Vector Analysis

Spring 2014

Ex Tempore 2

Mon 10.3.

- 1. Write a parametric presentation $\vec{r}(t) = \vec{r}(x(t), y(t), z(t))$ for the curve $y = x^2, z = 0$, where the starting point is (-1,1,0) and the end point is (1,1,0). Draw it. Evaluate the line integral of the vector field $\vec{F} = 5x^2\hat{i} + 6y\hat{j} + 7z\hat{k}$ along this curve.
- 2. Is the field $\vec{F} = 5x^2\hat{i} + 6y\hat{j} + 7z\hat{k}$ conservative? If yes, give the corresponding potential $\phi(x, y, z)$. Evaluate the line integral of \vec{F} from the point (-1,1,0) to the point (1,1,0) along the line connecting the two points.
- 3. Is the field $\vec{F} = 6y\hat{i} + 5x^2\hat{j} + 7z\hat{k}$ conservative?