

Exam 23.10.2013

3. Calculate the amount (mol) and composition (%) of the flue gases with the following input data. Composition of the fuel under consideration (in wt%): C 50 , H 6.3, S 0.1, O 42.5, N 0.1 and the rest is ash. Moisture content 25 wt%. The fuel is combusted with air (21 vol % O₂ and 79 vol % N₂). Assume stoichiometric combustion (no excess air). Use 1 kg of fuel as calculation basis. Useful molecular weights (g/mol) C 12.01, H 1.01, O 16.0, N 14.01, S 32.07, CO₂ 44.01, H₂O 18.02, O₂ 32.0, N₂ 28.01, SO₂ 64.07. (5 p.)
4. a) Considering the previous problem (3), calculate the average temperature of the flue gases, using the following input values: Fuel loose density 300 kg/m³, Heating value (as received) 14.01 MJ/kg, moisture 25 %. Wood is burned with air with the air factor 1.2. The temperature of air at inlet is 200 °C. Fuel is assumed to be at the reference temperature 25 °C. Heat loss from the combustor walls is 5 % of the thermal capacity. The capacity of the combustor is 1 MW_{th}. (4 p.)

Averaged specific heat constants (J/molK) CO₂ 51.7, H₂O 41.7, O₂ 32.0, N₂ 31.0, SO₂ 52.1

SOLUTION

Gas composition from the material balance:

Flowrates of species in and out

Fuel in (mol)	Flue gases out (mol)	vol %
C: $0.5 \cdot 1000 \cdot (1-0.25)/12.01 = 31.22$	CO ₂ : 31.22	16.2
H: $0.063 \cdot 1000 \cdot (1-0.25)/1.01 = 46.78$	H ₂ O: $46.78/2 + 13.87 = 37.26$	19.35
O: $0.425 \cdot 1000 \cdot (1-0.25)/16.0 = 19.92$	O ₂ : $32.98 + 19.92/2 - 42.94 = 0$	0
N: $0.001 \cdot 1000 \cdot (1-0.25)/14.01 = 0.053$	N ₂ : $124.07 + 0.053/2 = 124.1$	64.43
S: $0.001 \cdot 1000 \cdot (1-0.25)/32.07 = 0.023$	SO ₂ : 0.023	0.012
Ash: $0.01 \cdot 1000 \cdot (1-0.25) = 7.5$ g		
Water: $0.25 \cdot 1000/18.02 = 13.87$		
St. O₂: $31.22 + 0.5 \cdot 46.78/2 + 0.023 = 42.94$	Flue gases total 192.6	
O ₂ (air) = $1.0 \cdot 42.94 - 19.92/2 = 32.98$ (*)		
N ₂ (air) = $79/21 \cdot 32.98 = 124.07$	Ash: 7.5 g	

*) Stoichiometric combustion (no excess air): $\lambda = 1.0$

$\lambda = (n_{O_2,A} + n_{O_2,f}) / n_{O_2,St.} \rightarrow n_{O_2,A} = \lambda \cdot n_{O_2,St.} - n_{O_2,f} = 1.0 \cdot 3.07 - 1.42/2 = 2.36$ mol/s

Flue gas temperature from the energy balance:

Calculation basis the fuel heating value

Fuel heating value as fed (MJ/kg) = 14.01

\rightarrow Fuel feed 1 MJ/s / (14.01 MJ/kg) * 1000 g/kg = 71.38 g/s

Or if you have used 1 kg of fuel as basis, that is also ok.

Combustor heat loss: $0.05 \cdot 1$ MW = 0.05 MW = 5E4 J/s

Energy flowrates of species in and out

Fuel in (J/s) at reference temperature	Flue gases out (J/s)
C: $n_C \cdot c_p \cdot (298.15 - 298.15) = 0$	CO ₂ : $2.23 \cdot 51.7 \cdot (T_2 - 298.15) = ?$
H: $n_H \cdot c_p \cdot (298.15 - 298.15) = 0$	H ₂ O: $2.66 \cdot 41.7 \cdot (T_2 - 298.15) = ?$
O: $n_O \cdot c_p \cdot (298.15 - 298.15) = 0$	O ₂ : $0.614 \cdot 32 \cdot (T_2 - 298.15) = ?$
N: $n_N \cdot c_p \cdot (298.15 - 298.15) = 0$	N ₂ : $11.19 \cdot 31 \cdot (T_2 - 298.15) = ?$
S: $n_S \cdot c_p \cdot (298.15 - 298.15) = 0$	SO ₂ : $0.002 \cdot 52.1 \cdot (T_2 - 298.15) = ?$
Ash: $n \cdot c_p \cdot (298.15 - 298.15) = 0$	
Water: $n_{H_2O} \cdot c_p \cdot (298.15 - 298.15) = 0$	
Fuel combustion energy 1.0E6	H _{Ash} ≈ 0
Air feed:	
O ₂ = $2.36 \cdot 32 \cdot (473.15 - 298.15) = 1.32E4$	
N ₂ = $8.88 \cdot 31 \cdot (473.15 - 298.15) = 4.82E4$	H _{loss} = 5E4

Now Energy in = Energy out (J/s)

$$H_{\text{Fuel}} + H_{\text{combustion}} + H_{\text{Air}} = \Sigma H_{\text{gases}} + H_{\text{ash}} + H_{\text{loss}}$$

$$\rightarrow 0 + 1\text{E}6 + 1.32\text{E}4 + 4.82\text{E}4 = 2.23*51.7*(T_2-298.15) + 2.66*41.7*(T_2-298.15) + 0*32*(T_2-298.15) + 8.88*31*(T_2-298.15) + 0.002*52.1*(T_2-298.15) + 0 + 5\text{E}4$$

$$\rightarrow T_2 = 1011400/501.6 + 298.15 = 2314.5 \text{ K} = 2041.3 \text{ }^\circ\text{C}$$