

By rolling a dice you get an exam topic from $\{2, 3, \dots, 7\} \setminus \{x\}$ where x is the topic you may exclude before.

closed folder exam part

open folder exam part

2. Definition of Markov processes

Def 2.1 Markov process,
Thm 2.3 equivalences (without proof)
Def 2.4 transition function

proof of Thm 2.3

3. Existence of a Markov process

Cor 3.3 existence MP

Def 3.1 Thm 3.2

4. Strong Markov Processes

(1) stopping times and optional times

Def 4.1 stopping time,
Def 4.3 right-cont. filtr.,
Def 4.5 $\mathcal{F}_\tau, \mathcal{F}_{\tau+}$,
Def 4.7 optional time

Lemma 4.8

(2) strong Markov property

Def 4.12 strong Markov

Def 4.10, Proposition 4.13

(3) Lévy processes are strong Markov

Def 4.14 Lévy process,
Thm 4.15 strong Markov prop
for Lévy (without proof)

Remark 4.16, proof of Thm 4.15

(4) right-continuous filtrations

Def 4.19 Thm 4.20

5. The semigroup/generator approach

(1) contraction semigroups

Def 5.1 semigroup,
Def 5.2 \mathcal{B}_E

Lemma 5.3 without proof

(2) infinitesimal generator

Def 5.4 infinitesimal generator

Thm 5.6 without proof

(3) Martingales and Dynkin's formula

Def 5.7 martingale

Thm 5.8 with proof

6. Weak solutions of SDEs and martingale problems

Def 6.1, 6.4, Thm 6.5,
Def 6.7, Cor 6.8

7. Feller processes

(1) Feller semigroups, Feller transition functions, Feller processes

Def 7.1, 7.4, 7.6
Prop 7.2 without proof
Prop 7.5 without proof

(2) càdlàg modifications of Feller processes

Def 7.7 Lévy process in law

Thm 7.8 without proof
Lemma 7.9.
Lemma 7.10
Thm 7.11.

Exercises:

-1- (1) (2) (3)(5)

-2- (2) (3) (4)

-3- (1)(2) (3)

-4- (2)(4)(5)

-5- (2) (3)

-6- (2)(3)(4)

-7- coming