## Vector Analysis

Spring 2014

## Ex Tempore 2

Mon 10.3.

1. Write a parametric presentation $\vec{r}(t)=\vec{r}(x(t), y(t), z(t))$ for the curve $y=x^{2}, z=0$, where the starting point is $(-1,1,0)$ and the end point is $(1,1,0)$. Draw it. Evaluate the line integral of the vector field $\vec{F}=5 x^{2} \hat{i}+6 y \hat{j}+7 z \hat{k}$ along this curve.
2. Is the field $\vec{F}=5 x^{2} \hat{i}+6 y \hat{j}+7 z \hat{k}$ conservative? If yes, give the corresponding potential $\phi(x, y, z)$. Evaluate the line integral of $\vec{F}$ from the point $(-1,1,0)$ to the point $(1,1,0)$ along the line connecting the two points.
3. Is the field $\vec{F}=6 y \hat{i}+5 x^{2} \hat{j}+7 z \hat{k}$ conservative?
