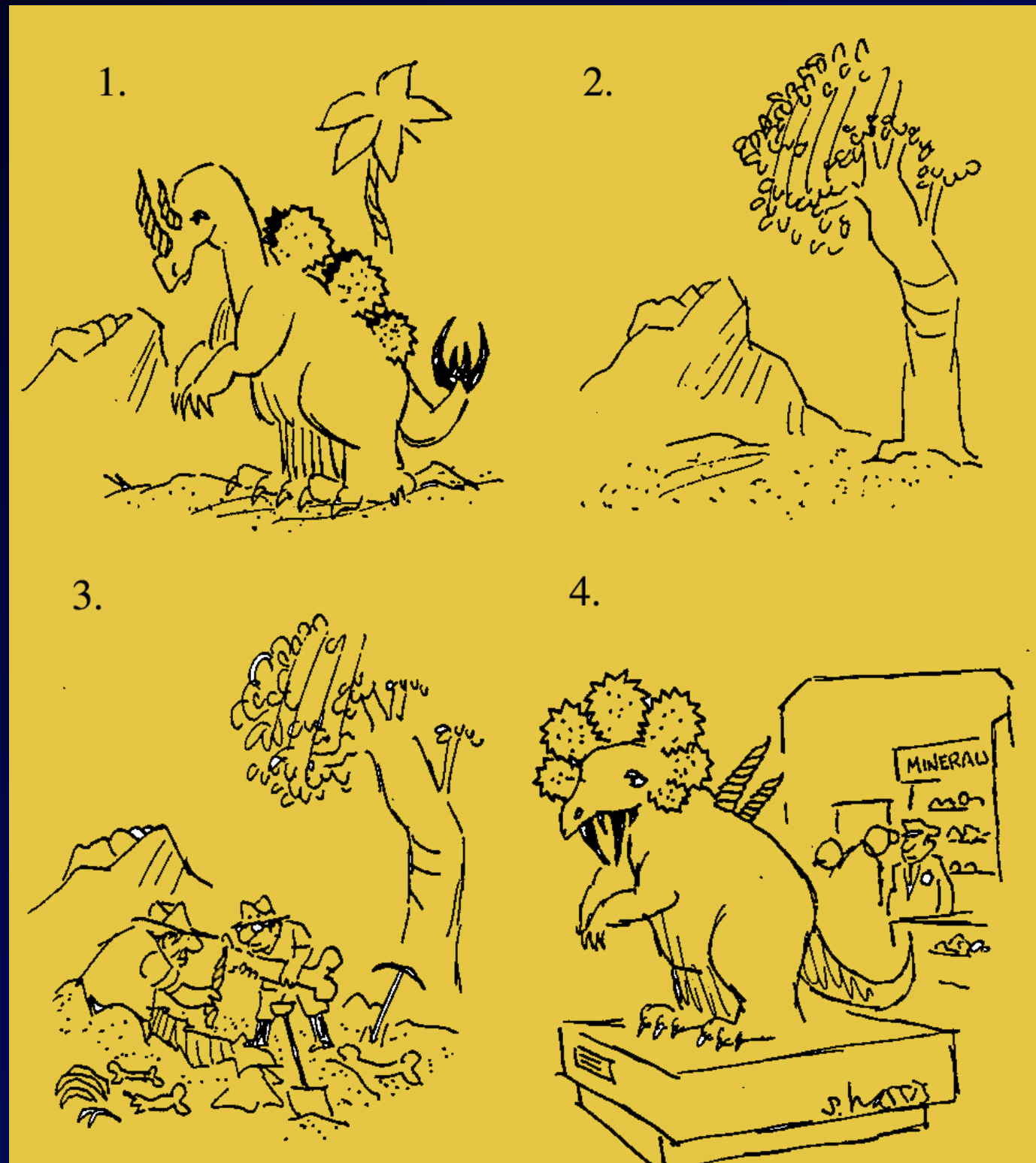
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Another Kind of an Inverse Problem

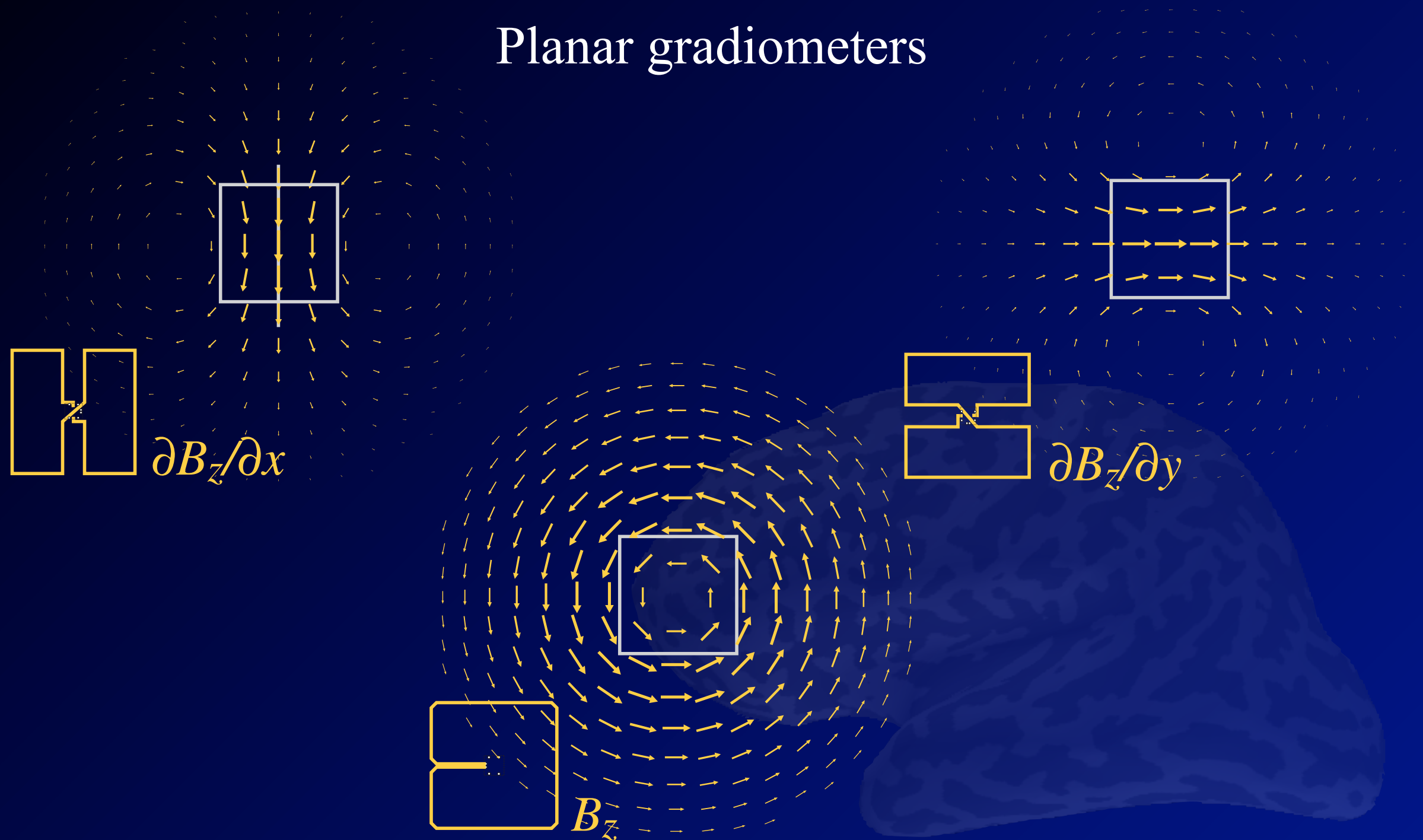


Another Kind of an Inverse Problem



Lead fields

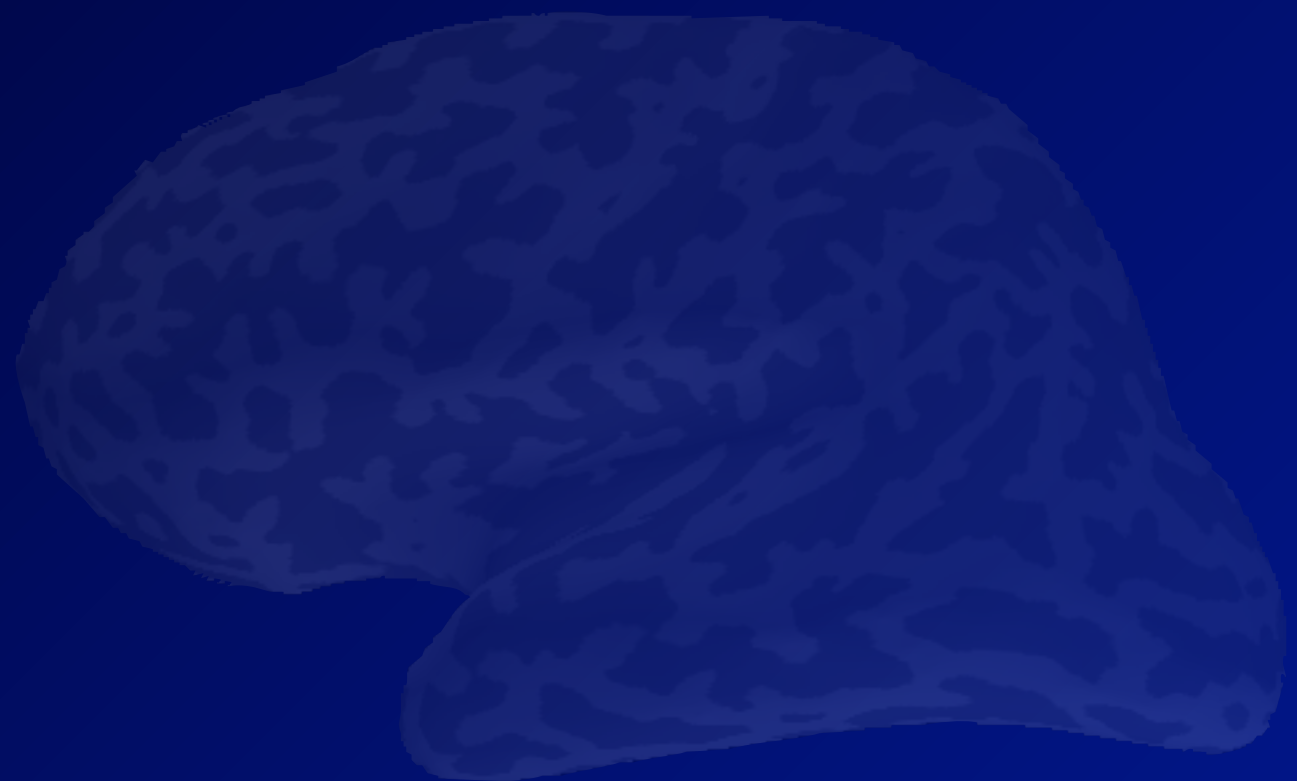
Planar gradiometers



Magnetometer

Cohen, 1979

MEG/EEG Inverse Problem



MEG/EEG Inverse Problem

- An ill-posed problem
 - Many different current distributions can explain the data
 - Solution may be sensitive to noise, *i.e.*, unstable



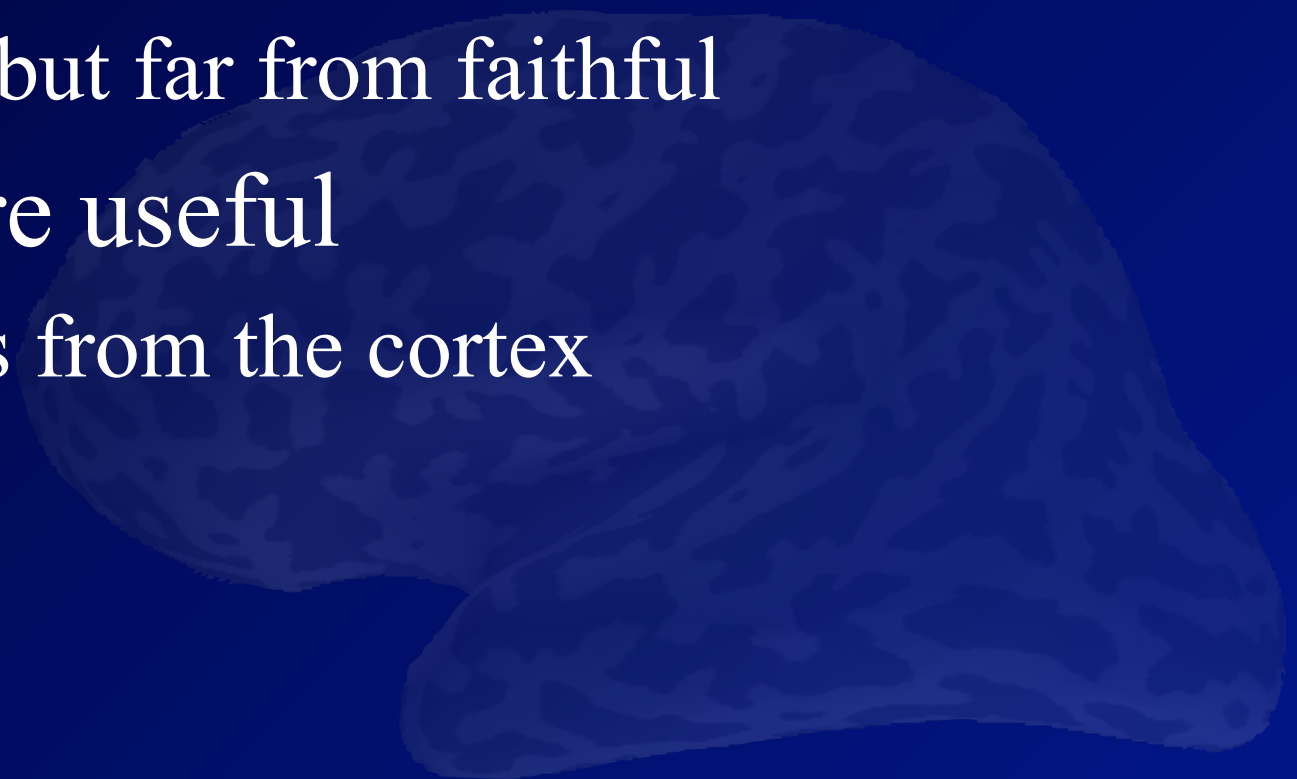
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 - How do we know the model is faithful to the actual current distribution in the brain?
 - A solution can be unique but far from faithful

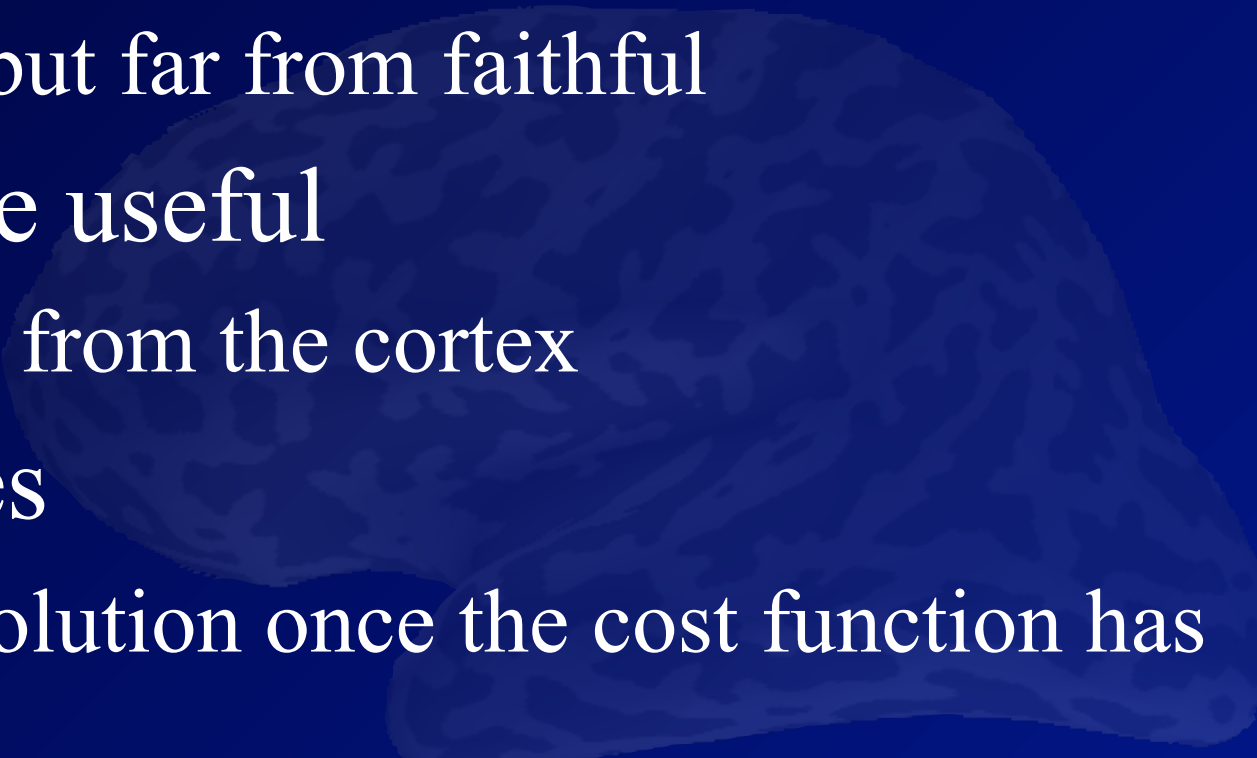


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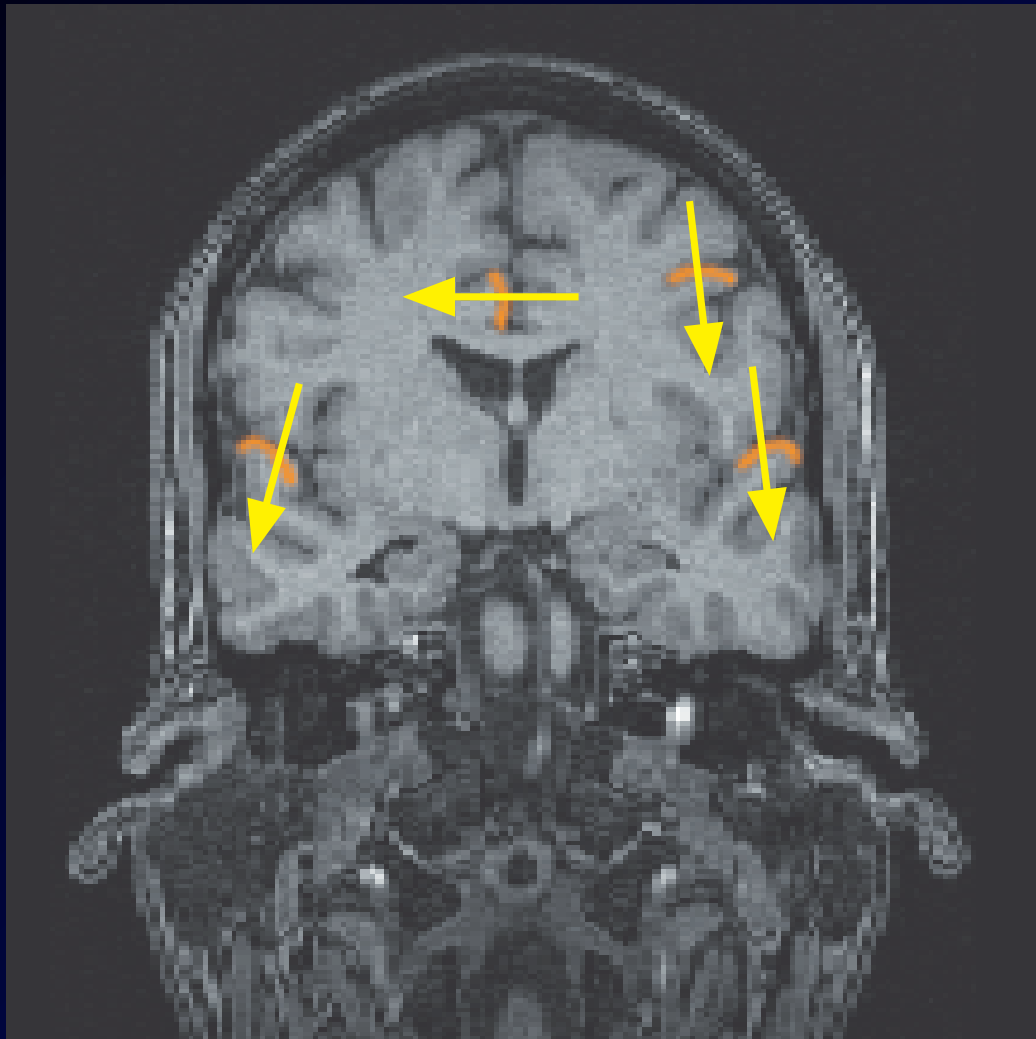
MEG/EEG Inverse Problem

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 - Computational challenges
 - How to find the optimal solution once the cost function has been specified?
- 

Current dipole models

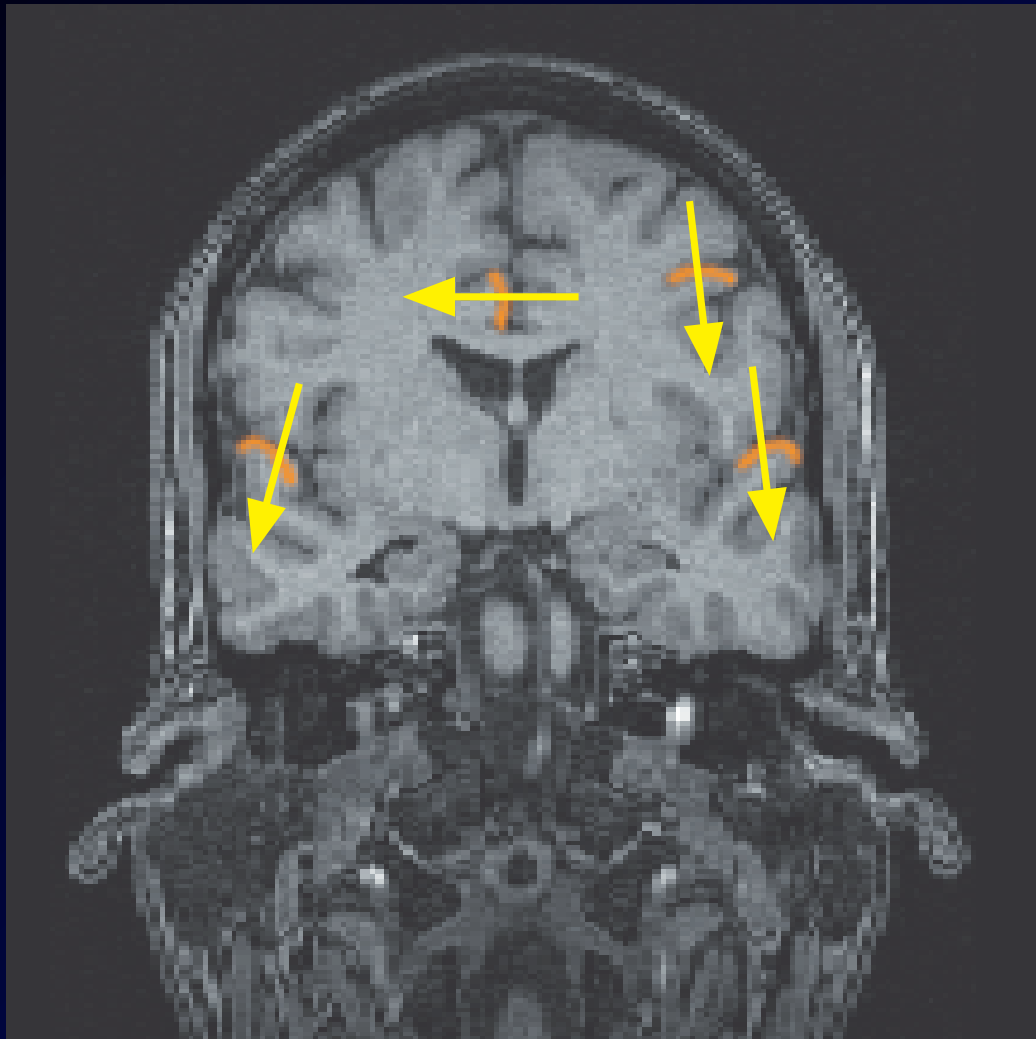


Example: The time-varying current-dipole model



- The neural currents on a few-cm² patch of cortex are approximated with a current dipole
- Dipole locations are fixed over time
- Dipole amplitudes are allowed to vary

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Scherg *et al.*, 1984

Model for the measurement

- Data predicted by the forward model + additive zero-mean Gaussian noise with a known spatial covariance matrix:



Model for the measurement

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$$\mathbf{B} = \mathbf{GQ} + \mathbf{N} = \sum_{p=1}^P \mathbf{g}_p(\vec{r}_p, \hat{e}_p) \mathbf{q}_p^T + \mathbf{N}$$



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Data produced by unit
dipoles at known locations



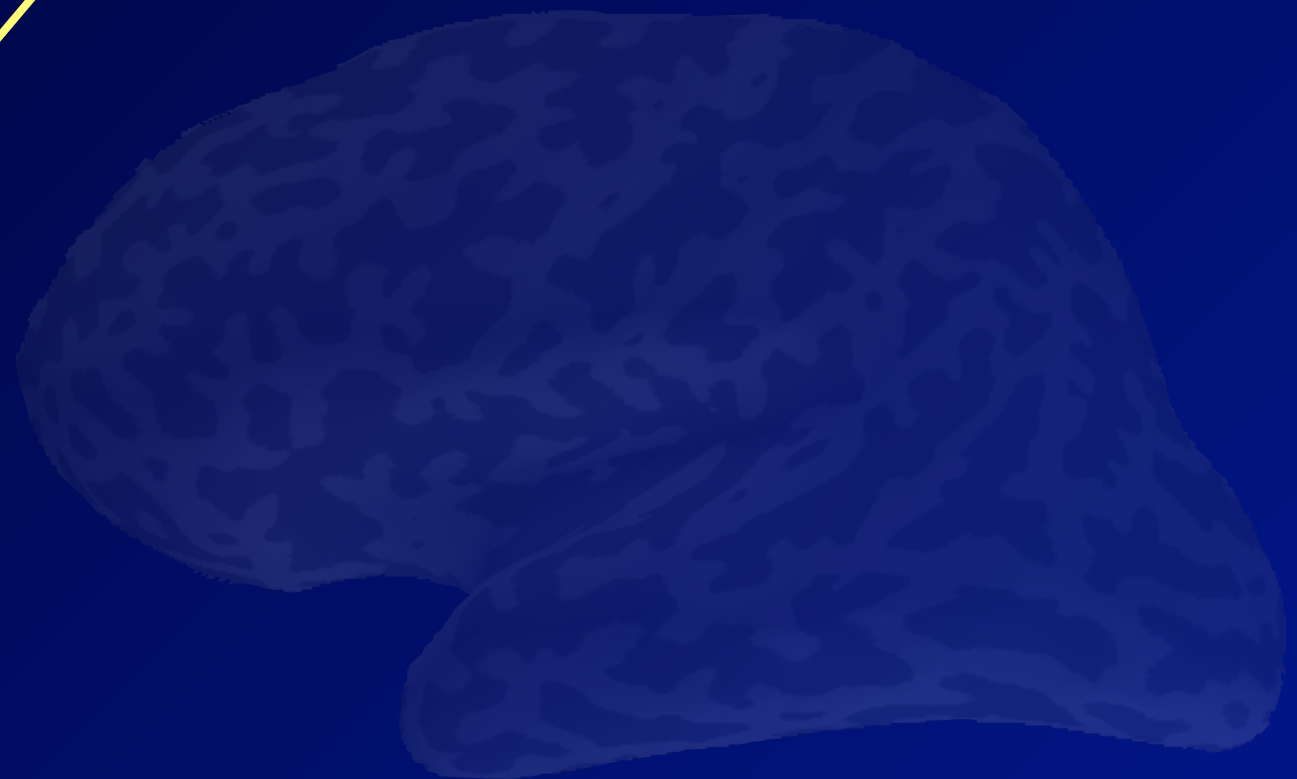
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Dipole locations

Dipole orientations



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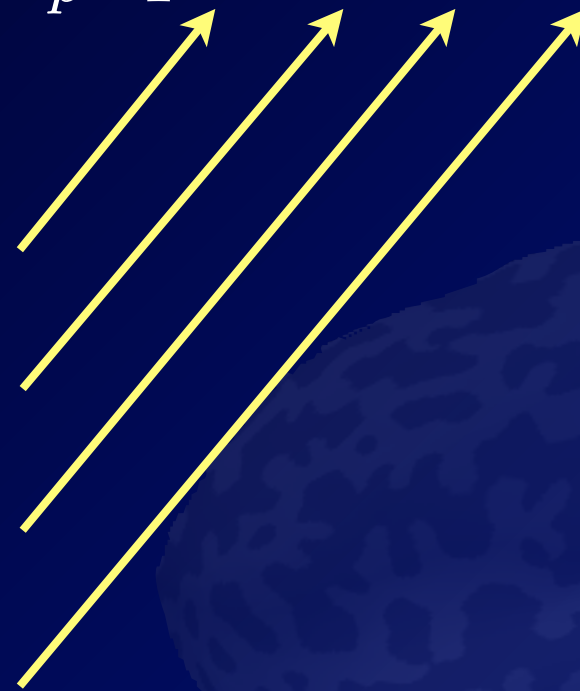
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Source waveforms



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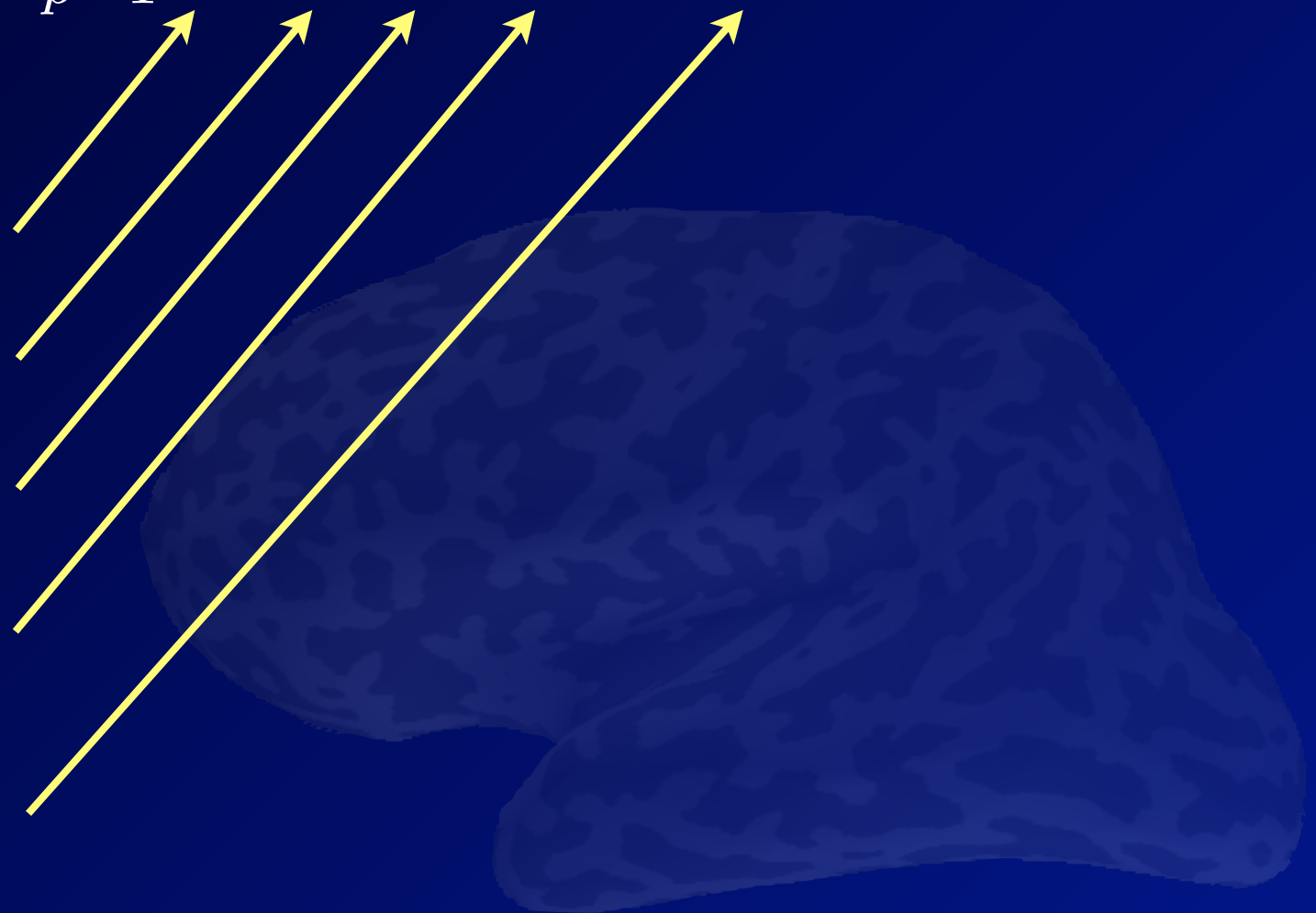
Data produced by unit
dipoles at known locations

Dipole locations

Dipole orientations

Source waveforms

Noise



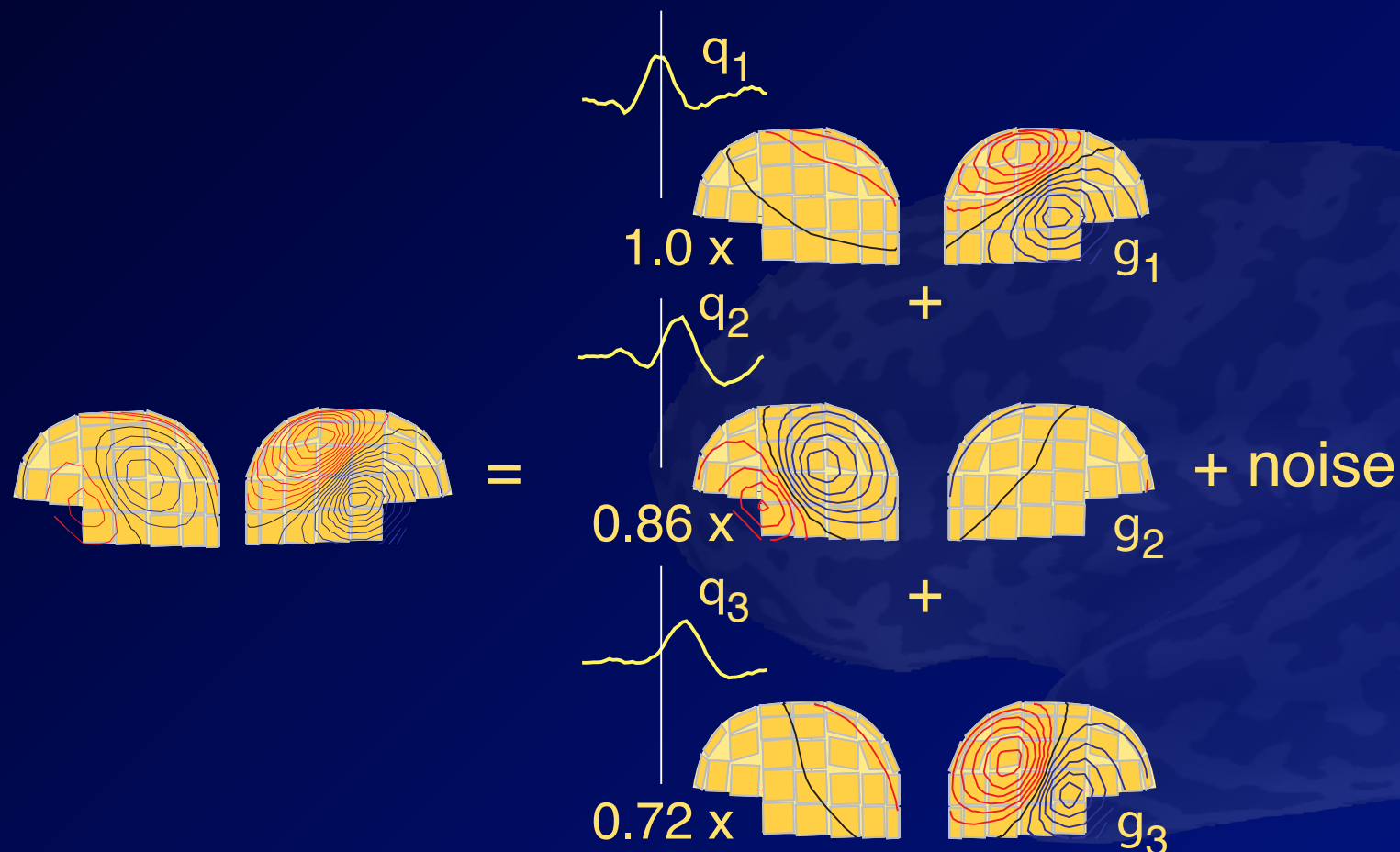
Model for the measurement

- Data predicted by the forward model + additive zero-mean Gaussian noise with a known spatial covariance matrix:

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Measured data

Model



Fitting

$$\{\hat{\mathbf{q}}_p, \hat{\mathbf{r}}_p\} = \operatorname{argmin}_{\{\mathbf{q}_p, \mathbf{r}_p\}} \|\mathbf{B}_{\text{meas}} - \mathbf{B}_{\text{model}}\|^2$$



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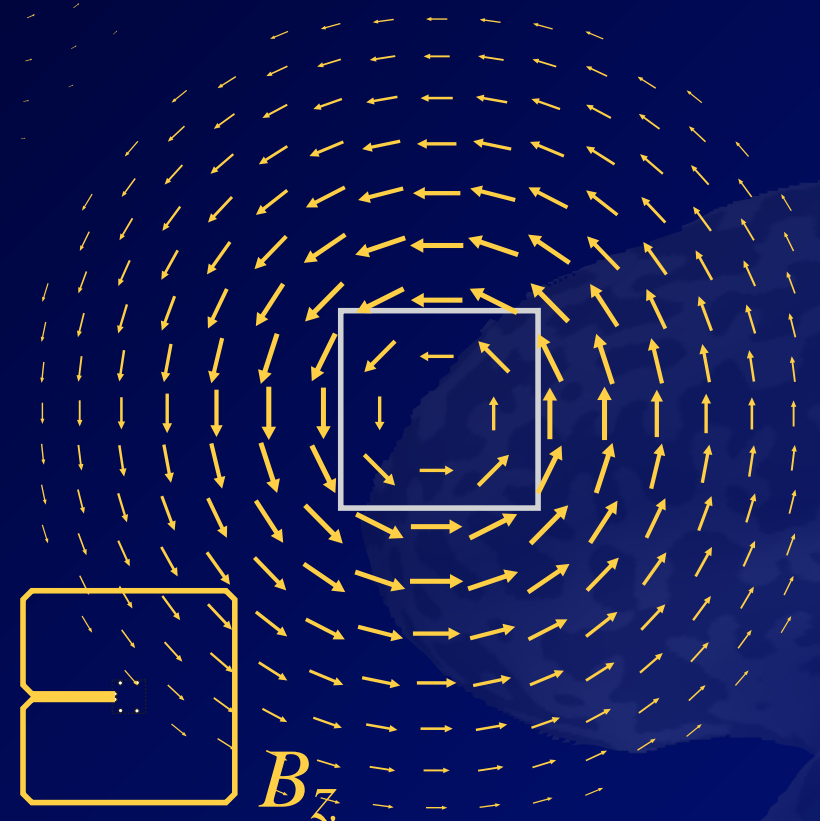
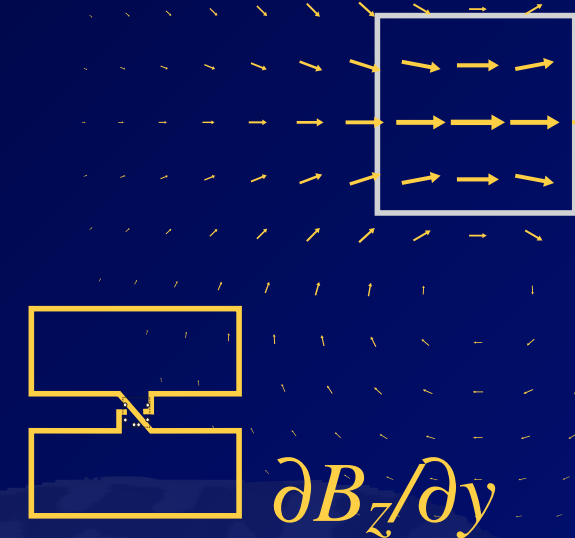
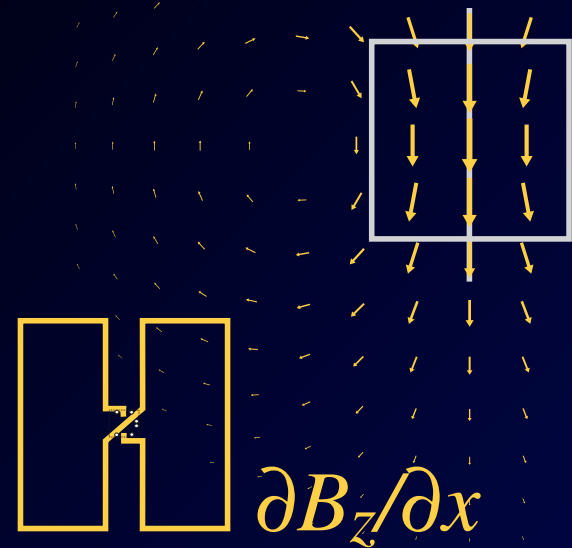
Heuristic strategies

- Try to select time points when only one dipole is active
- Use channel selections
- Construct the model dipole-by-dipole



Vectorview sensor triplets (306 = 3 x 102)

Planar gradiometers

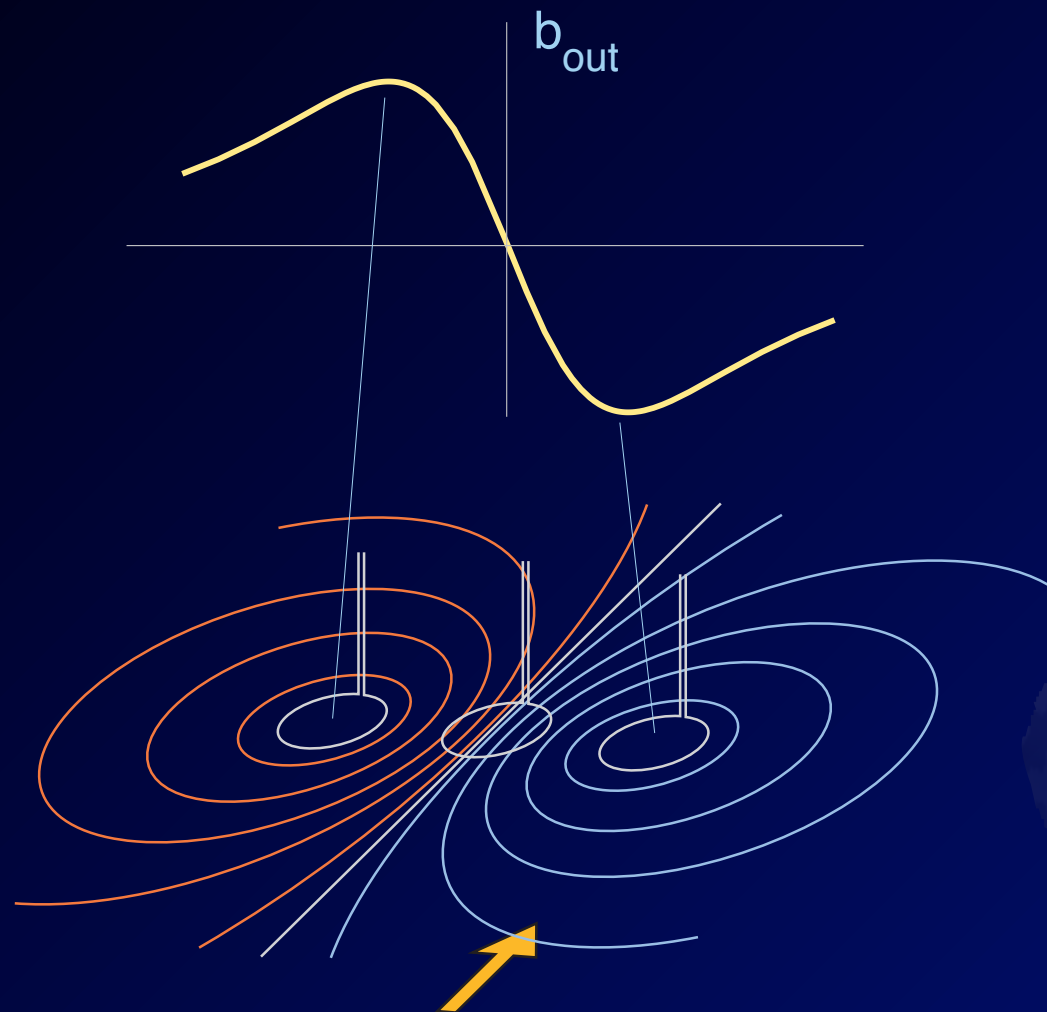


Magnetometer

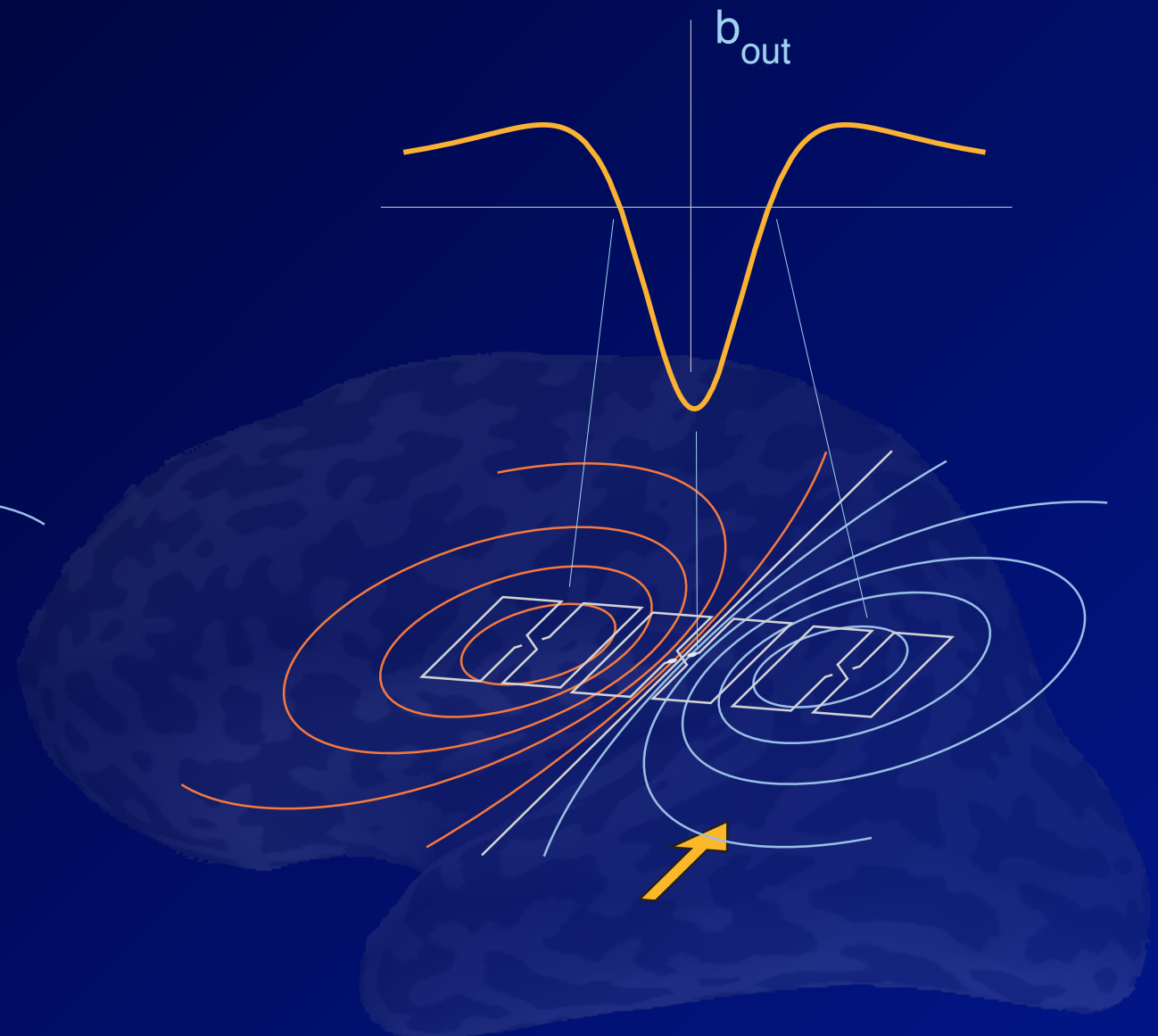
Cohen, 1979

Magnetometers and planar gradiometers

Magnetometer



Planar gradiometer



An example of averaged MEG data

- Somatosensory median nerve data
- Activity expected at least in SI (left) and SII (left and right)

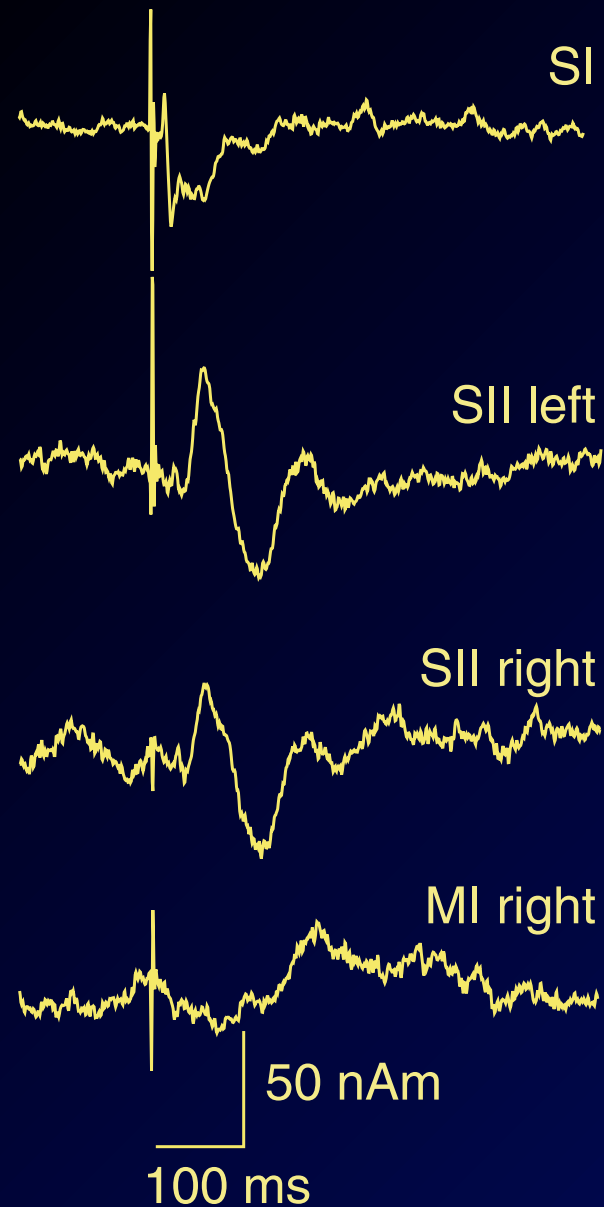


Possible strategy

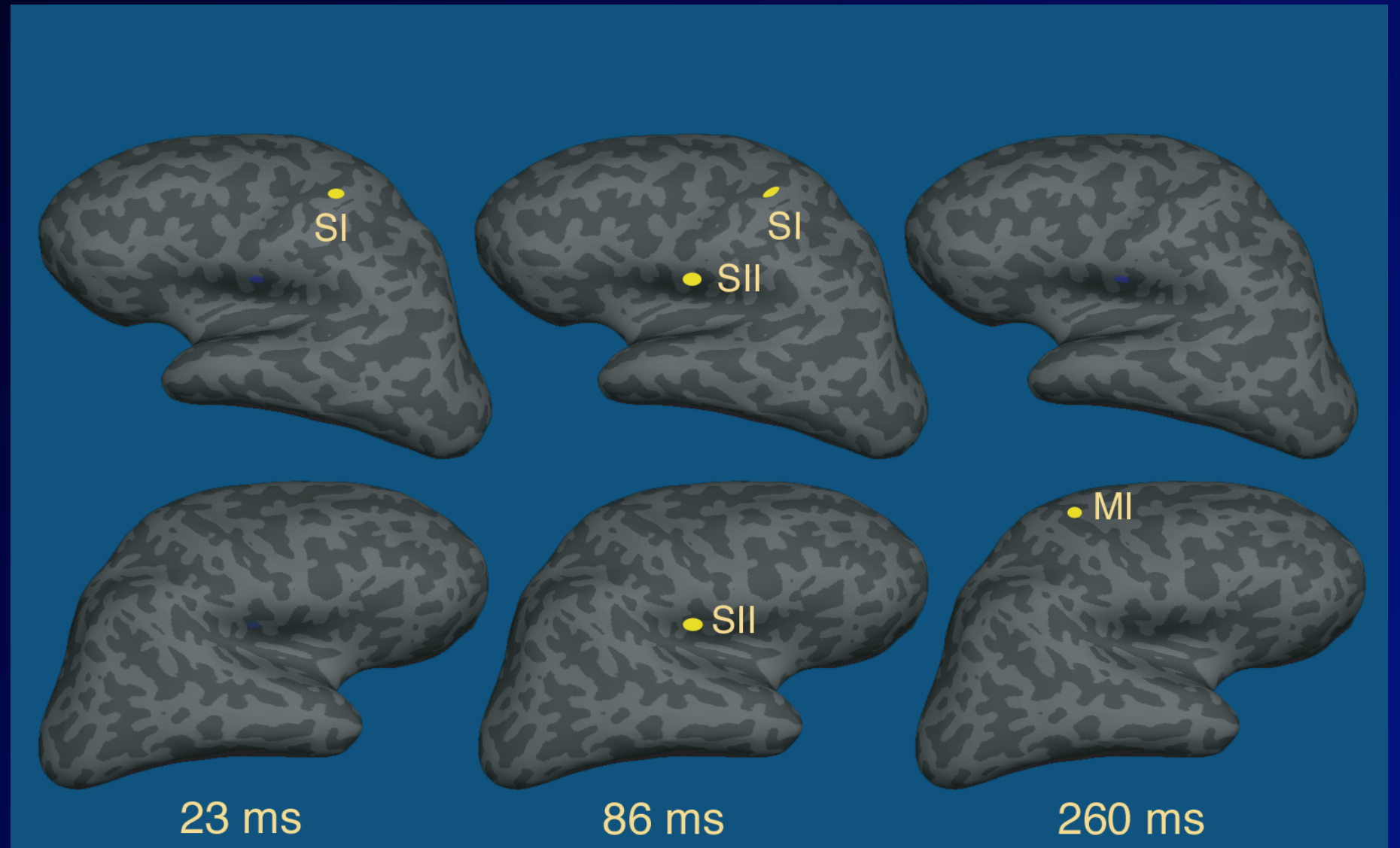
- Fit SI at an early latency when it is active alone
- Fit the two SII responses using channel selections
- Fine tune SII fitting by keeping SI dipole fixed



Dipole analysis: SEF with a motor task



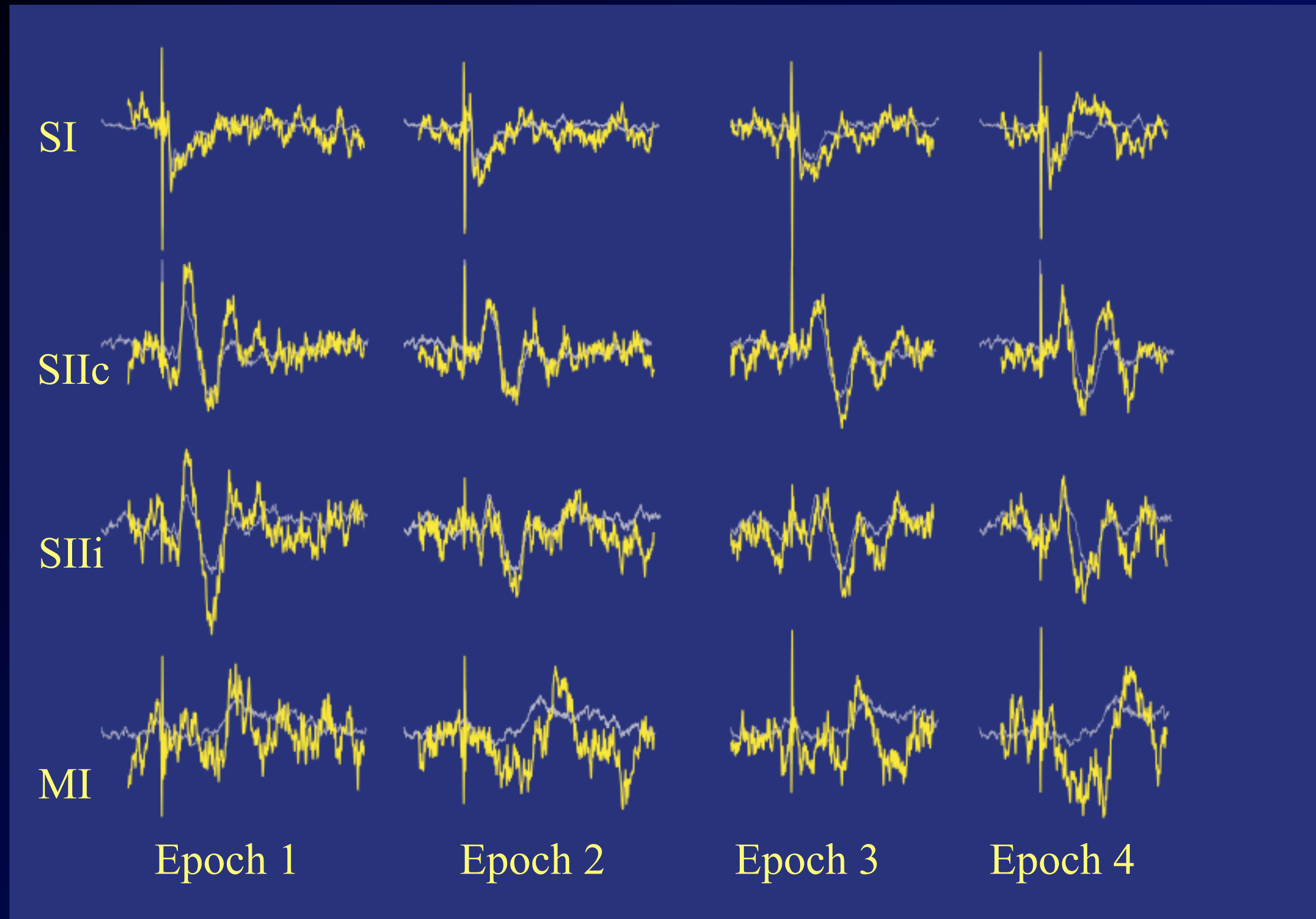
Source waveforms



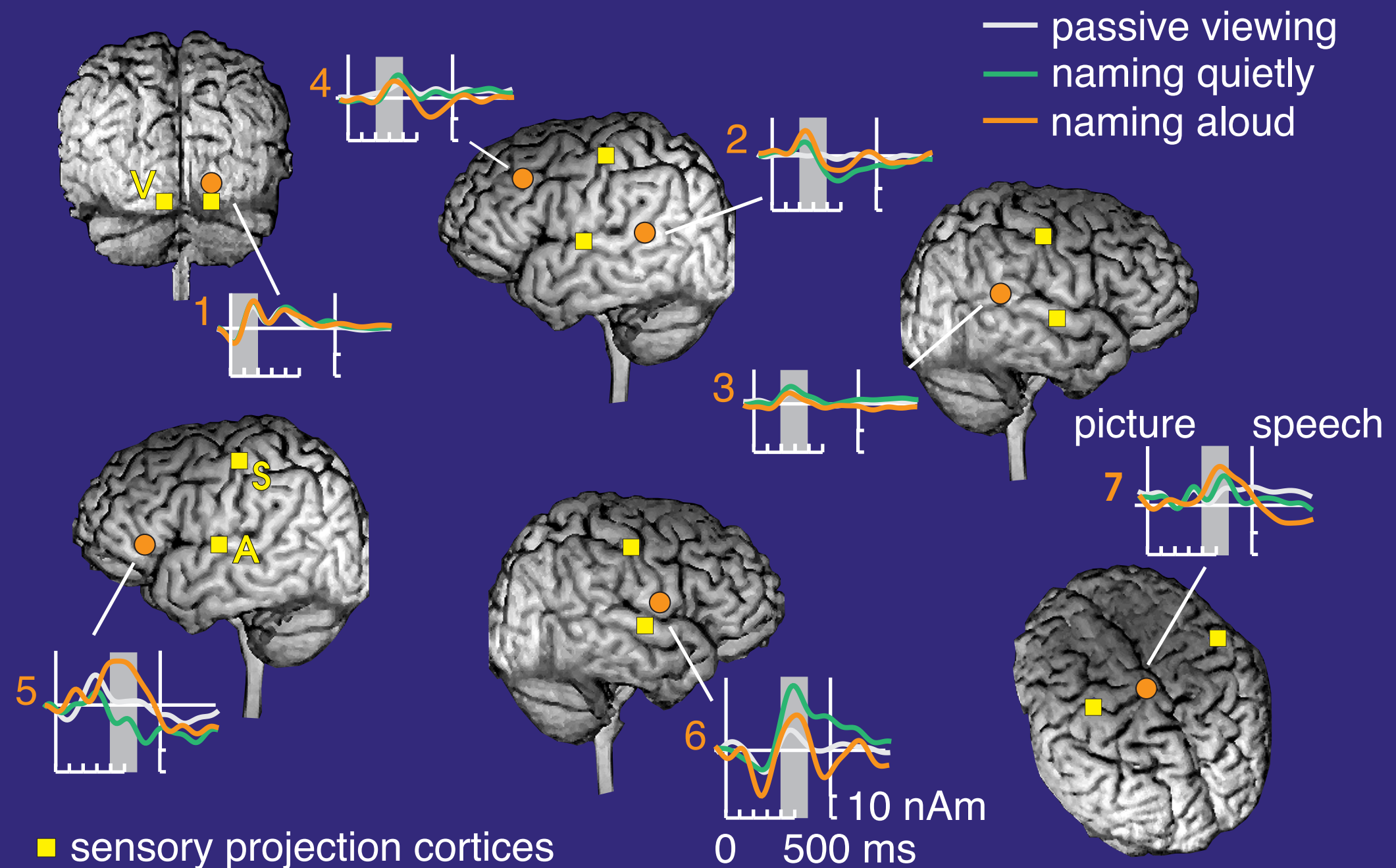
Source locations

Raij *et al.*

Single-epoch analysis

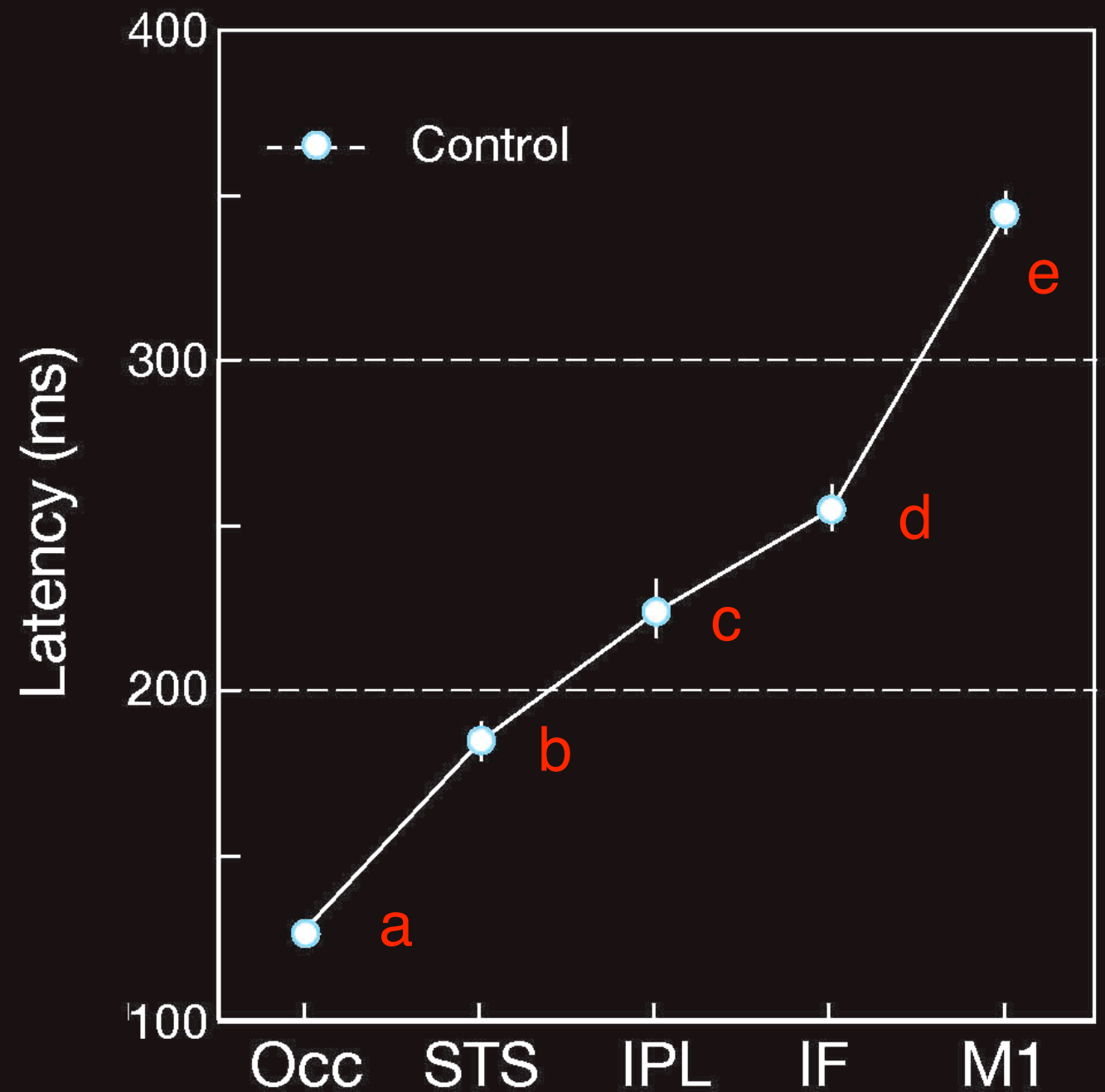
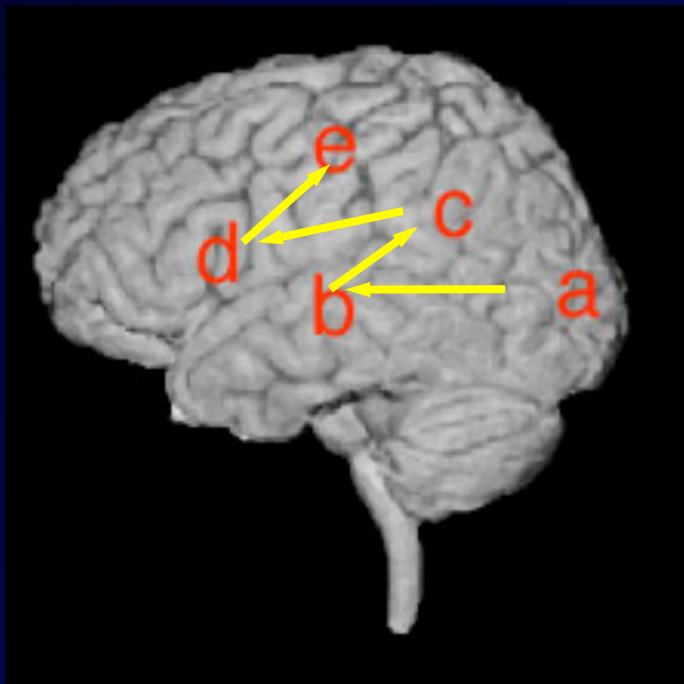


Dynamics of Brain Activation in Picture Naming



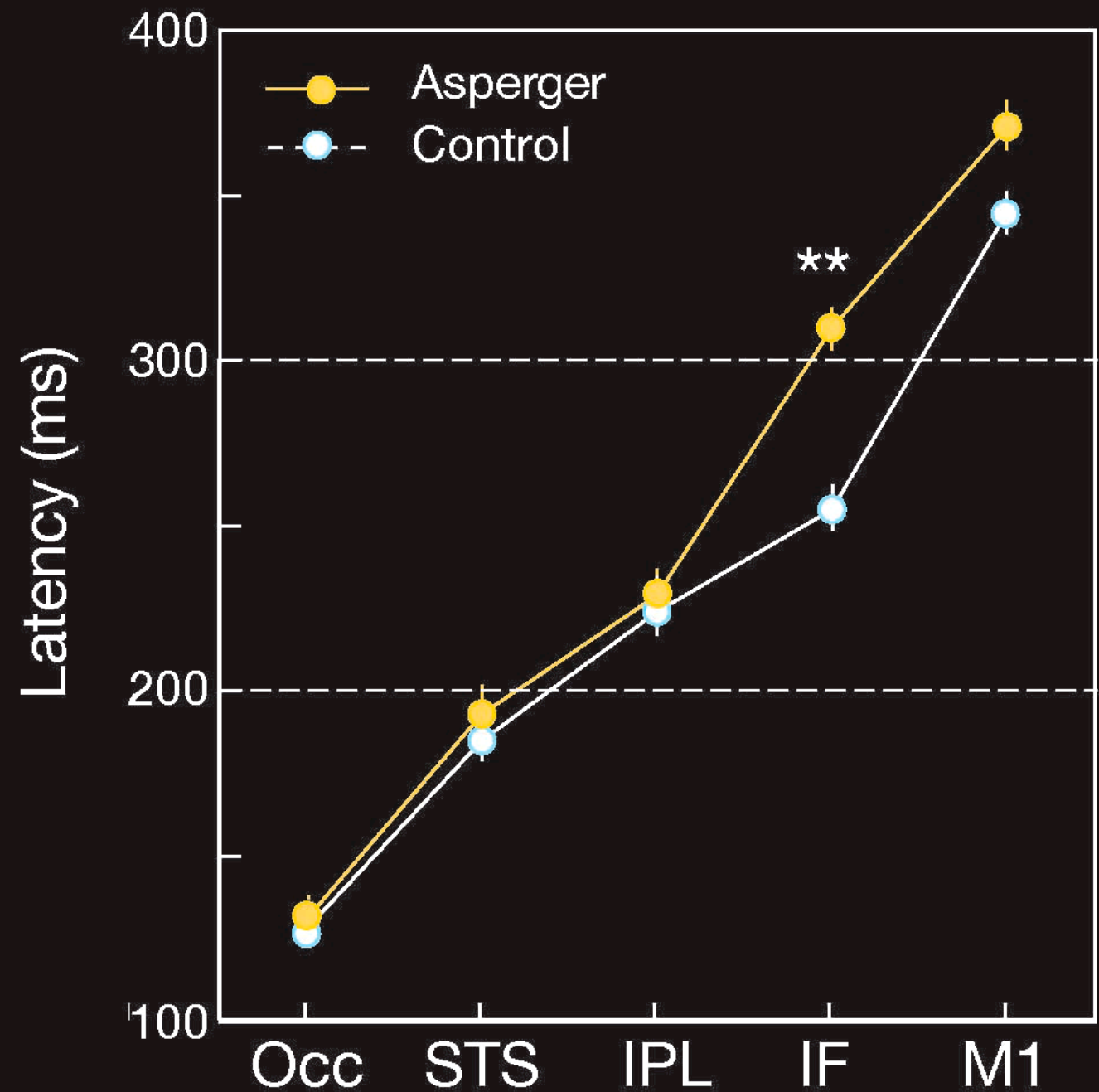
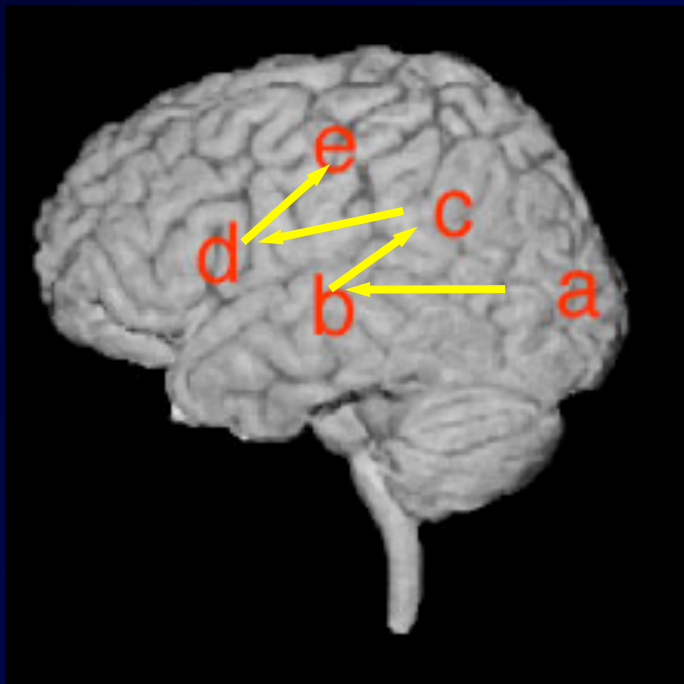
Salmelin et al., Nature 1994

Imitation of orofacial gestures



Nishitani & Hari, Neuron 2002; Nishitani et al. Ann Neurol 2004

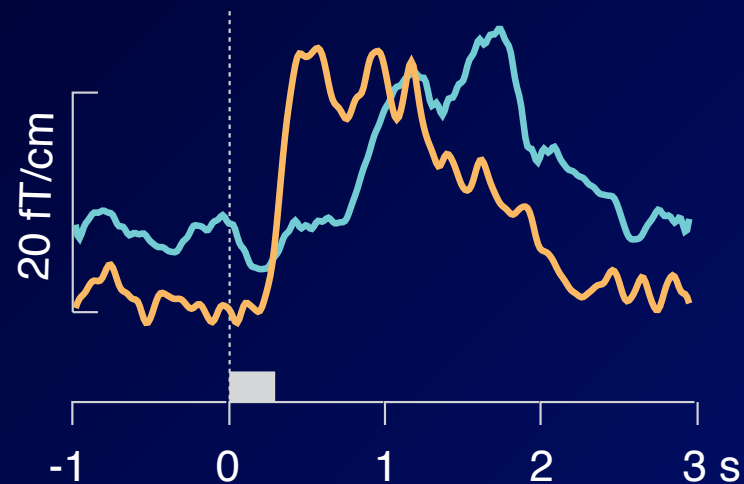
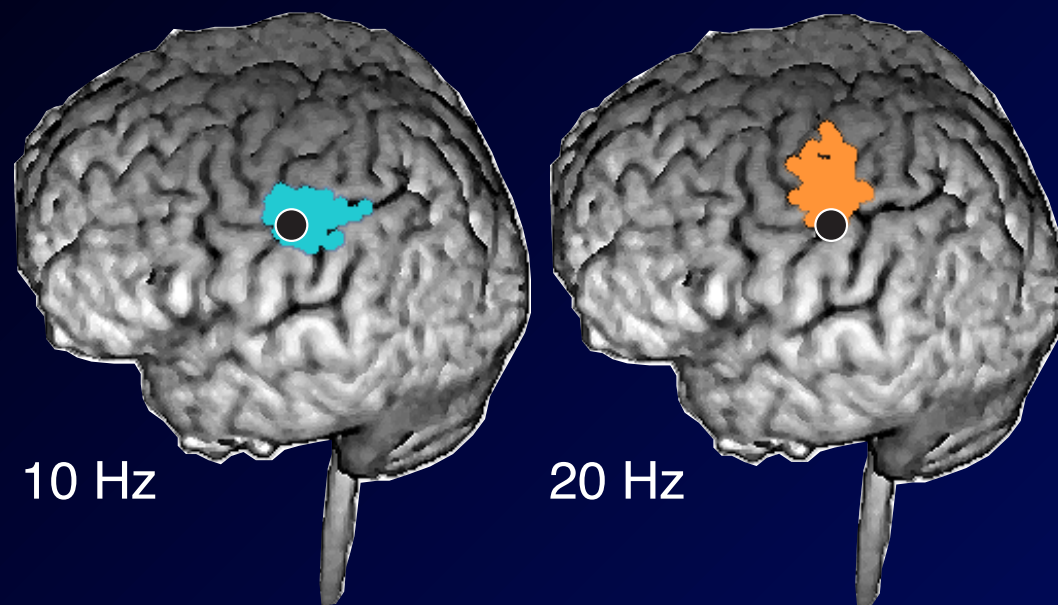
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Spatiotemporal analysis of the somatomotor (m) rhythms

Modulation with finger movements

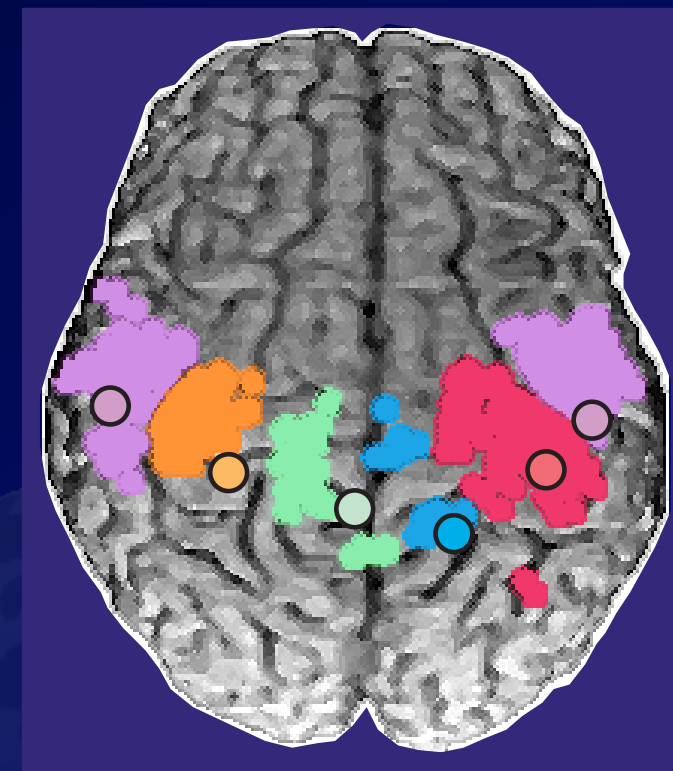
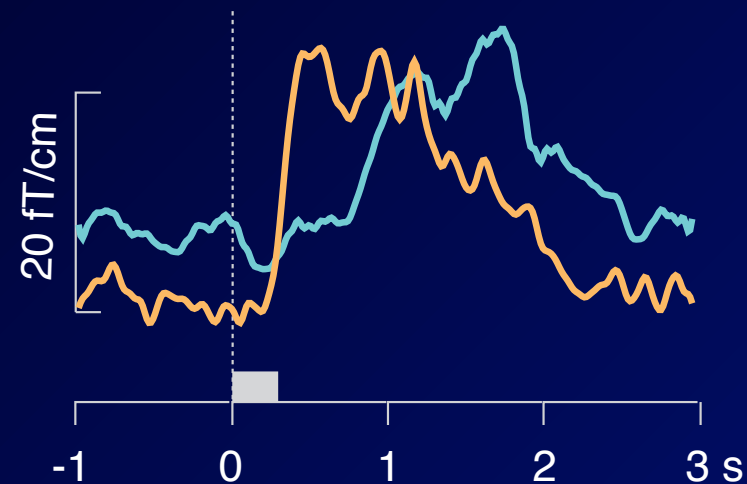
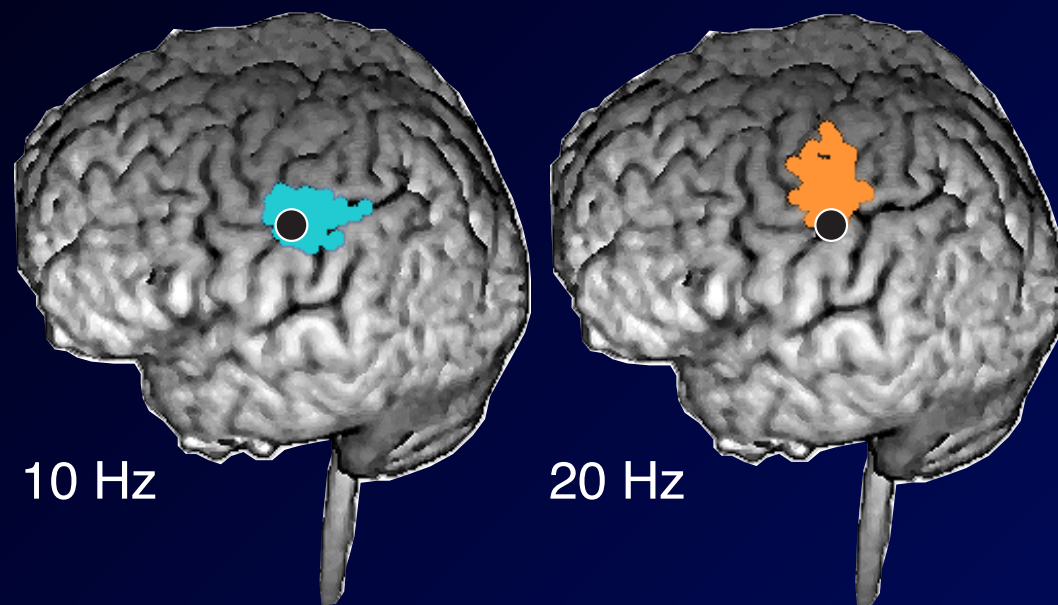


Salmelin et al., NeuroImage, 1995

Spatiotemporal analysis of the somatomotor (m) rhythms

Modulation with finger movements

Homunculus of the 20-Hz component



SEF

- left tibial nerve
- right tibial nerve
- left median nerve
- right median nerve
- lip

MOVEMENT

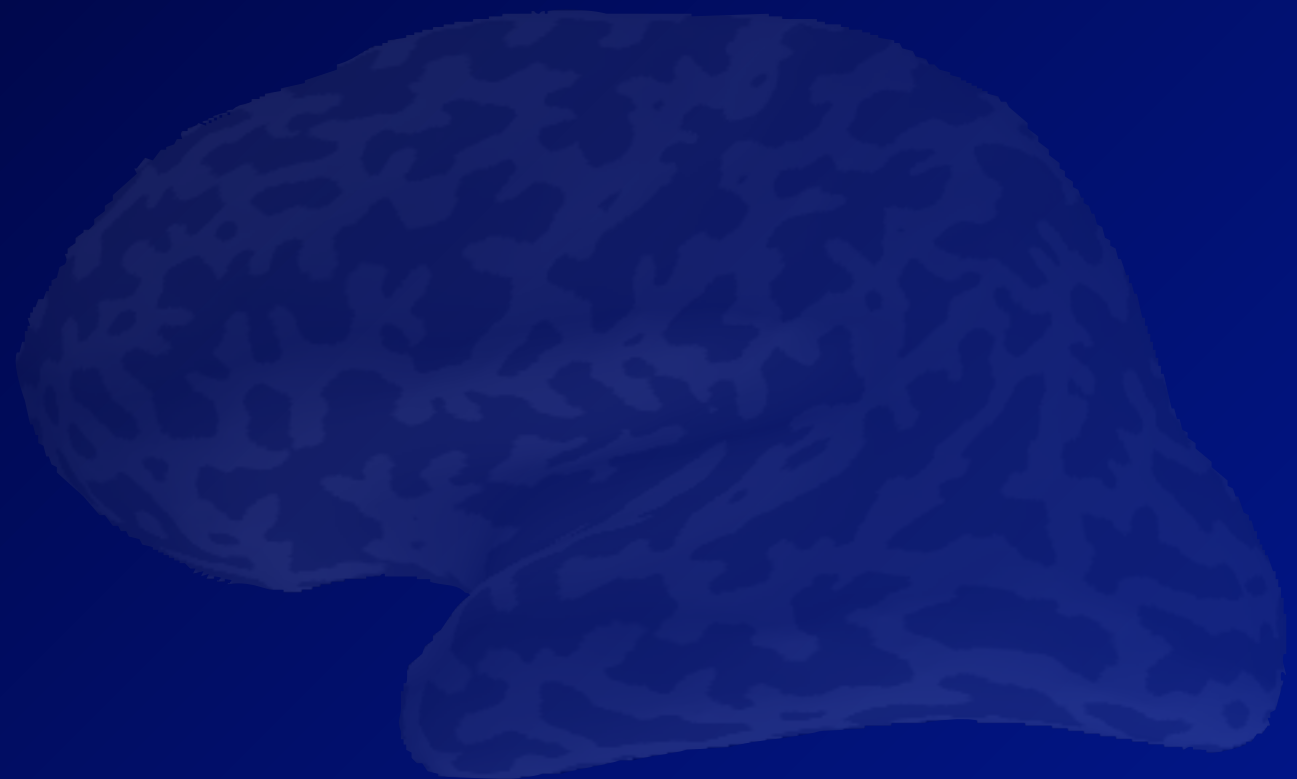
- left toes
- right toes
- left finger
- right finger
- mouth

Salmelin et al., NeuroImage, 1995

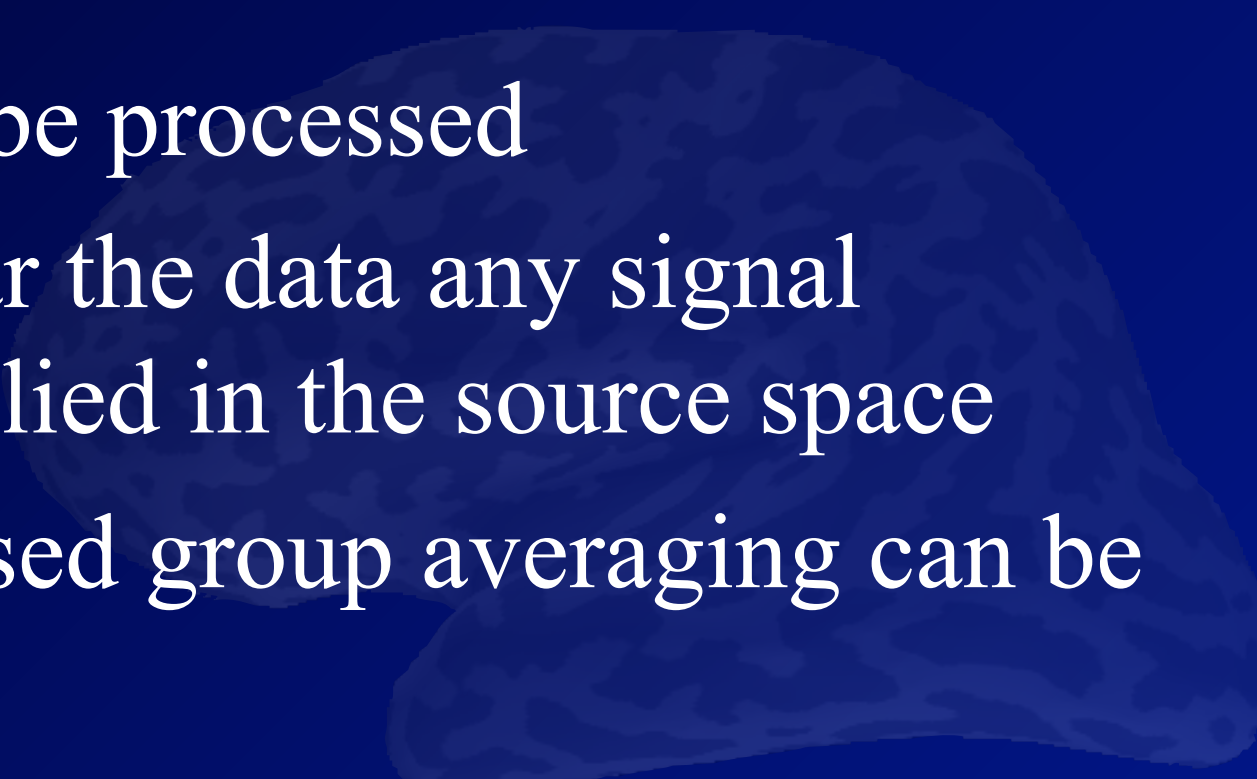
Dipole models: caveats

- It is difficult to find the optimal dipole locations automatically:
 - Heuristics: Build the model one dipole at a time
 - Genetic algorithms: Find the global minimum
 - Multistart simplex: Perform a lot of fits with different initial guesses
 - MUSIC algorithms: Possible to scan one dipole at a time
- The least-squares solution might not be closest to the truth
- Sources might be too extended to be represented by a dipole

Anatomically and functionally constrained source estimates



Motivation to use distributed source models

- Account for non-focal (extended) sources
 - Automatic analysis without heuristic choices often needed in multidipole models
 - Incorporate anatomical and functional MRI constraints
 - Lower SNR data can be processed
 - If the estimate is linear the data any signal processing can be applied in the source space
 - Surface or volume based group averaging can be employed
- 

Minimum-Norm Solutions

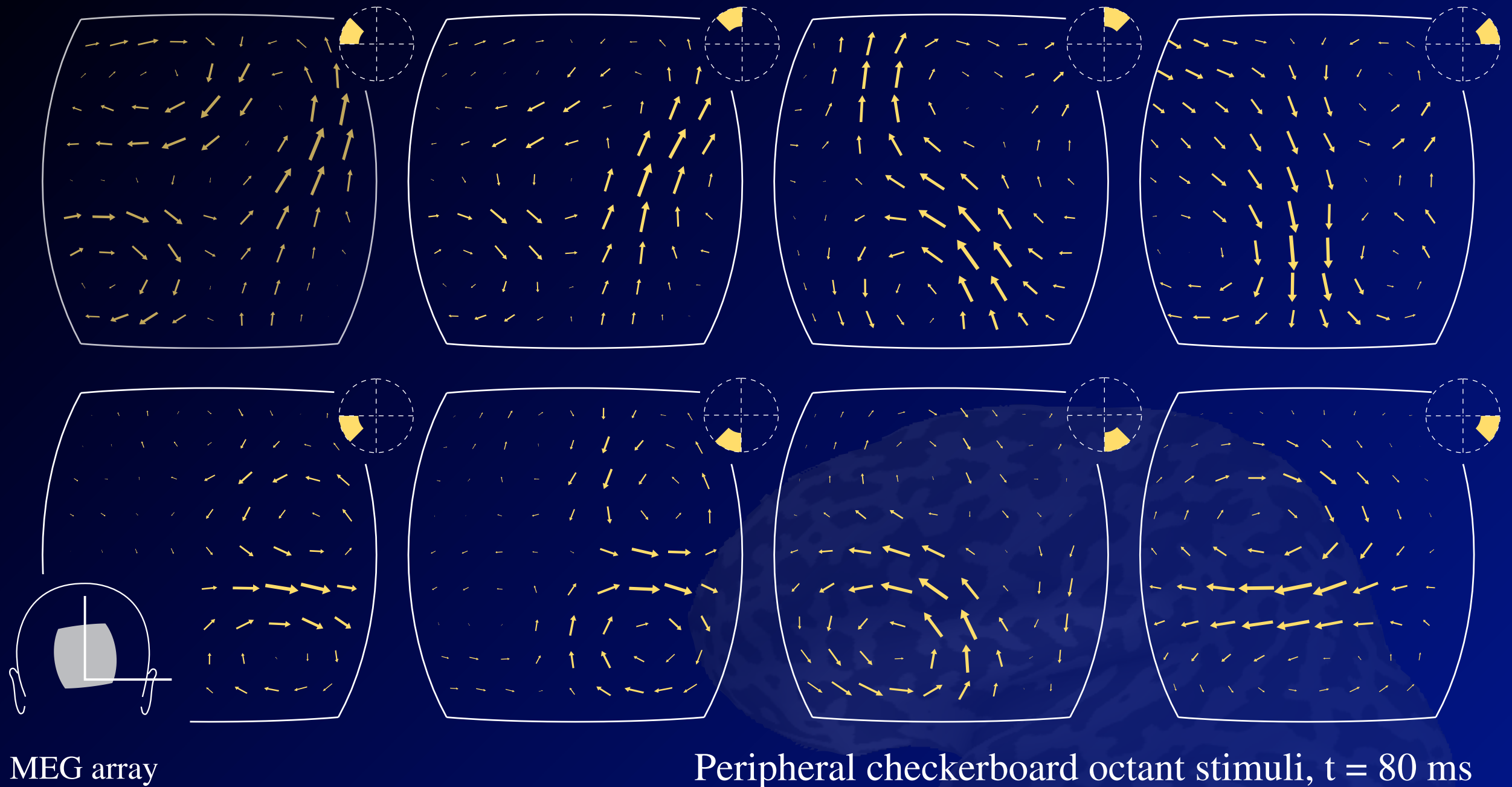
- Grid of dipoles in a volume or on a surface
- Underdetermined: $n_{\text{sources}} \gg n_{\text{meas}}$
- Find an optimal solution among those fitting the data

$$\hat{\mathbf{q}} = \operatorname{argmin}_{\mathbf{q}} (||\mathbf{y} - \mathbf{G}\mathbf{q}||_{\mathbf{C}}^2 + ||\mathbf{q}||_{\mathbf{R}}^p)$$

Examples:

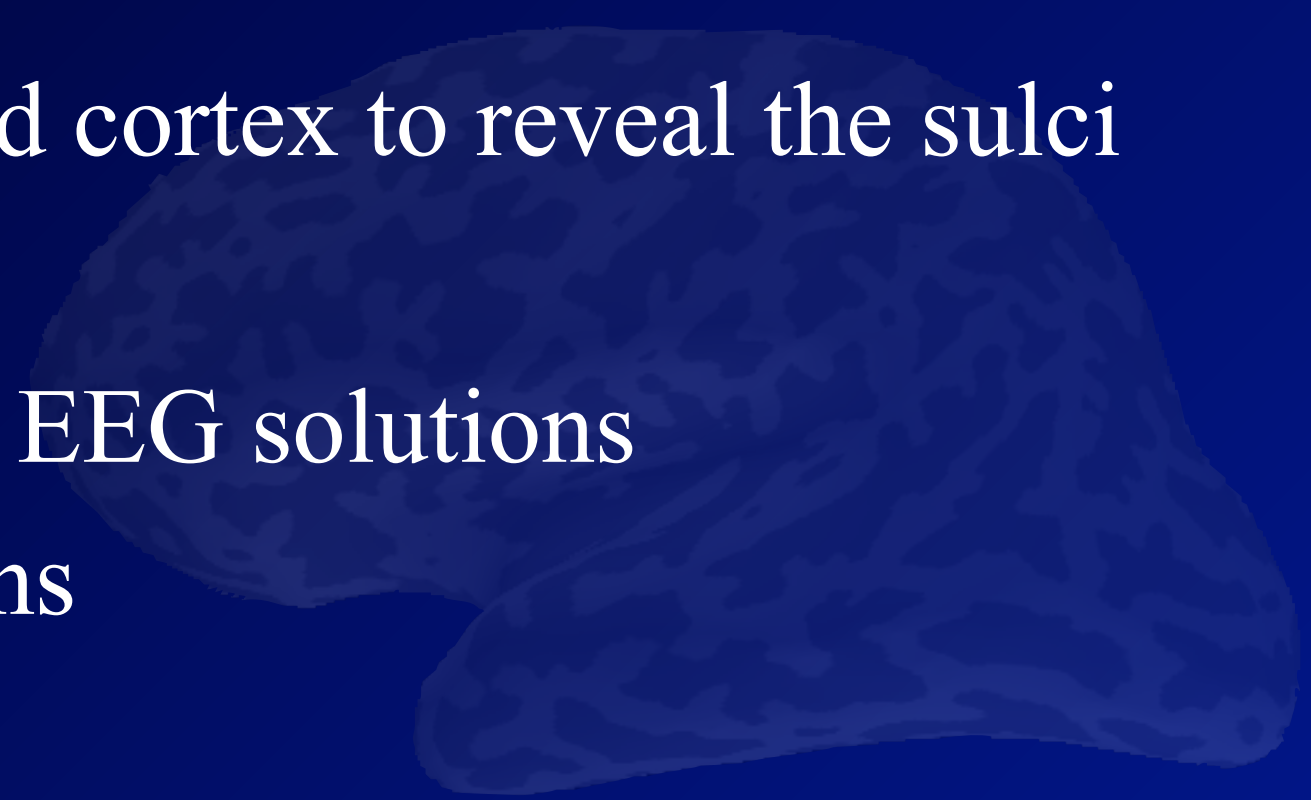
- Minimum-norm estimates (MNE): $p = 2$
- LORETA: $p = 2$, $R = \text{Laplacian operator}$
- Minimum-current estimates (MCE): $p = 1$

Retinotopic mapping with MNE



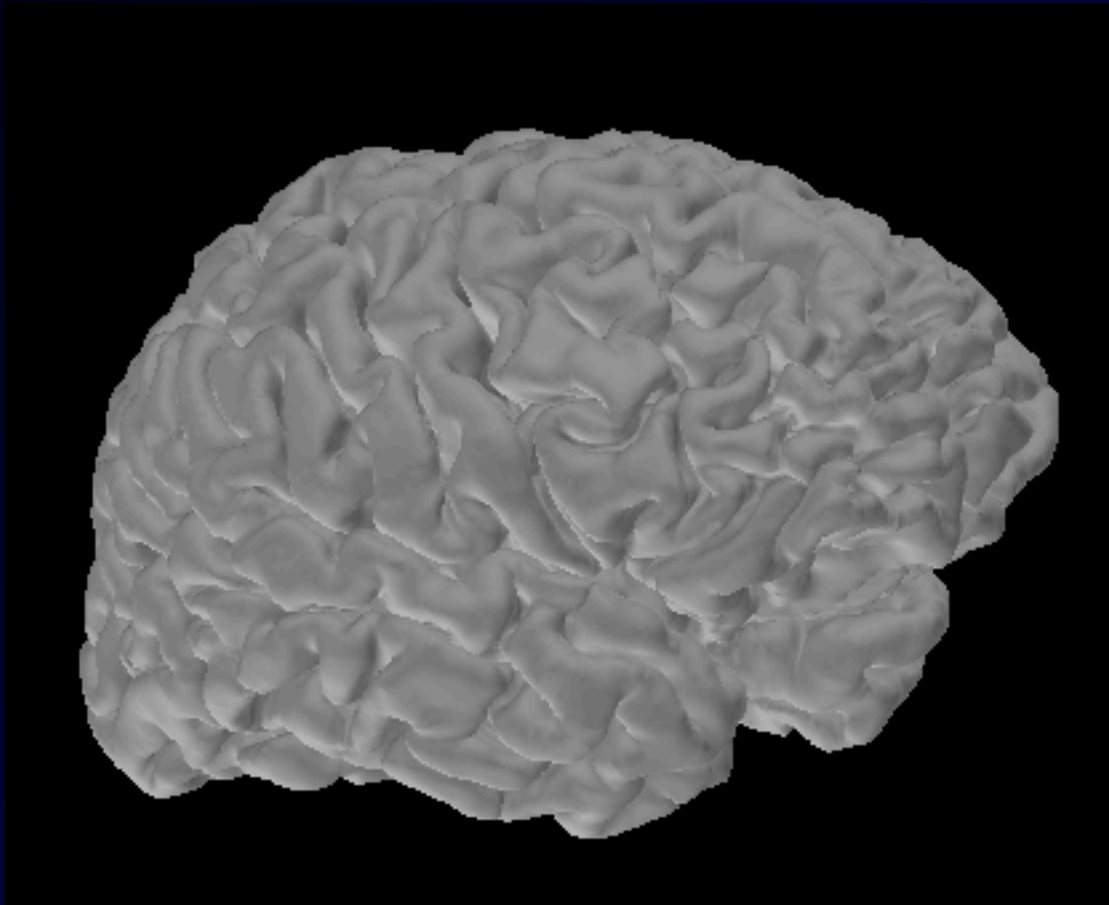
Ahlfors *et al.* 1992

Modern MNE

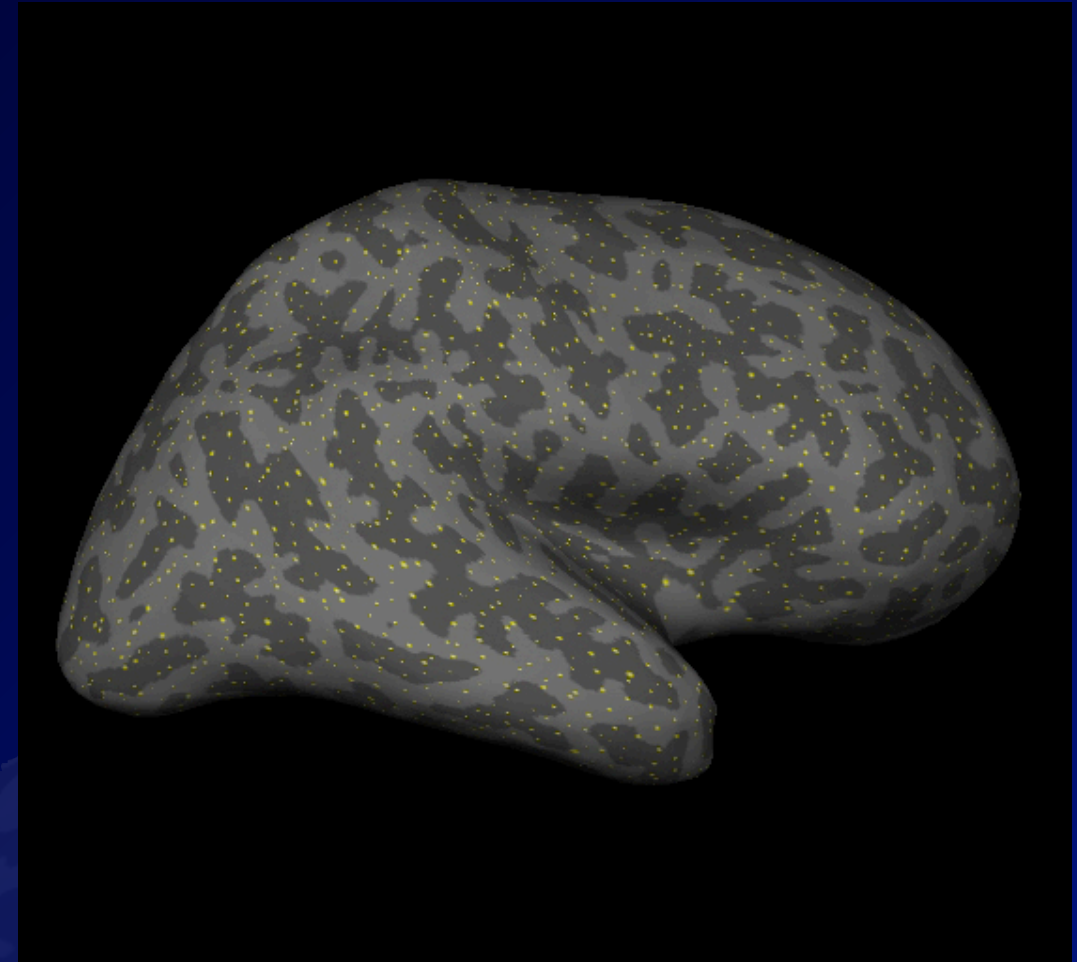
- Source locations (and orientations) constrained to the cortical mantle
 - Forward solution with BEM
 - Full noise-covariance matrix estimates computed from raw data
 - Display on an inflated cortex to reveal the sulci
 - Compute statistics
 - Combined MEG and EEG solutions
 - fMRI-guided solutions
- 

Dale *et al.* 2000

Cortical Source Location Constraints

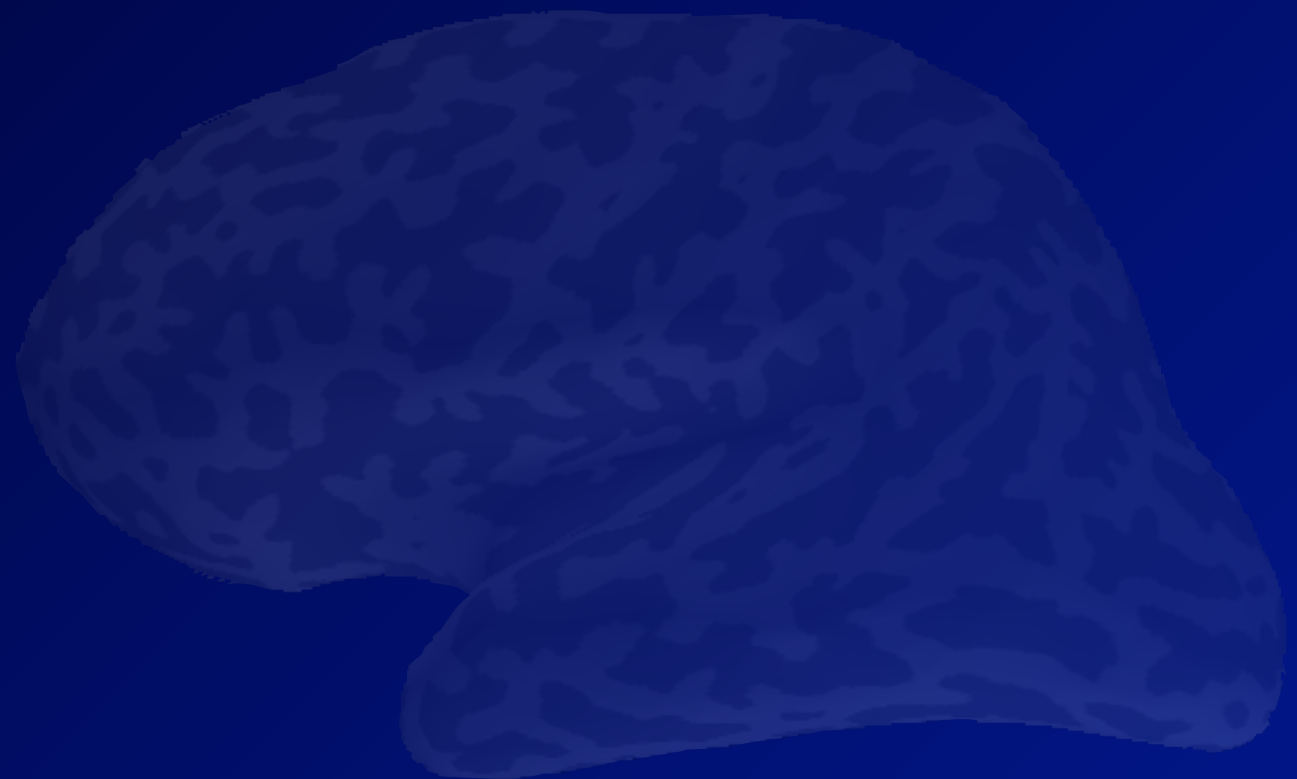


Tessellation of the cortex:
Source location and orientation
information



For source estimation, the surface
is typically decimated, resulting
in 6000 - 10000 source locations

Inflated Cortex



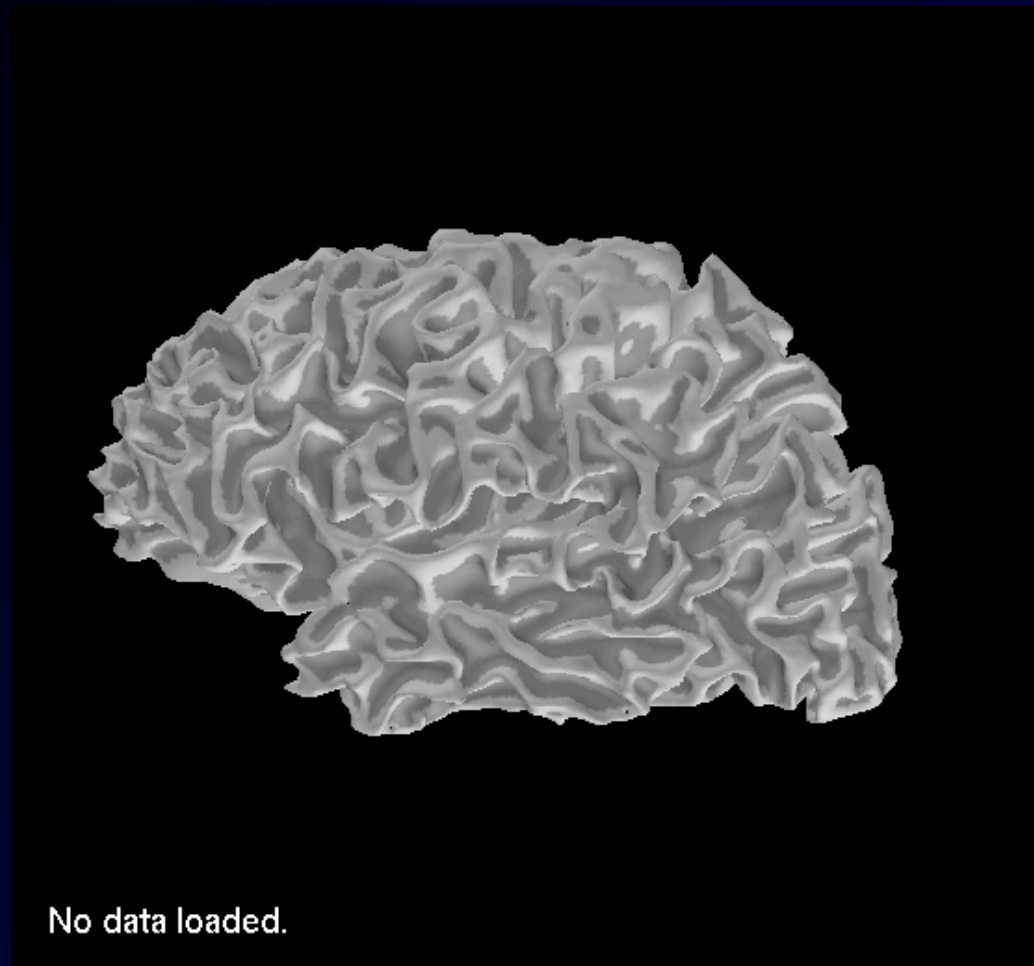
Inflated Cortex



Topologically correct tessellation
can be inflated



Inflated Cortex

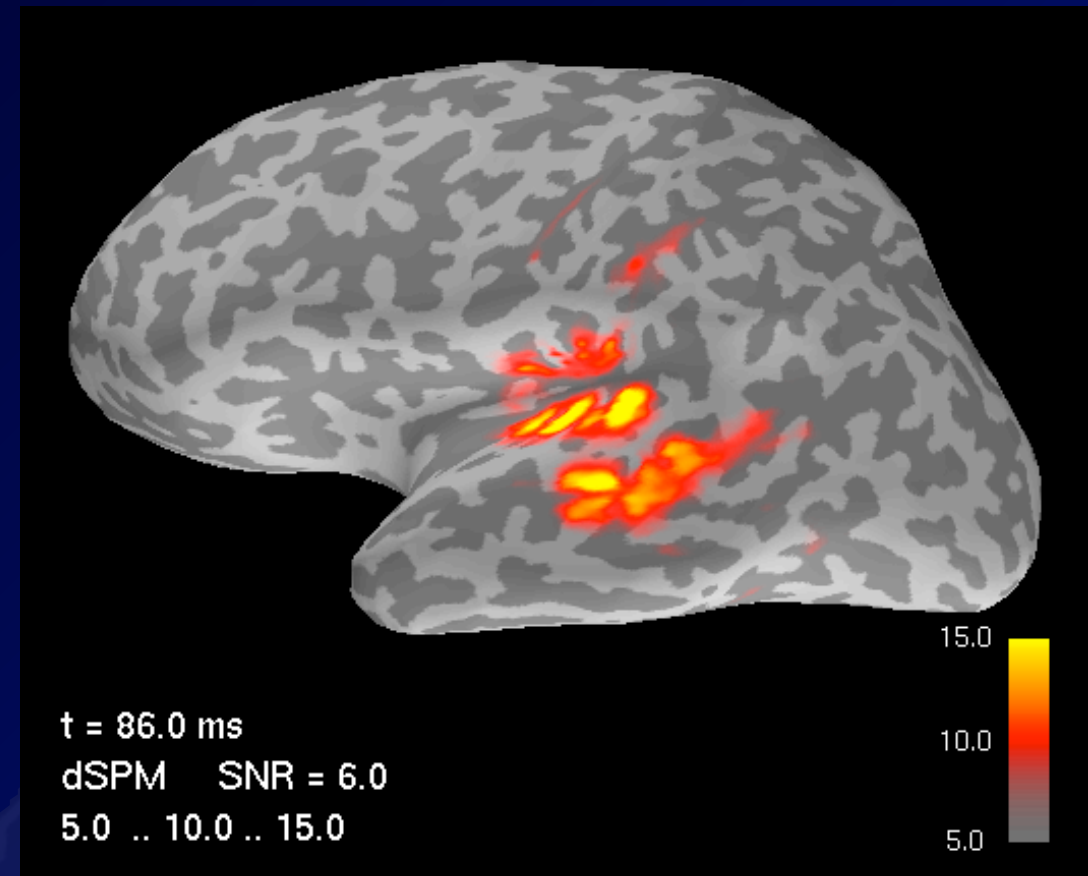
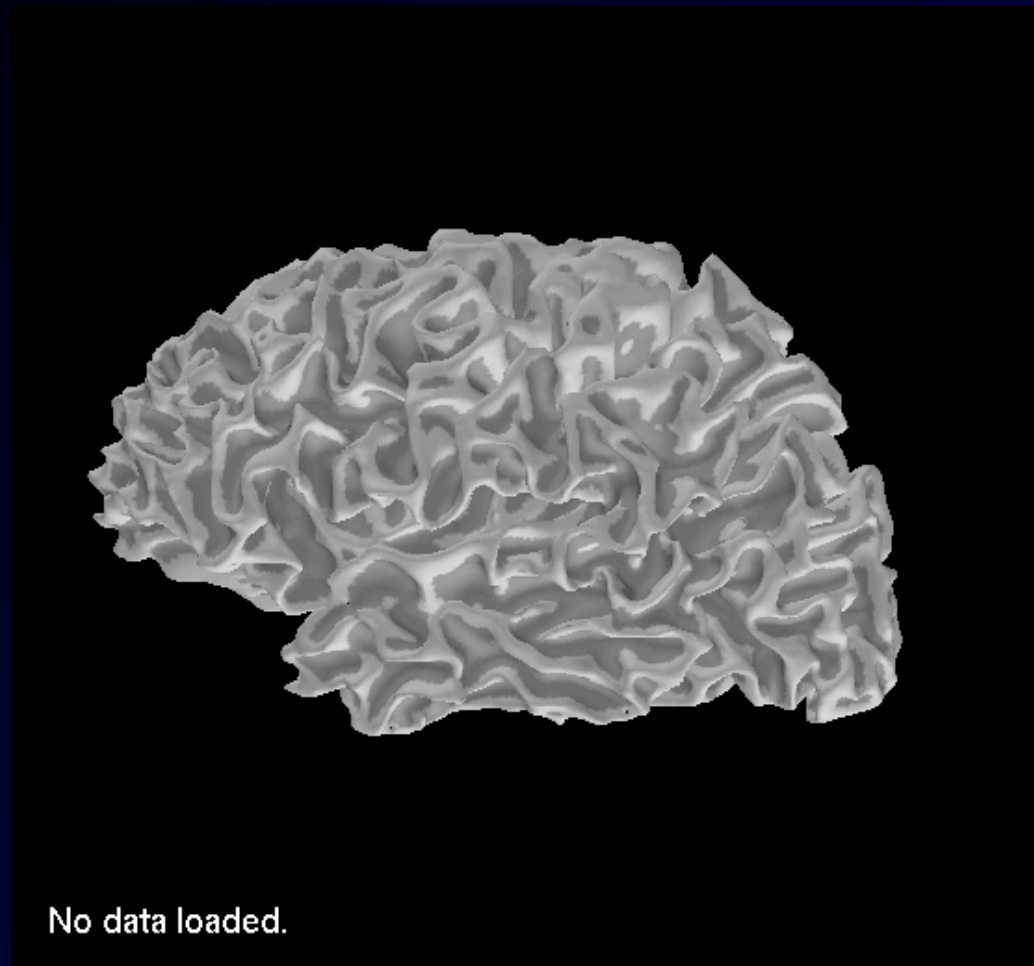


Topologically correct tessellation
can be inflated



Dale, Fischl, Sereno *et al.*

Inflated Cortex

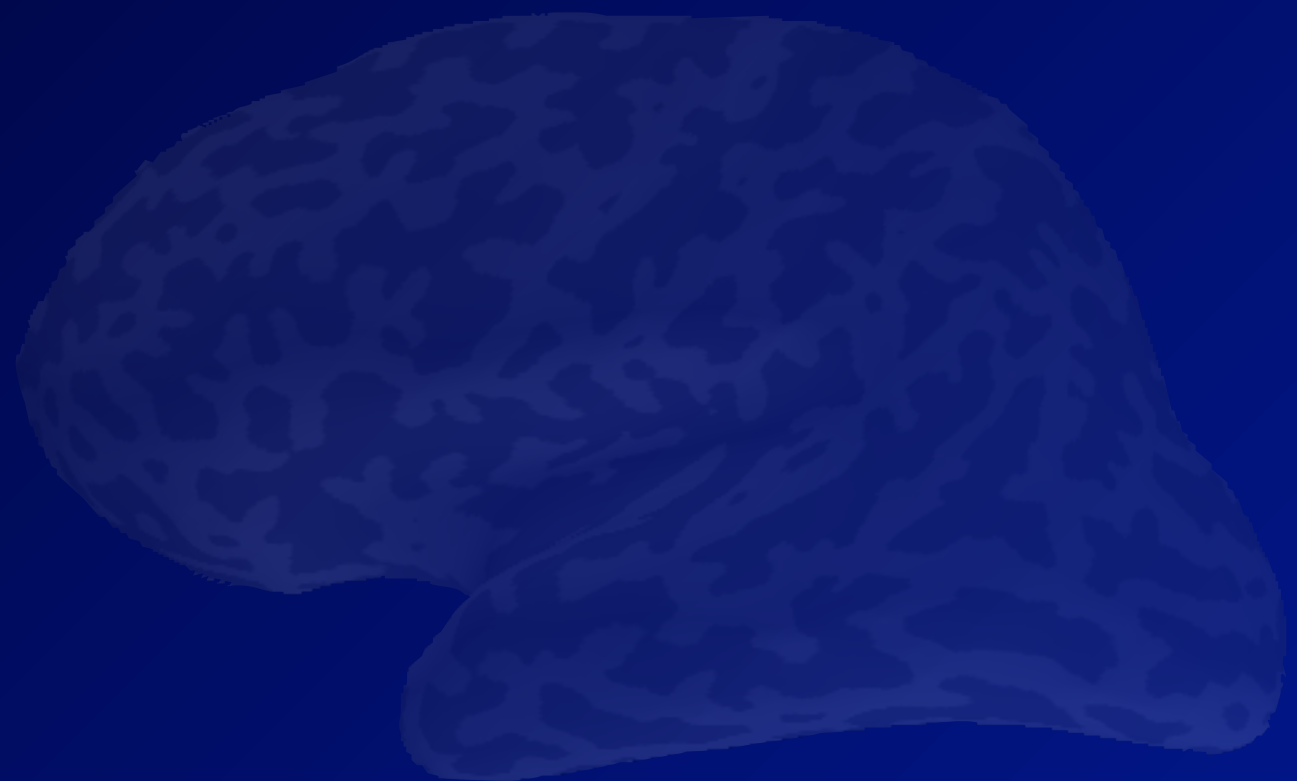
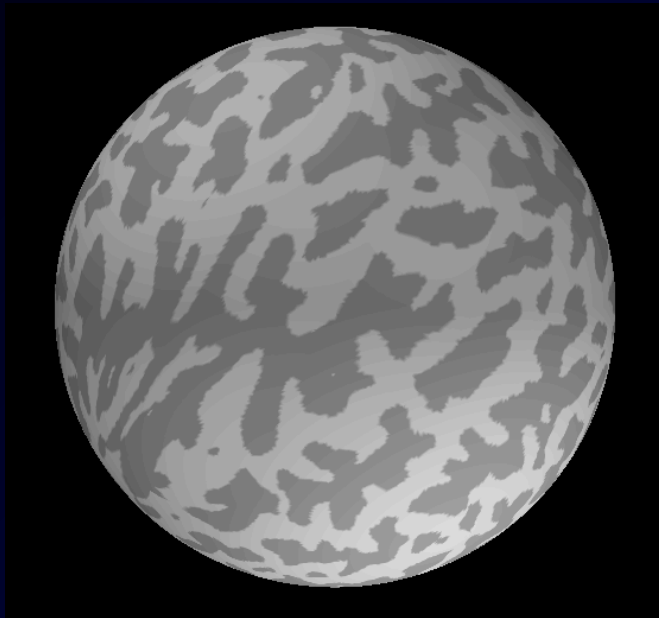


Topologically correct tessellation
can be inflated

Dale, Fischl, Sereno *et al.*

Inflation to a Sphere and Registration

Individual

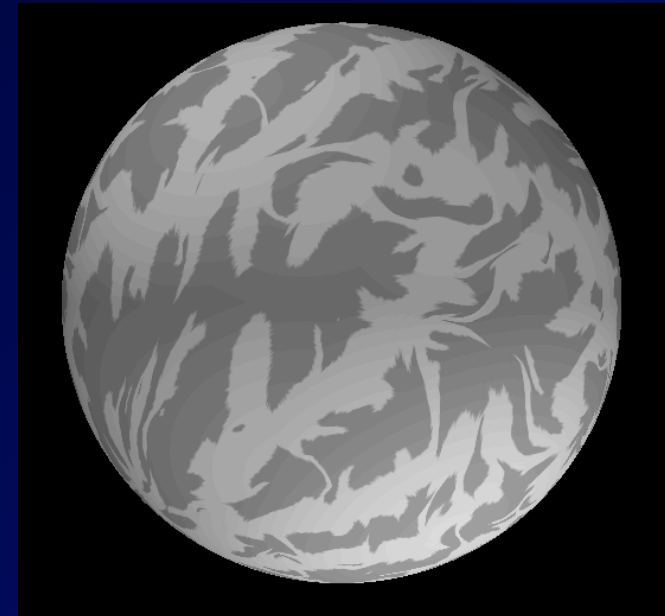


Inflation to a Sphere and Registration

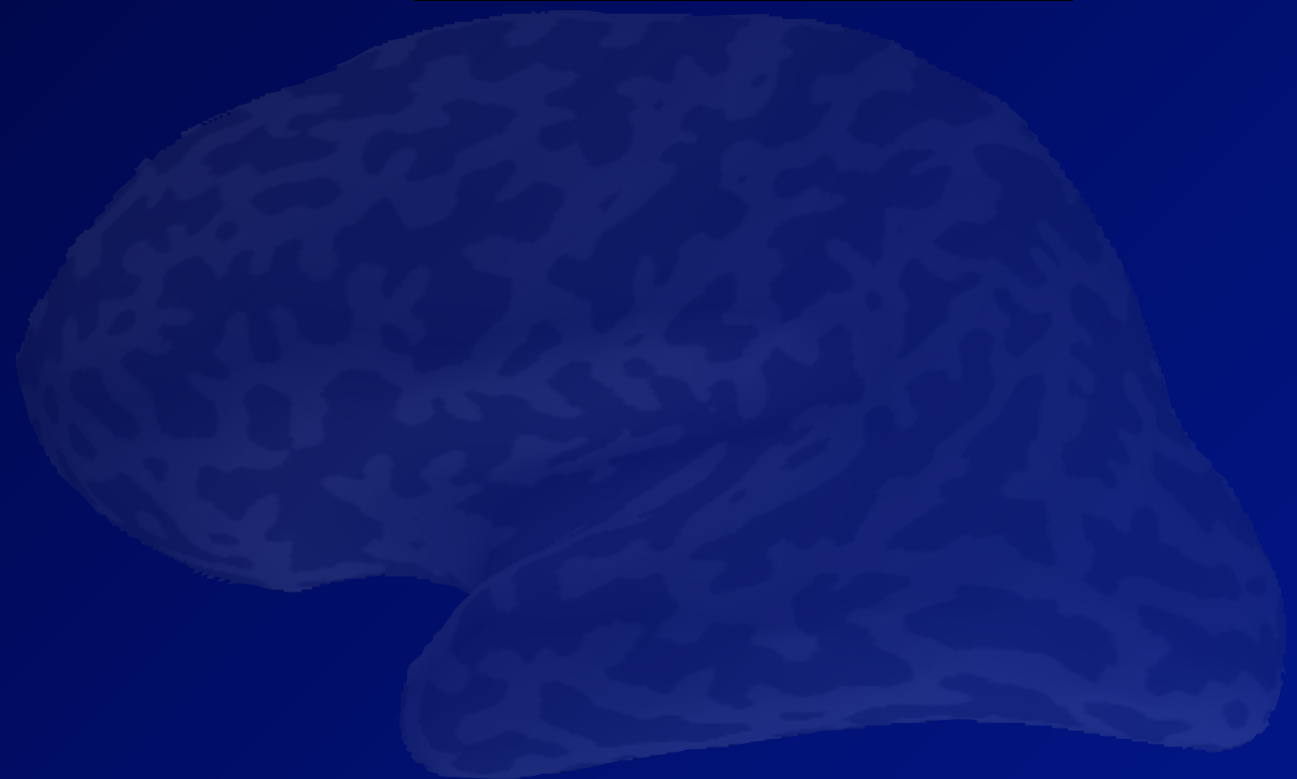
Individual



Aligned with average brain



Align sulcal patterns
→
to the average brain



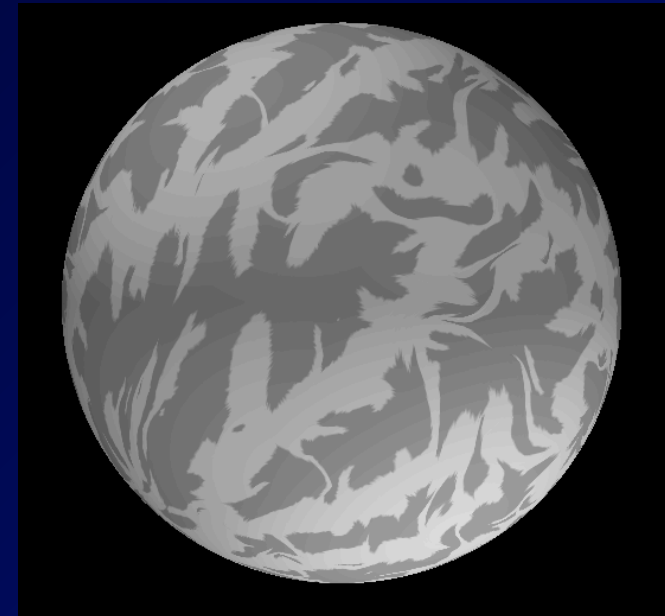
Inflation to a Sphere and Registration

Individual

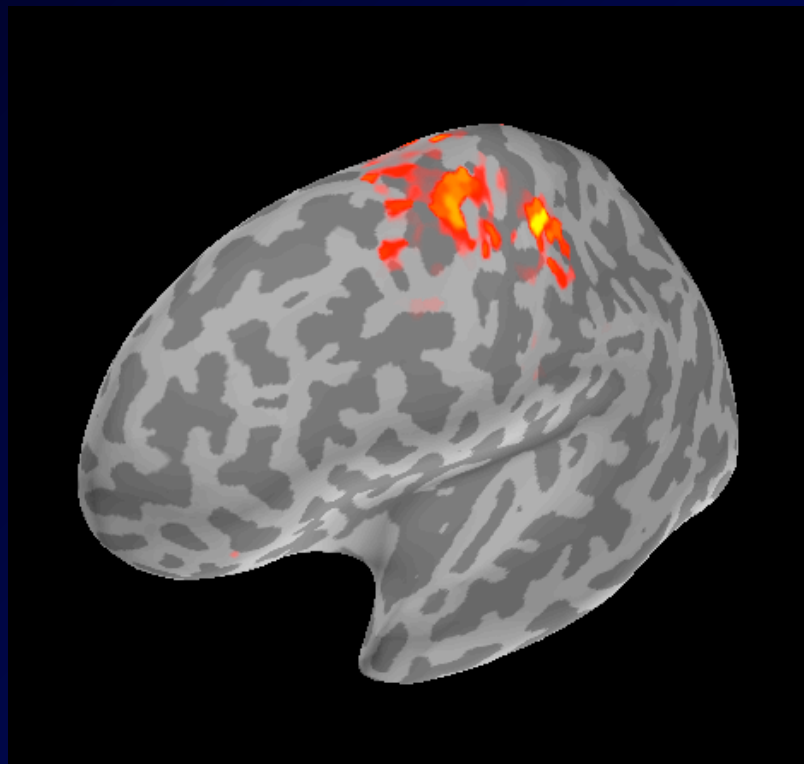
Aligned with average brain



Align sulcal patterns
→
to the average brain



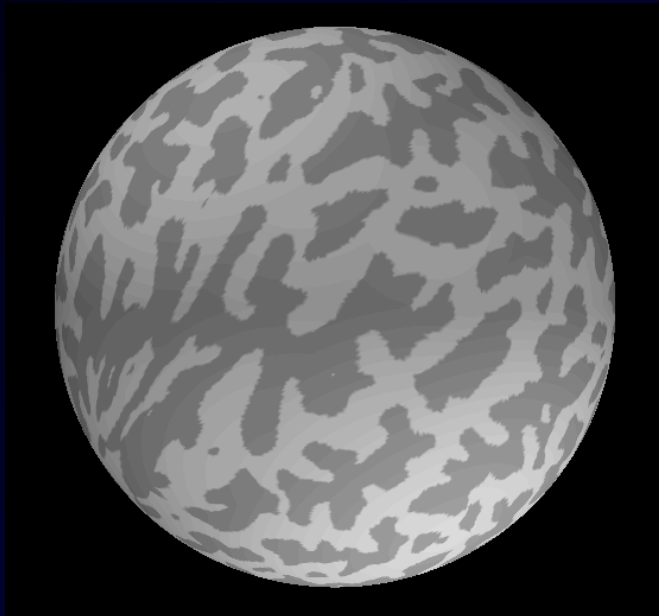
MEG activity estimate



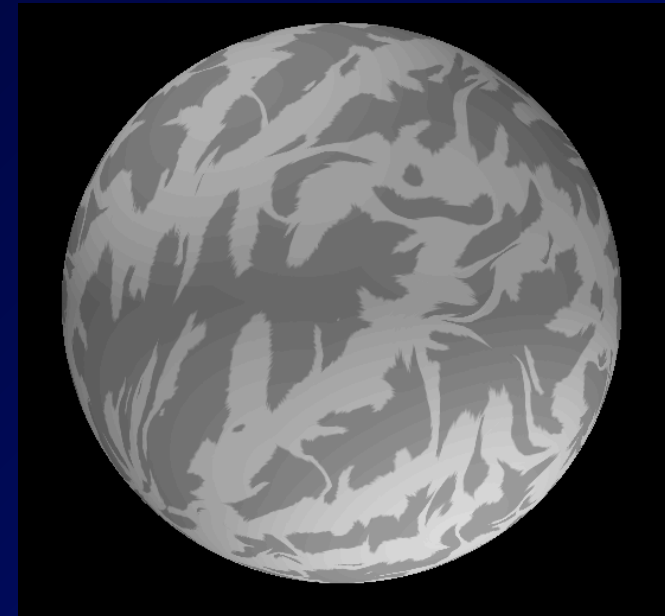
Inflation to a Sphere and Registration

Individual

Aligned with average brain

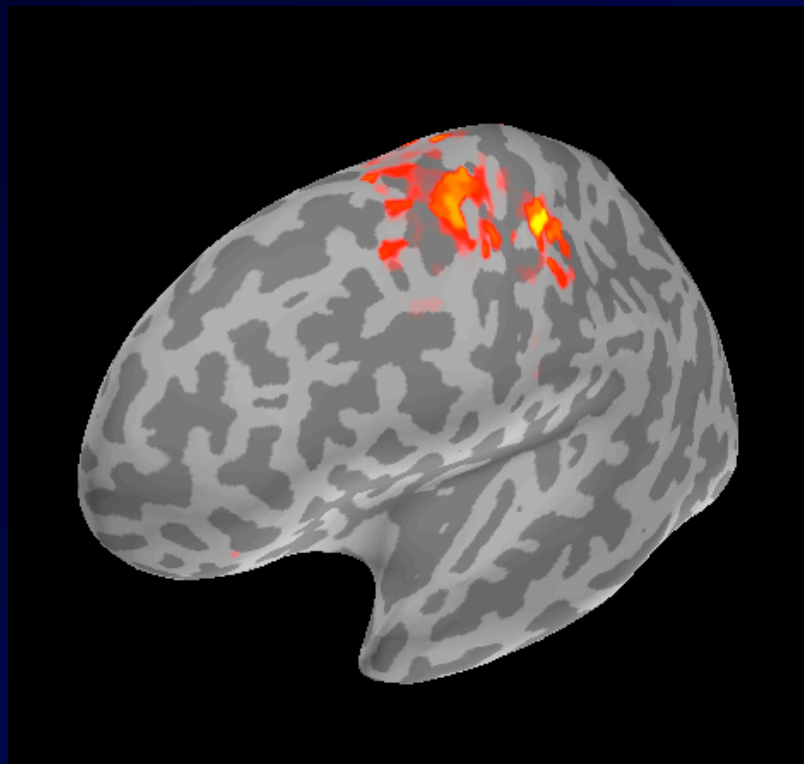


Align sulcal patterns
→
to the average brain

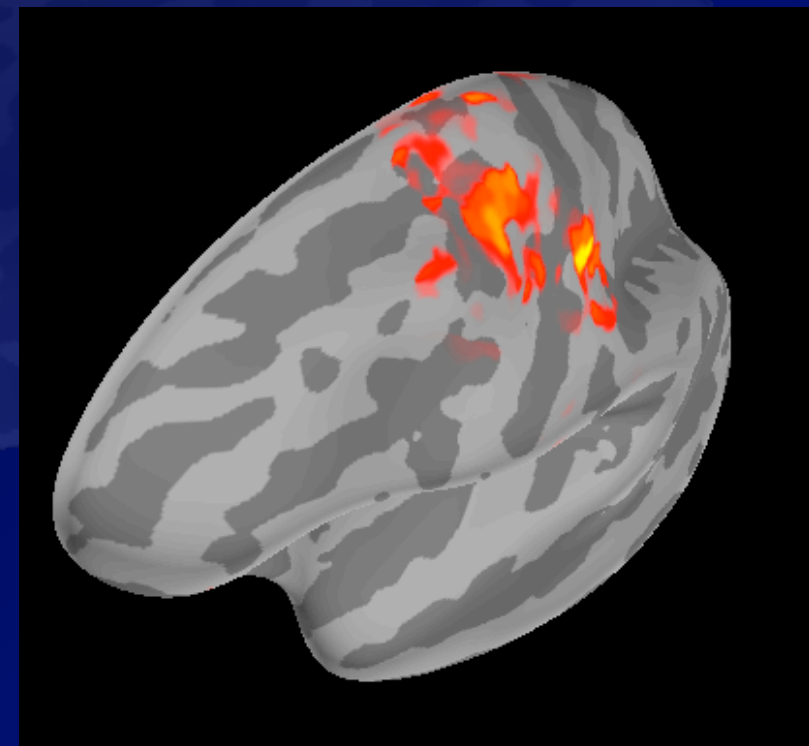


MEG activity estimate

Mapped to the average brain



Morph



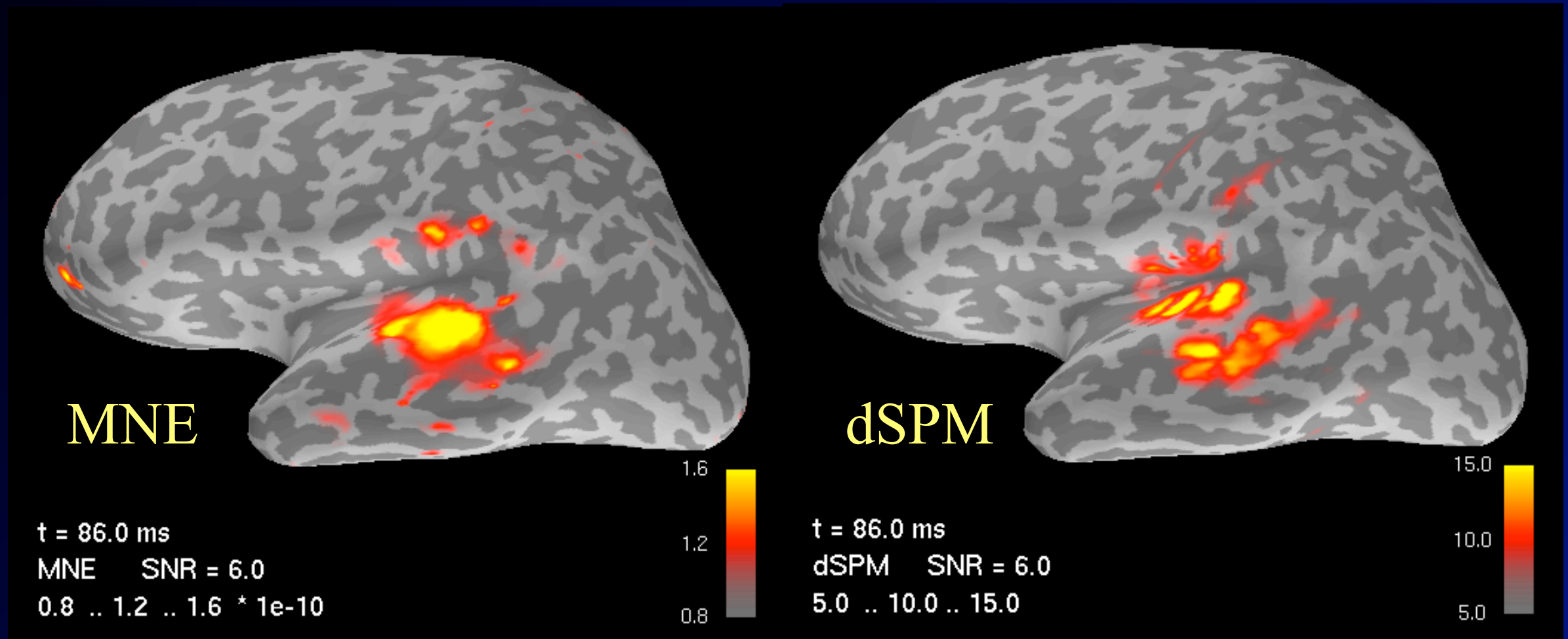
Noise normalization

- Convert the current values into a test statistic
 - dSPM (Dale *et al.*)
 - sLORETA (Pascual-Marqui *et al.*)
- Divide the current with its standard deviation
- Analyze MEG/EEG data like fMRI or PET



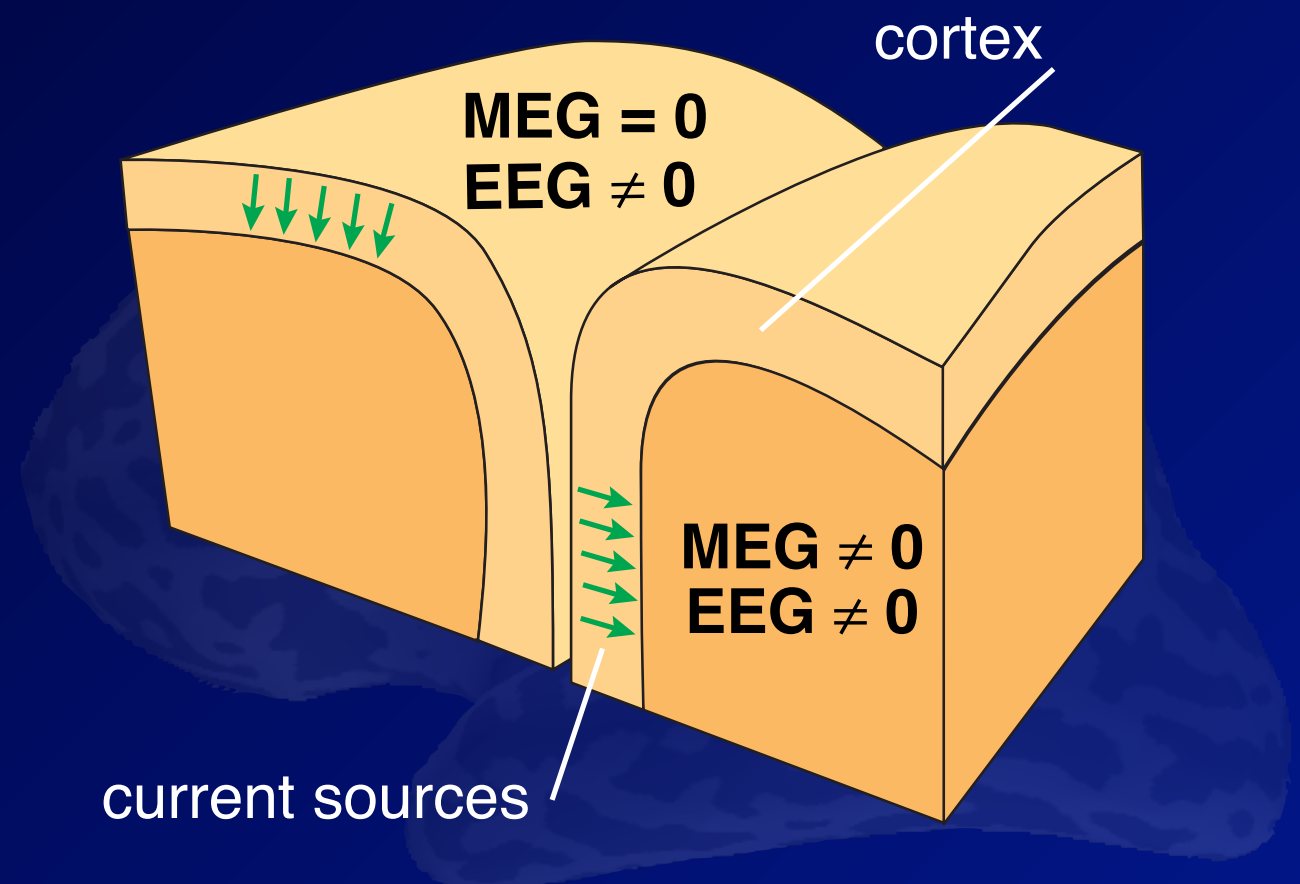
Dale *et al.* 2000

MNE and dSPM



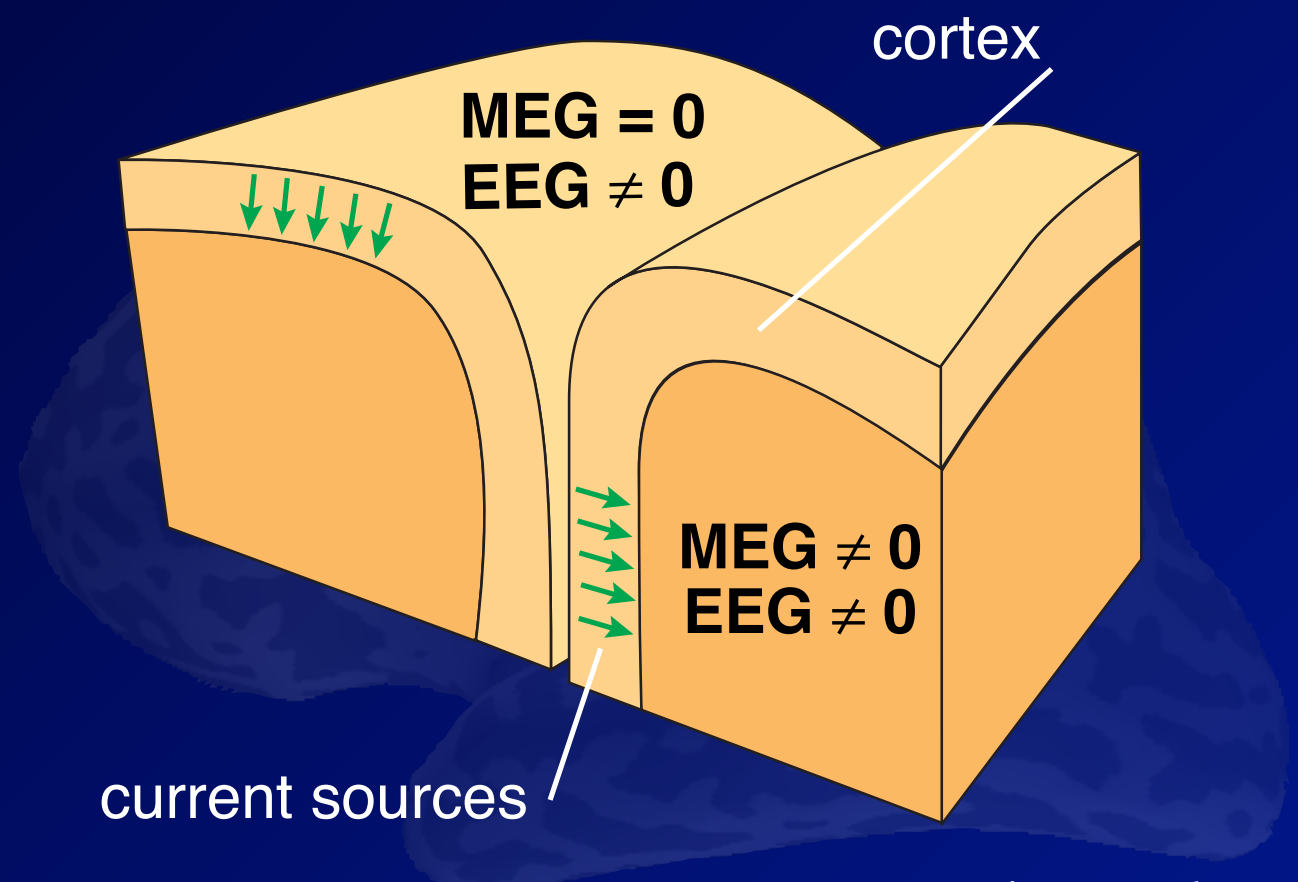
- Auditory MEG data
- Source locations constrained to the cortex
- No orientation constraint
- dSPM and sLORETA produce very similar results with real data

Loose orientation constraint



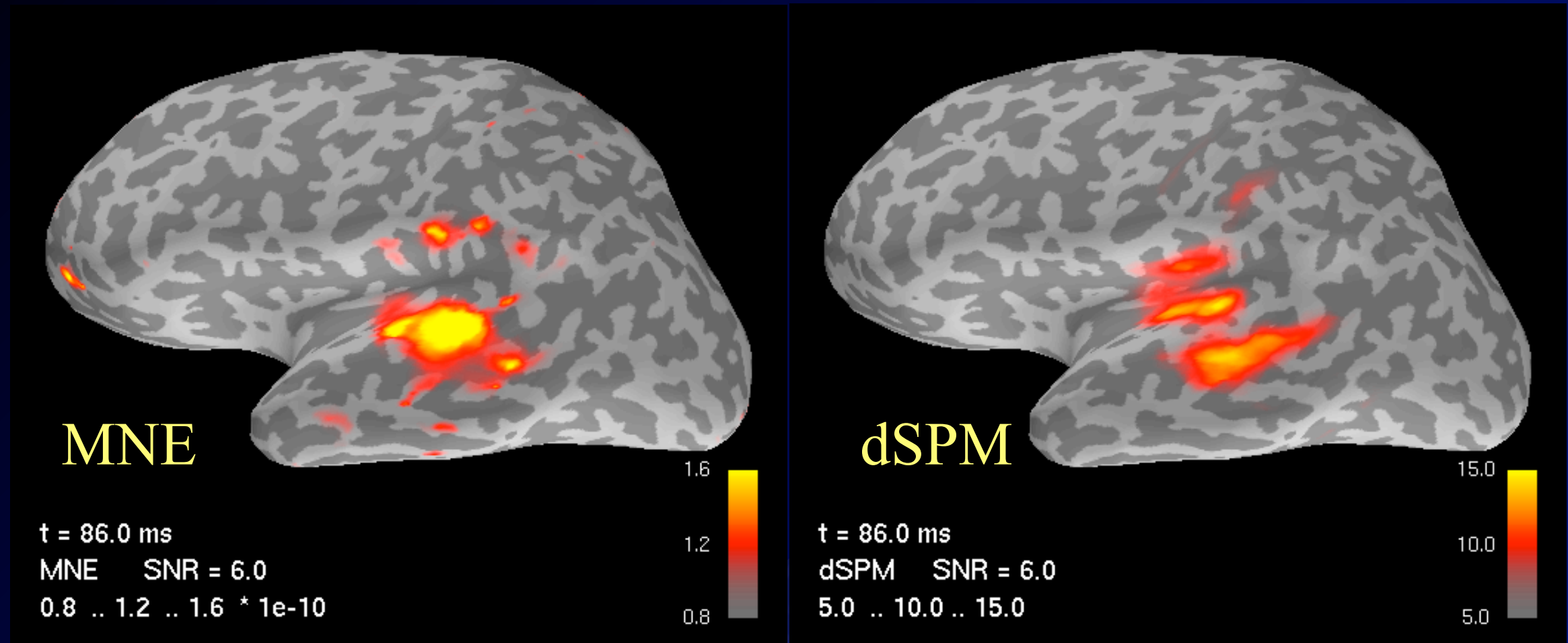
Loose orientation constraint

- Penalize current components tangential to the cortex
- Takes the finite spacing between elementary sources into account



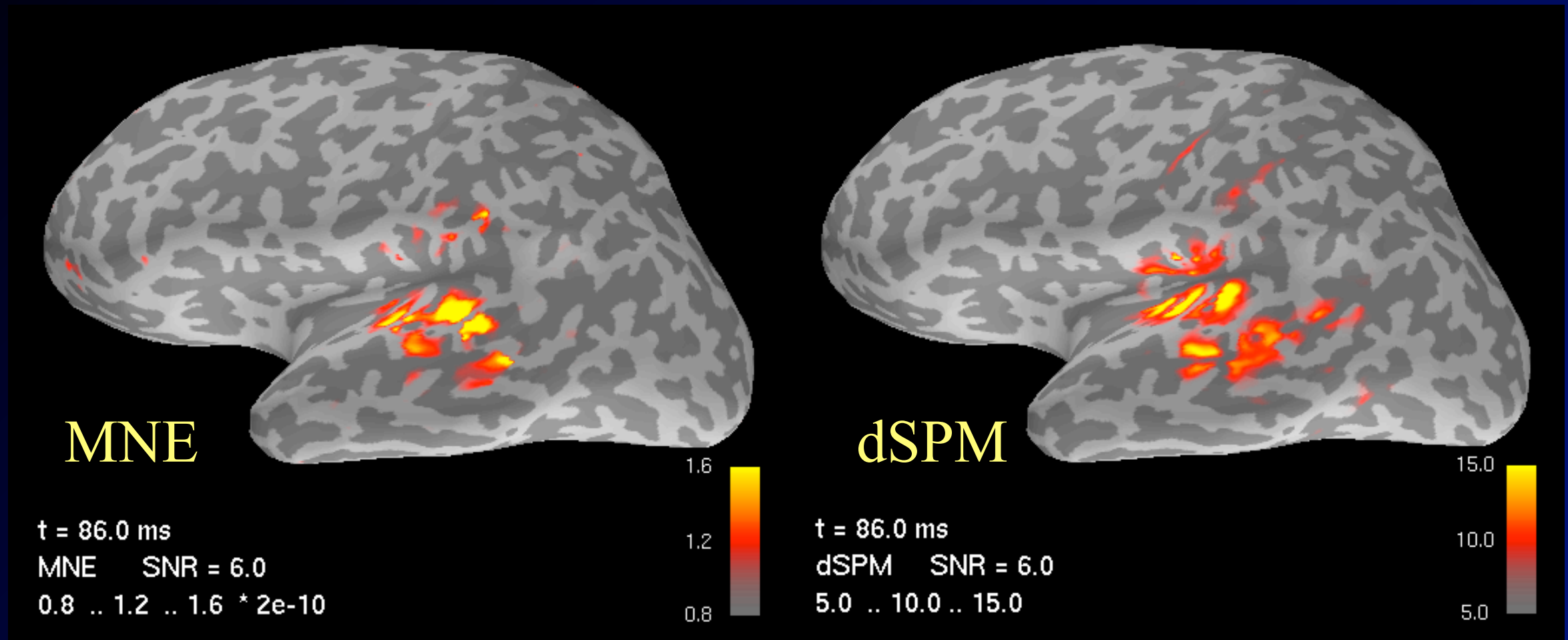
Lin *et al.* 2006

Effect of the orientation constraint



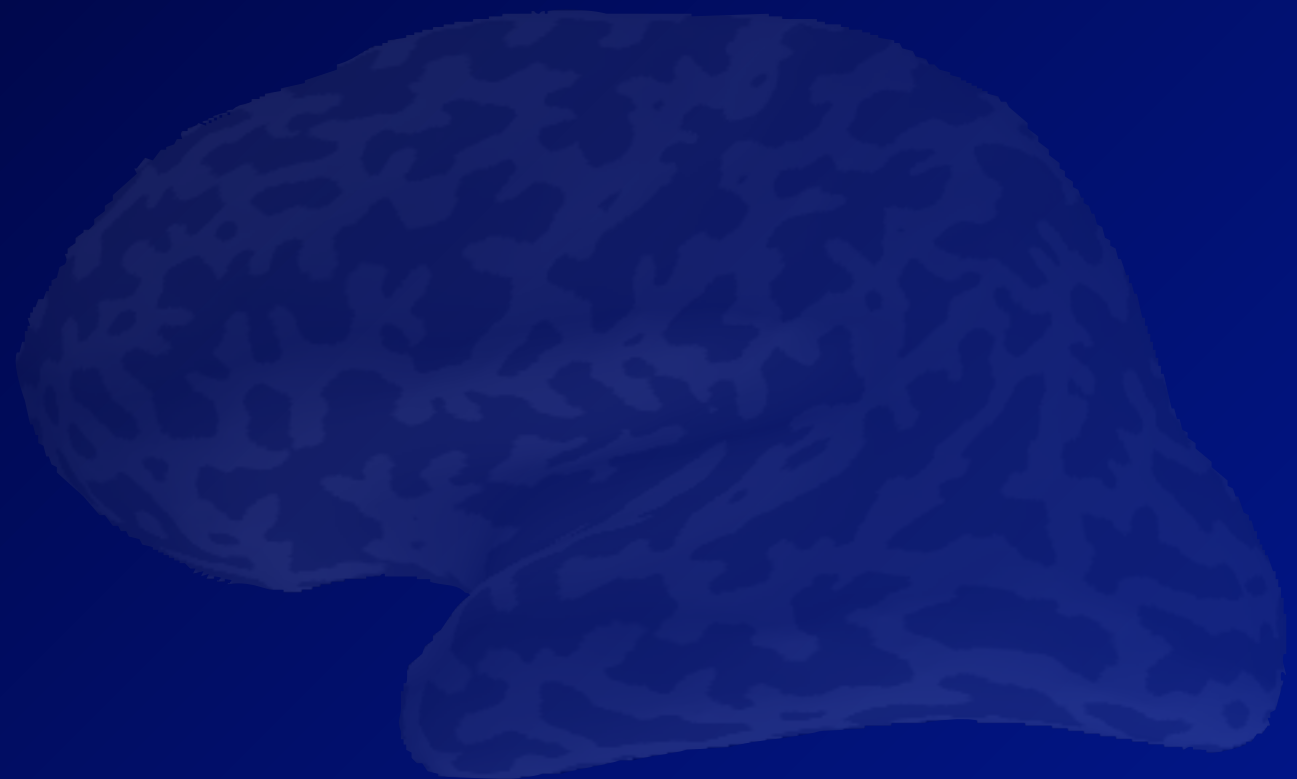
- Auditory responses to short tones
- Depth-weighted MNE and dSPM
- Without and with loose orientation constraint
- The orientation constraint rules out infeasible sources

Effect of the orientation constraint

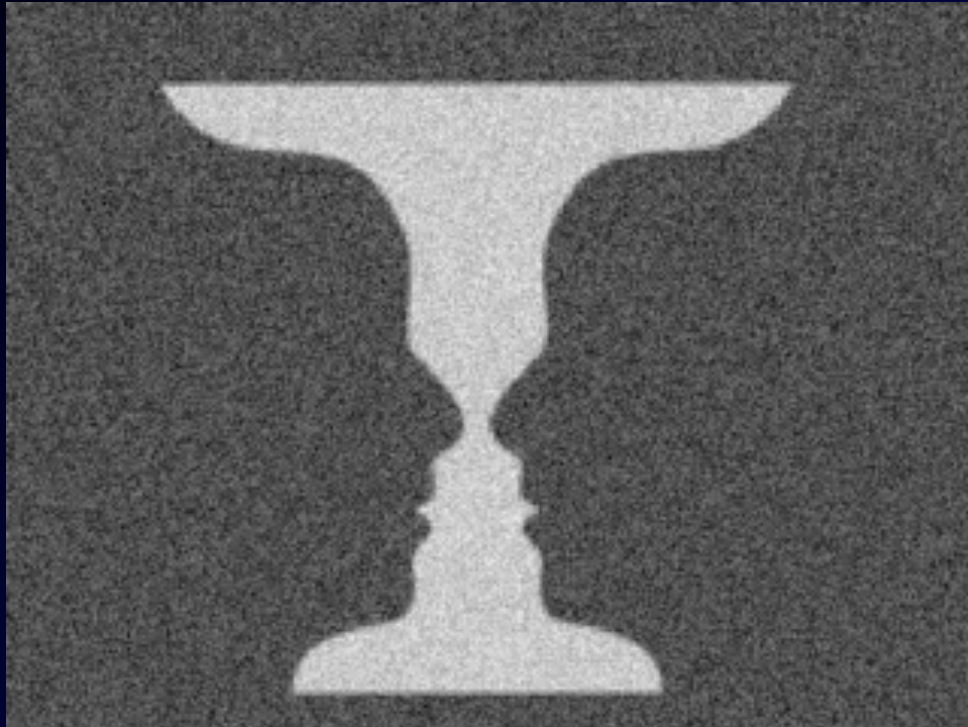


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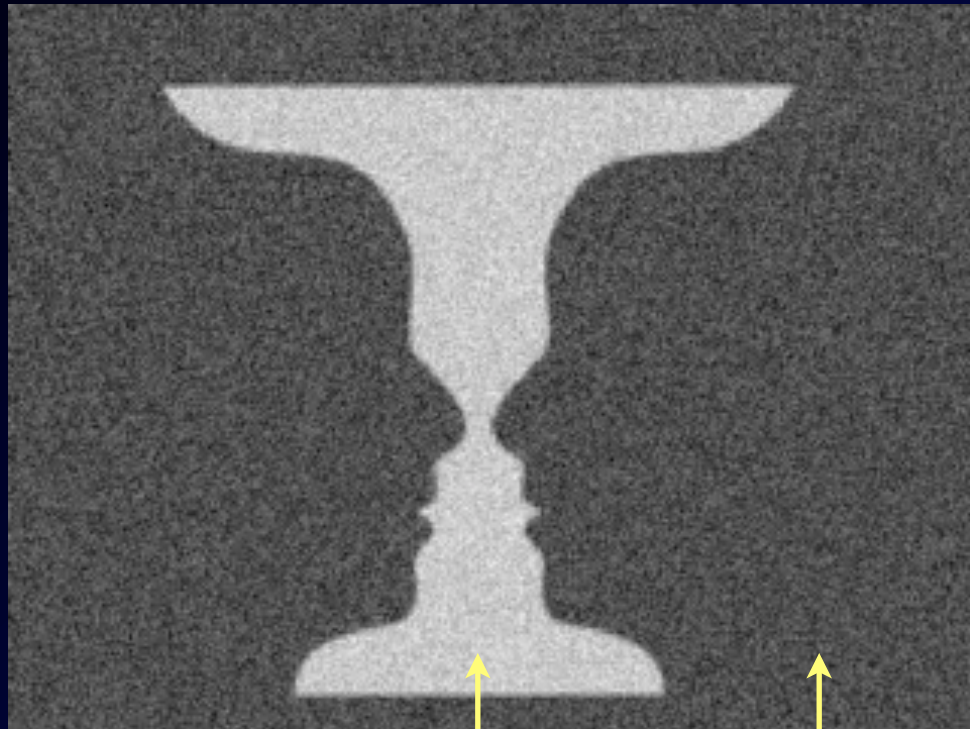
Visual percepts of an ambiguous scene



Visual percepts of an ambiguous scene



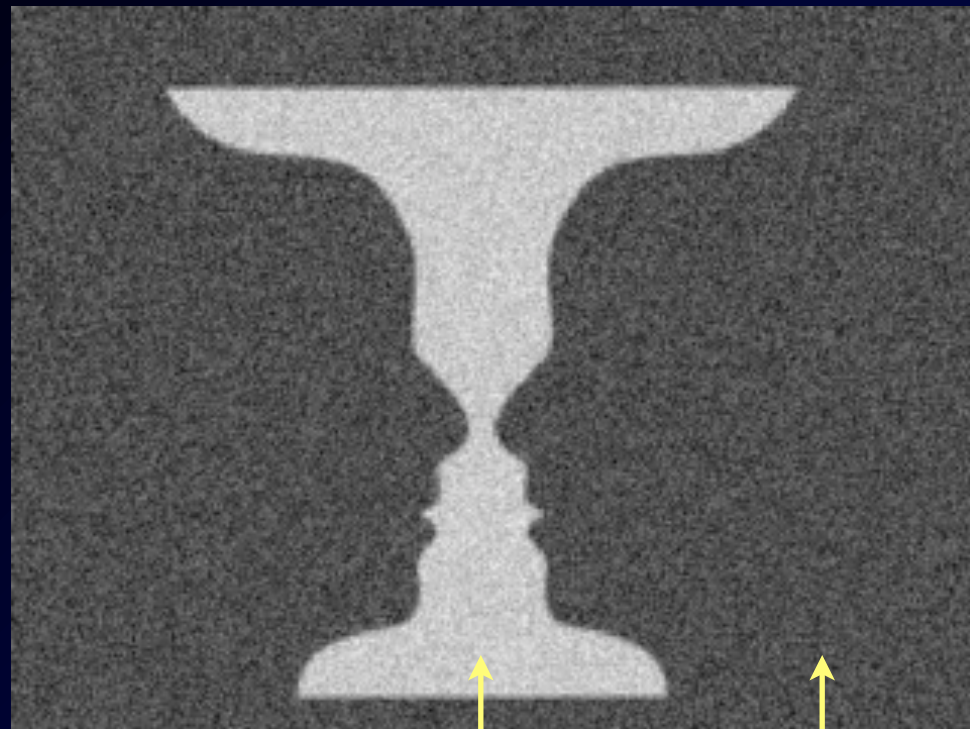
Visual percepts of an ambiguous scene



Noise: 12 Hz 15 Hz

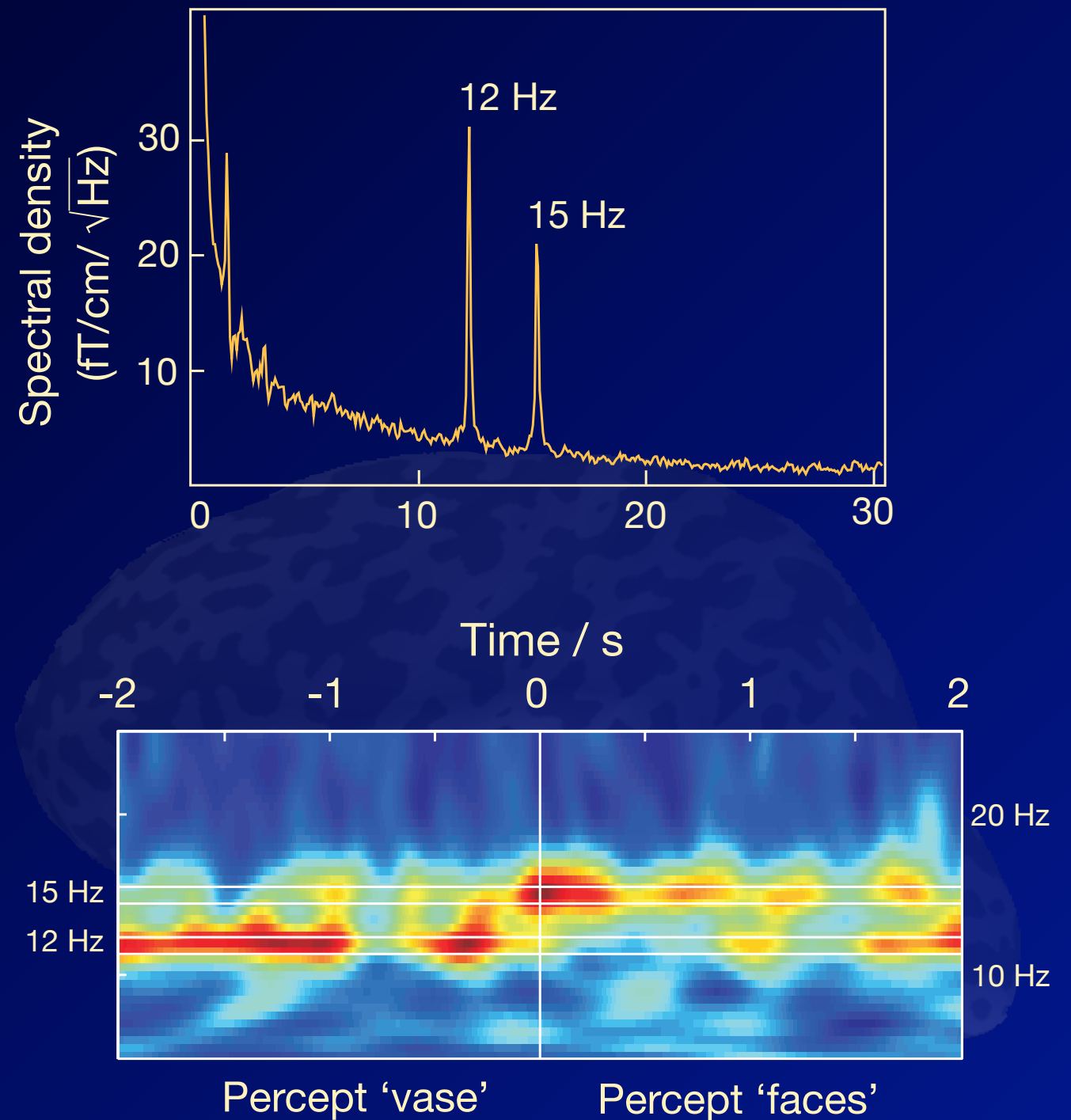


Visual percepts of an ambiguous scene



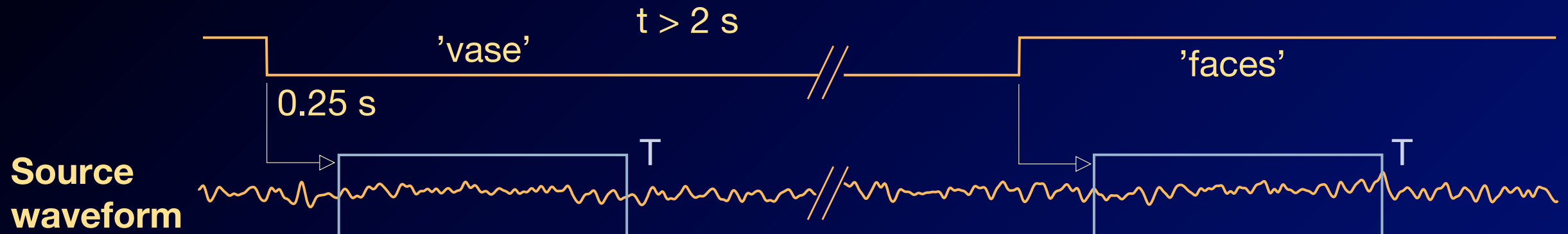
Noise: 12 Hz 15 Hz

MEG signals at an occipital sensor



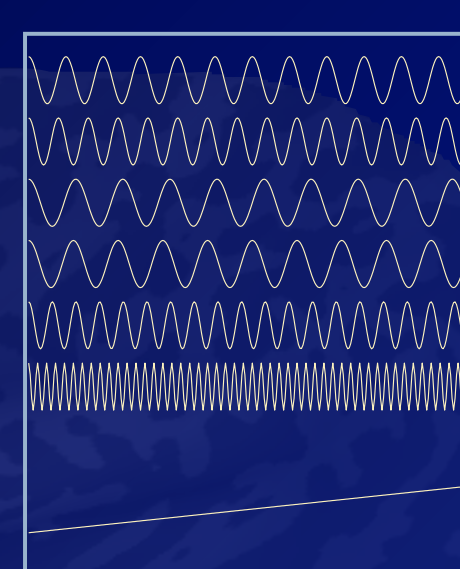
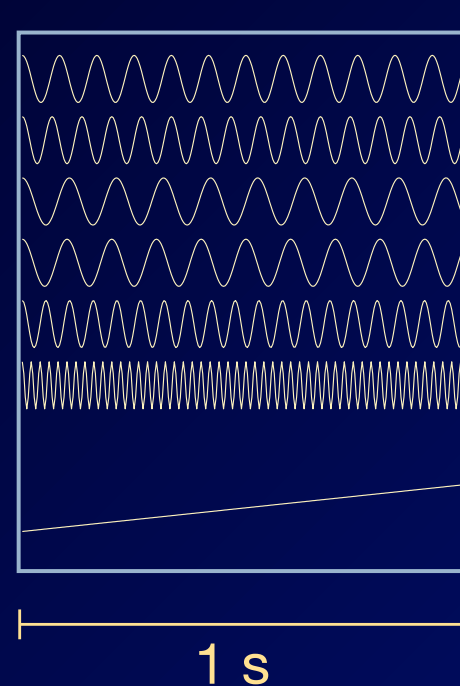
Extract tag-related activity: MNE + GLM

Behavioral report



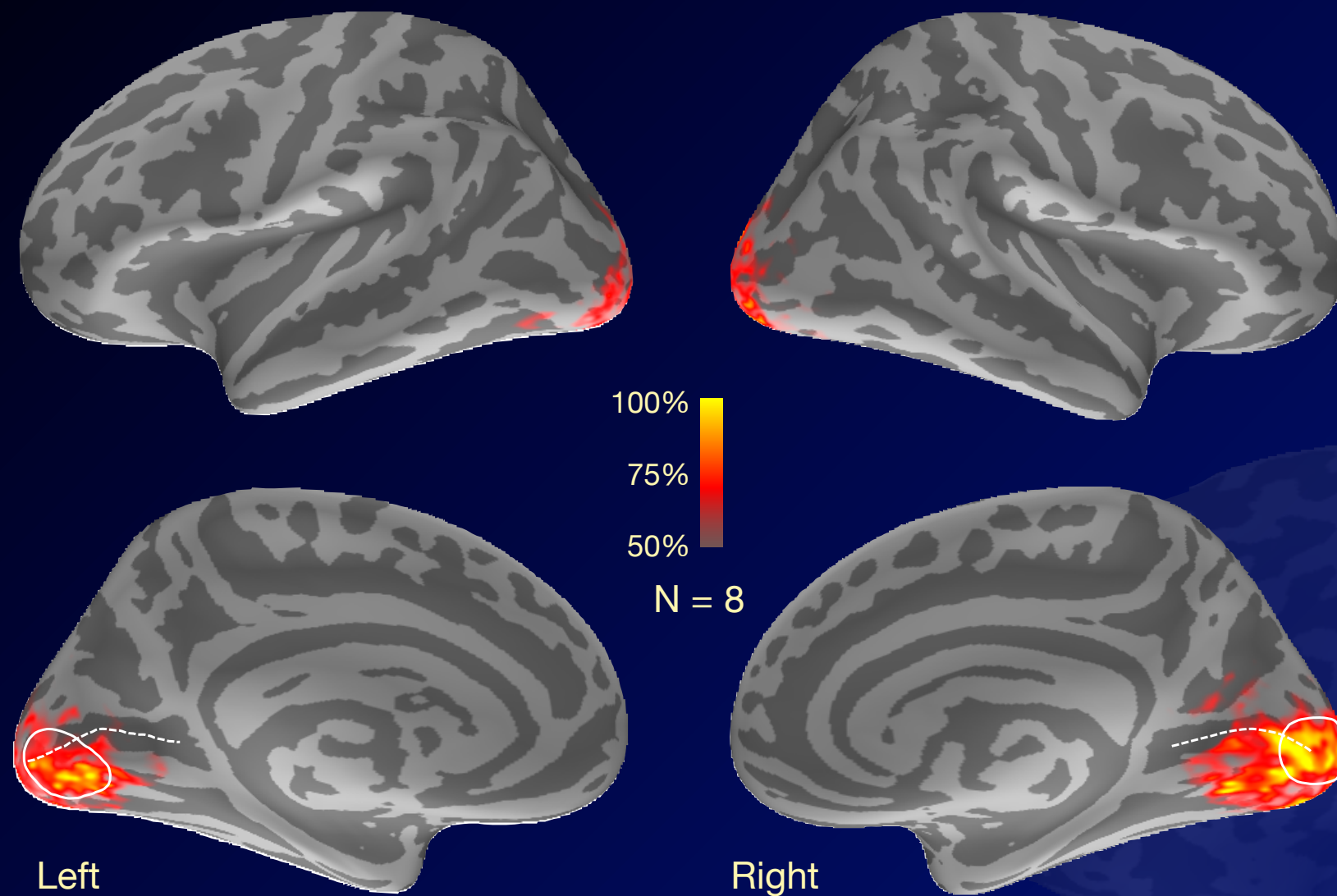
GLM

tags 12.0 Hz
 15.0 Hz
 alpha 9.5 Hz
 mu 10.0 Hz
 18.9 Hz
 mains 50.0 Hz
 linear trend

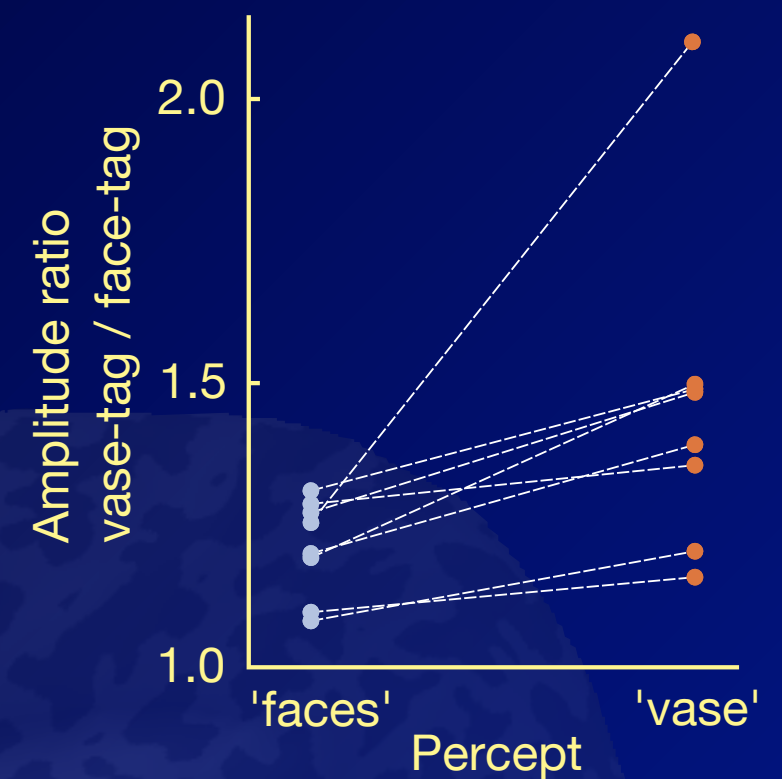


Group analysis

Significant activity in either tag frequency



Amplitude ratio
at ROI

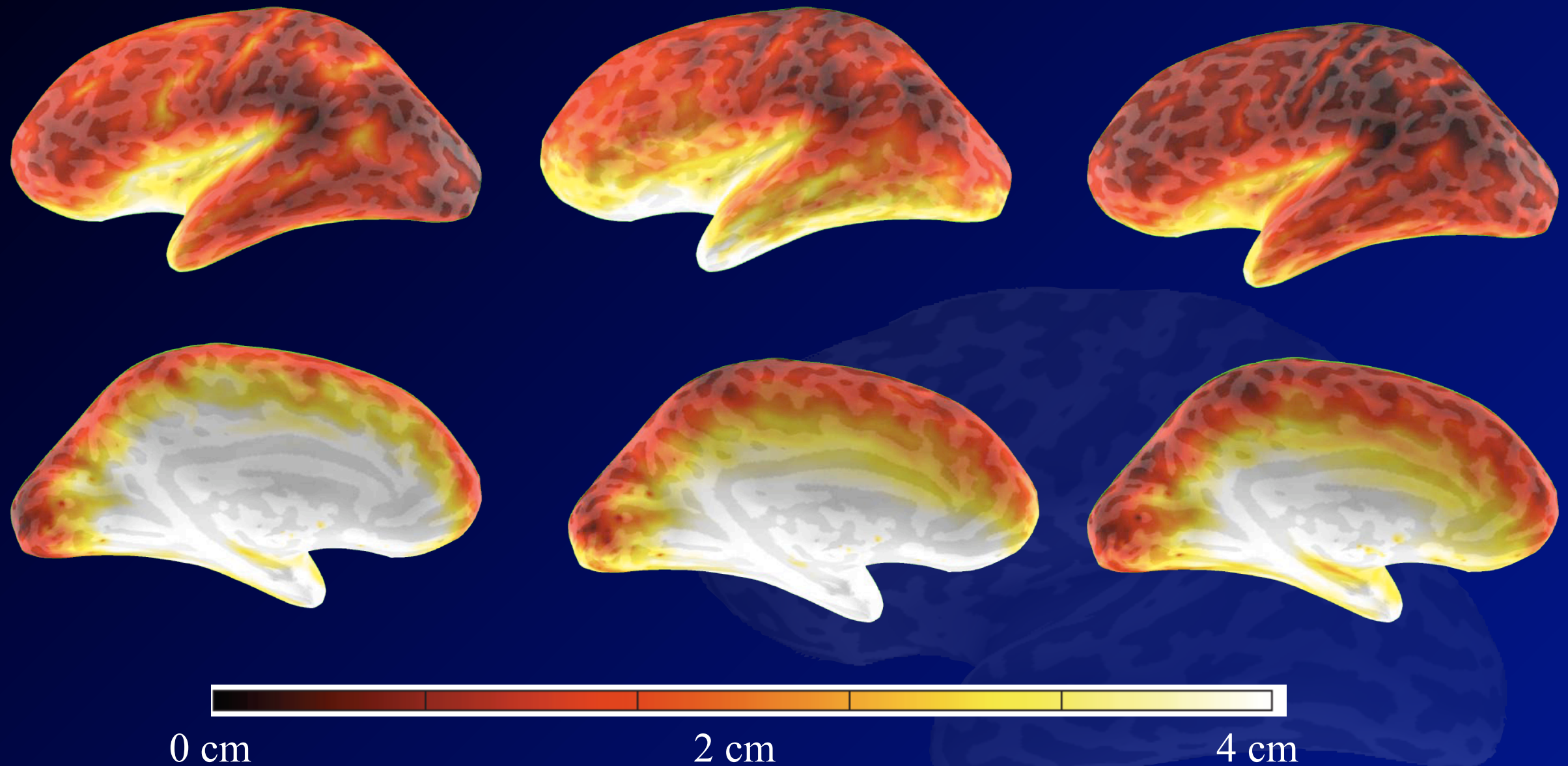


Spatial dispersion of cortically-constrained MEG and EEG source estimates

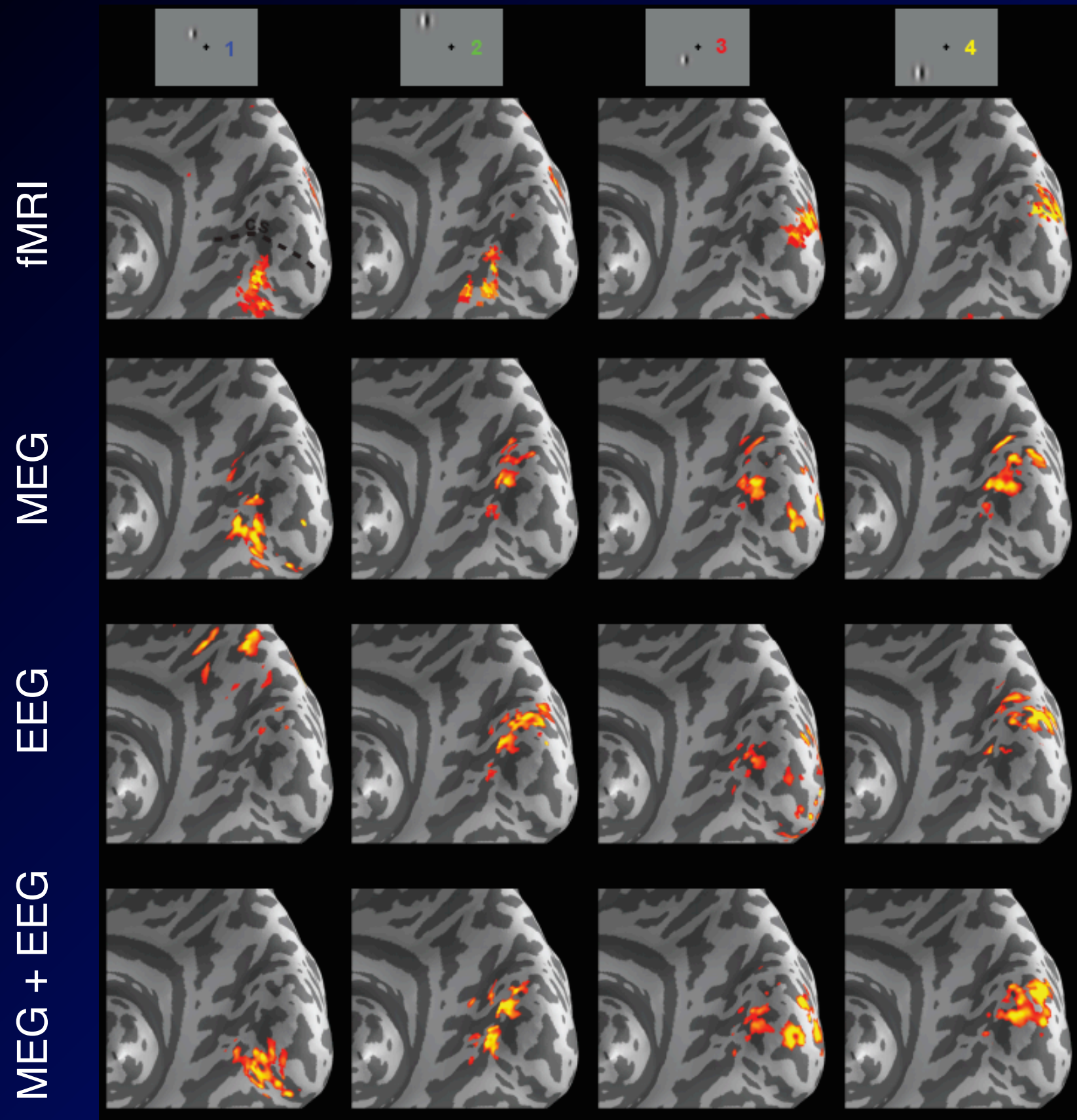
MEG

EEG

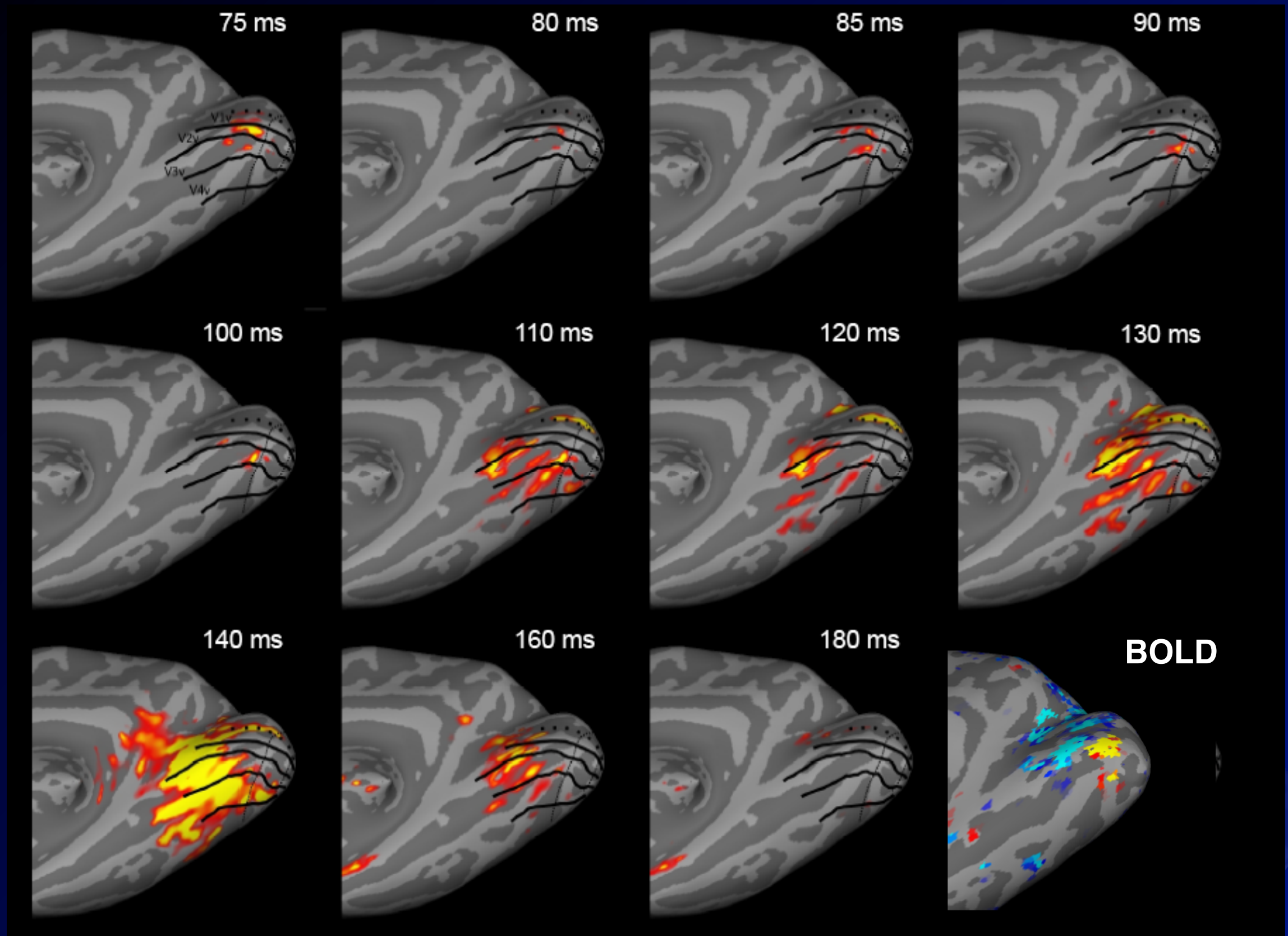
MEG+EEG



Comparison of MEG, EEG, and fMRI (dSPM)



MEG/EEG response dynamics



fMRI-guided estimates

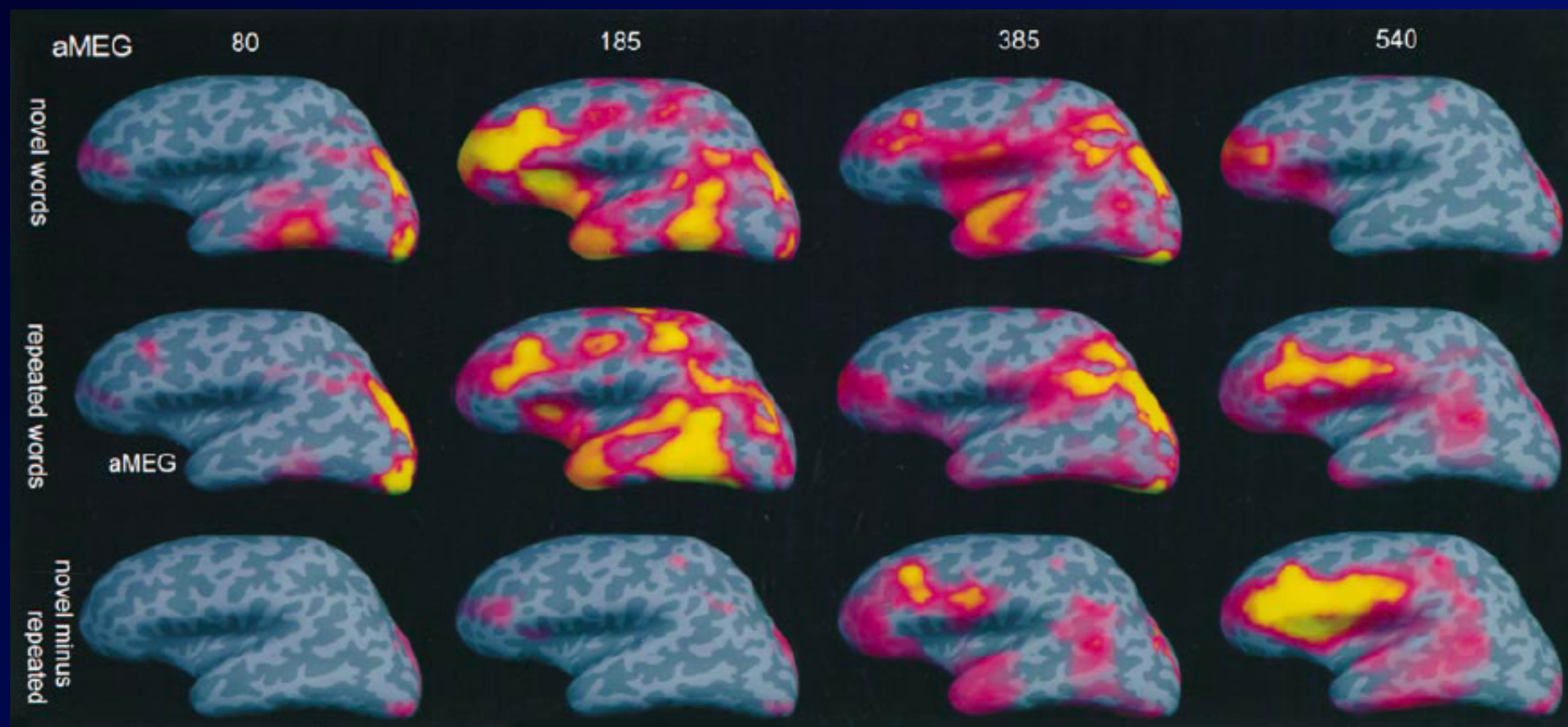
- Prioritize locations of significant fMRI activity (increase source variance)
- fMRI incorporated as a constraint, not an integrated analysis procedure



Dale *et al.* 2000

fMRI-guided estimates

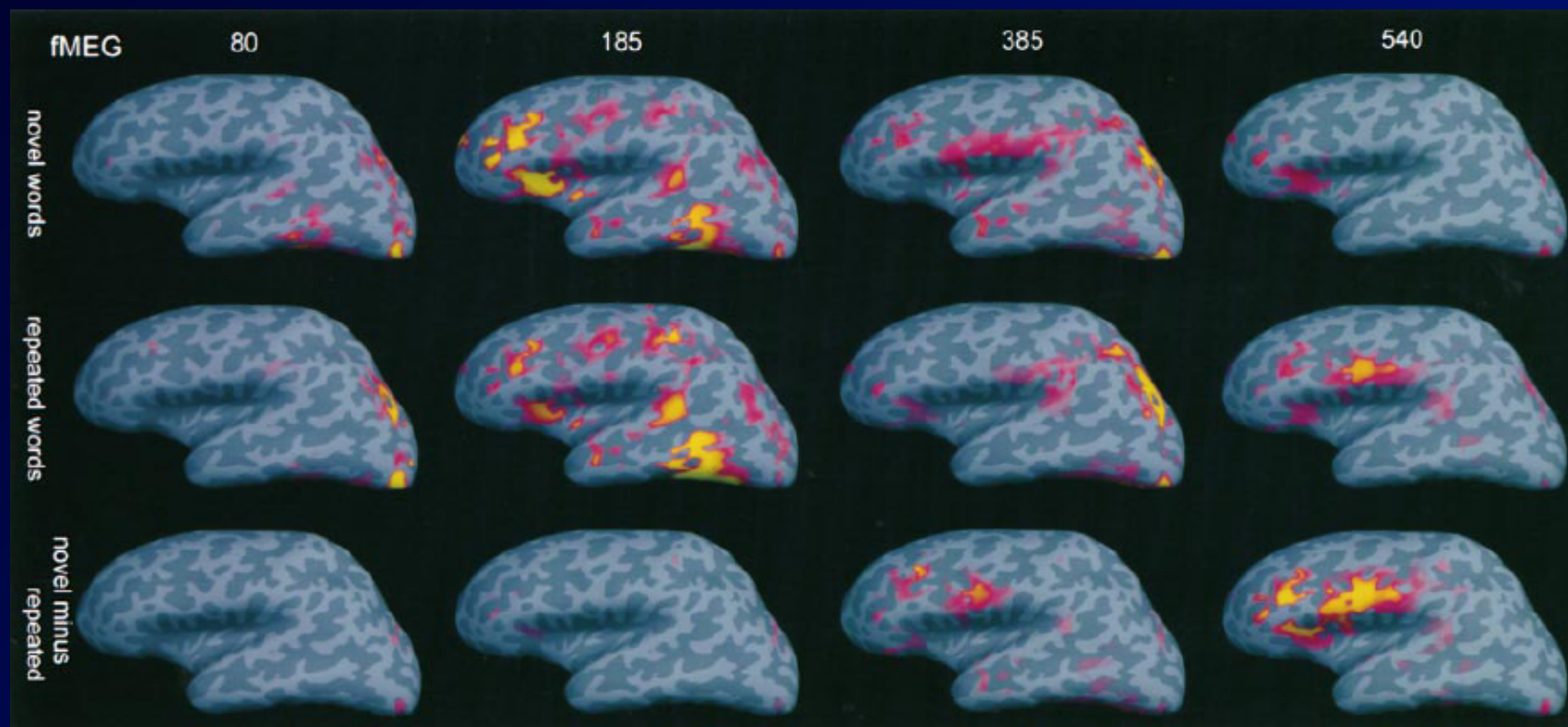
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Dale *et al.* 2000

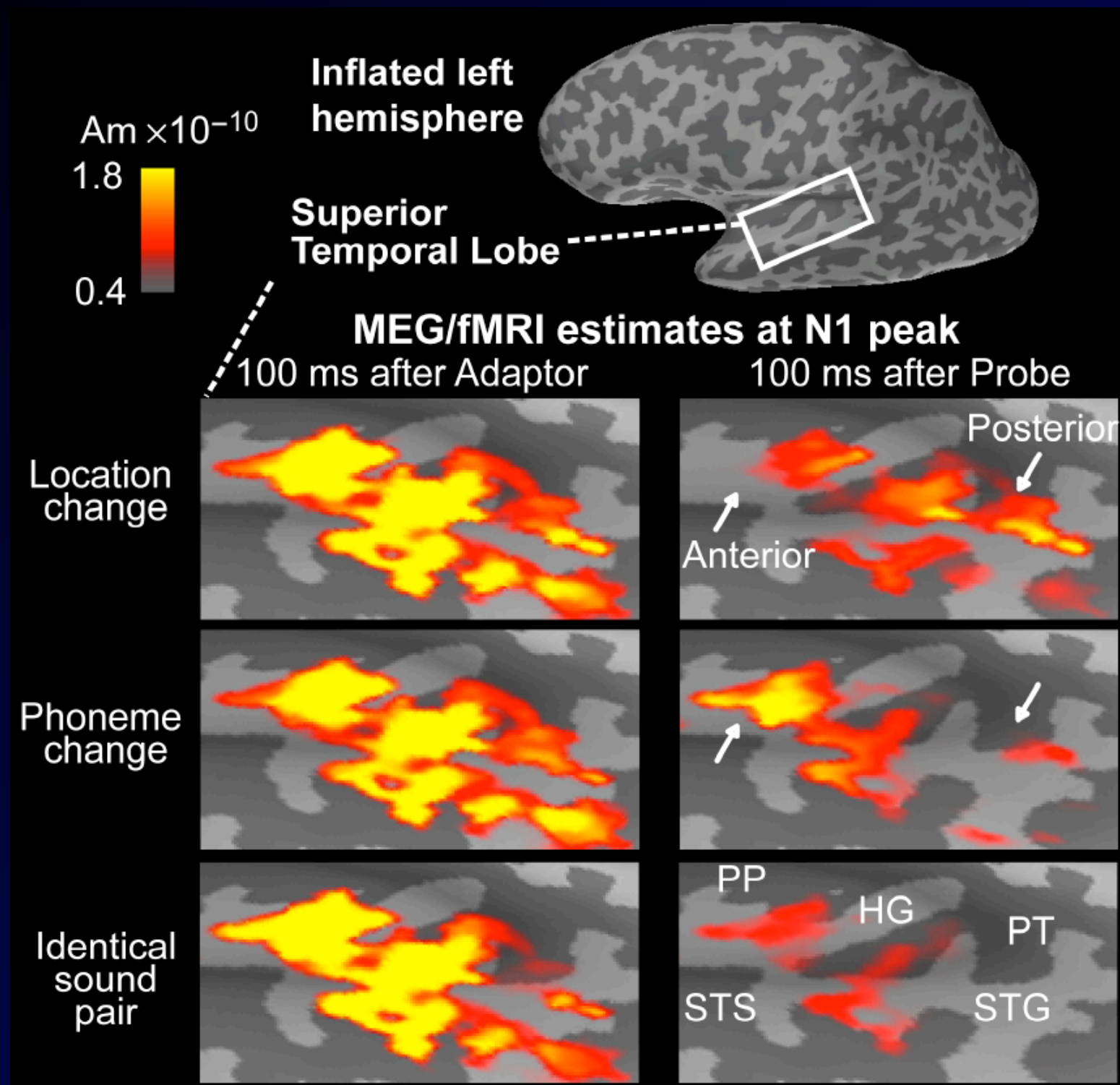
fMRI-guided estimates

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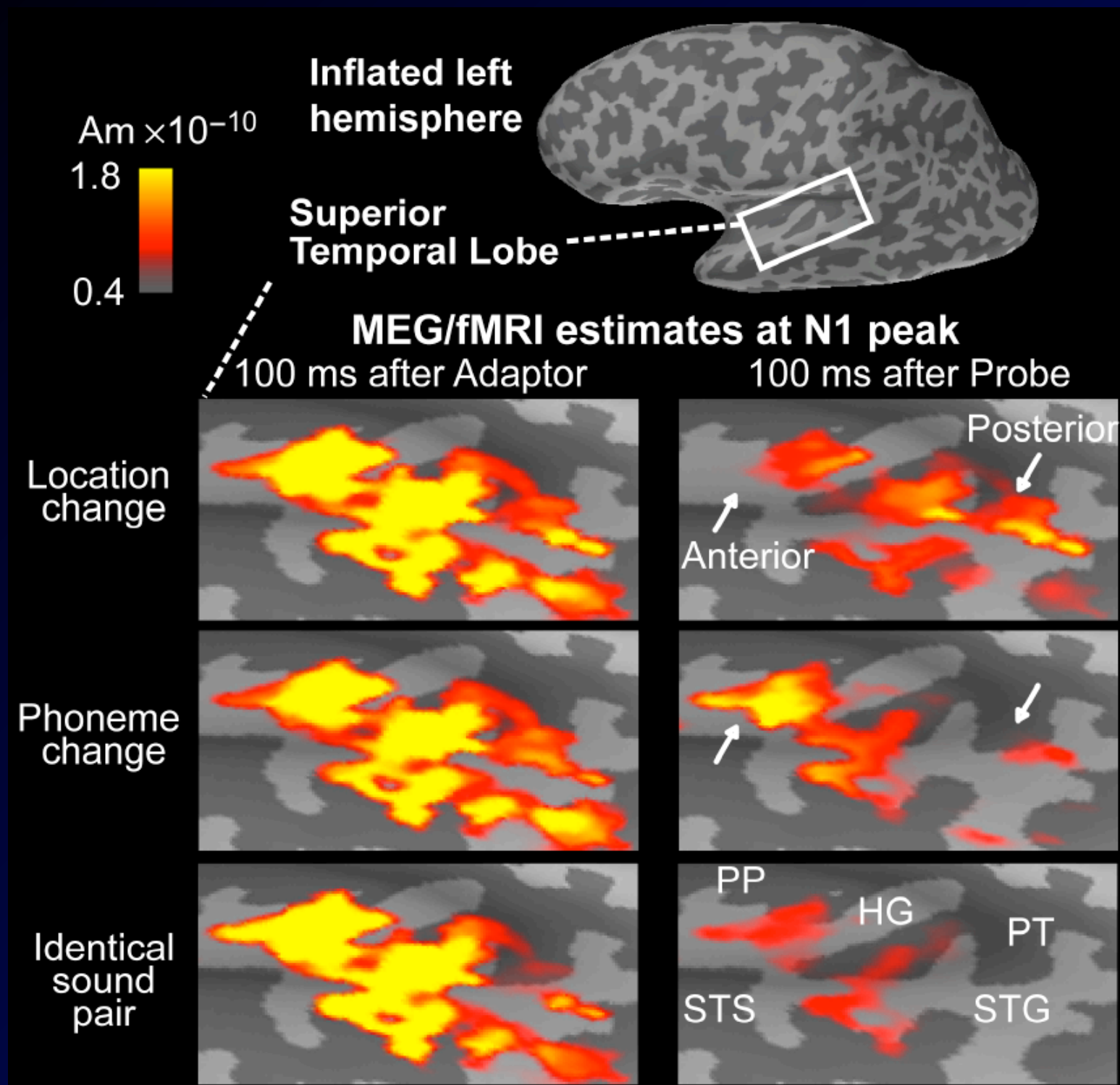
Dale *et al.* 2000

What and Where pathways in the auditory cortex

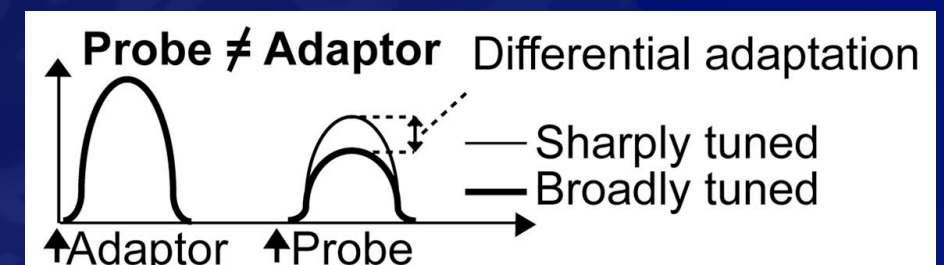
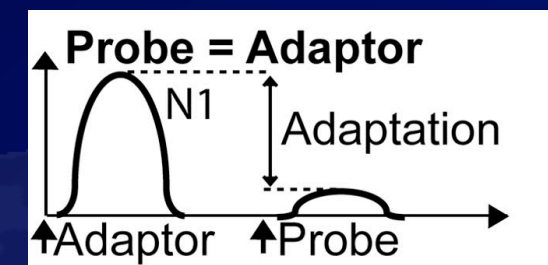


fMRI weighted MEG estimates to sound pairs which were different in location, phonemic content, or neither

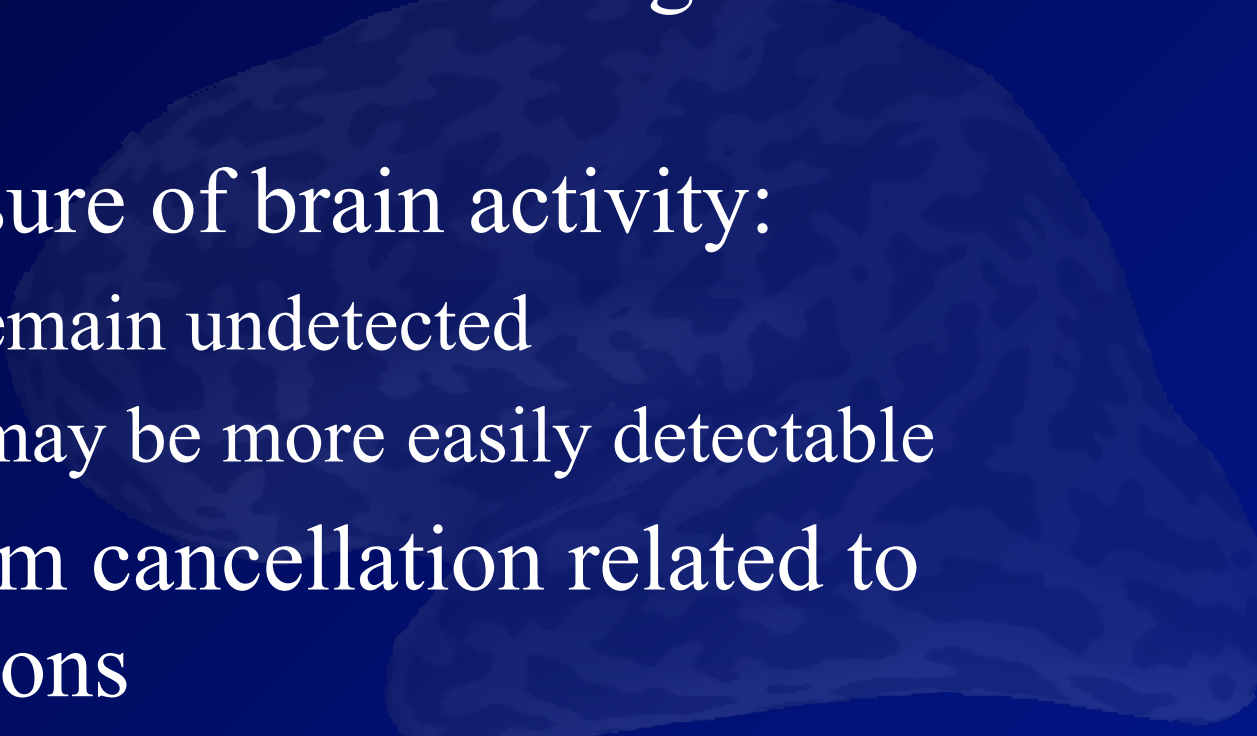
What and Where pathways in the auditory cortex



fMRI weighted MEG estimates to sound pairs which were different in location, phonemic content, or neither



MEG/EEG and fMRI: Similarities and differences

- An ill-posed inverse problem is not involved in fMRI analysis: better spatial resolution
 - MEG/EEG have an exquisite temporal resolution
 - Both fMRI and MEG/EEG are most likely related to LFPs measured at the microscopic level
 - Synchronous activity has an overwhelming contribution to MEG/EEG
 - fMRI is an indirect measure of brain activity:
 - Transient changes may remain undetected
 - Sustained weak activity may be more easily detectable
 - fMRI does not suffer from cancellation related to different source orientations
- 

Why both MEG and EEG?

- Sources at the periphery of the sensor arrays can be estimated better when both modalities are available
- Different cancellation properties for multiple focal sources and extended source patches
- Missing signal in one modality is valuable information for the interpretation of the other
- Initial combined MEG/EEG experiments can provide valuable guidelines for further single-modality (MEG or EEG) large-cohort or clinical studies



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Daniel Wehner
Thomas Witzel

Thank you!